

Active Learning Beyond Label Feedback

Kamalika Chaudhuri

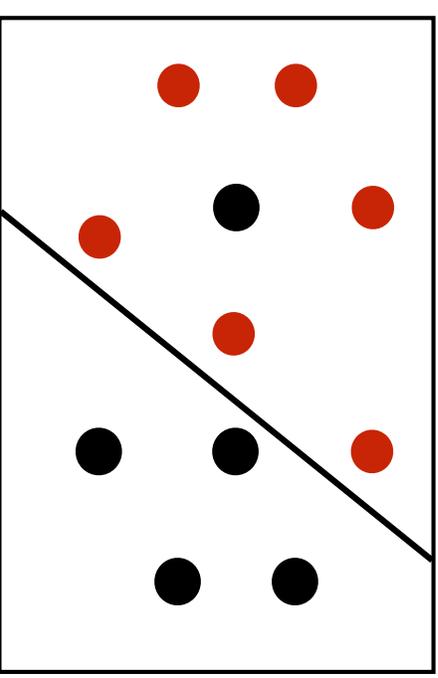
University of California, San Diego

Joint work with **Chicheng Zhang,**
Tara Javidi and **Songbai Yan**

Classification

Given: (x_i, y_i)

Vector of features Discrete Labels



Find: Prediction rule in a class to predict y from x

Challenge: Acquiring Labeled Data

Unlabeled data
is cheap



Labels are
expensive



Active Learning

Given: (x_i, y_i)

Find: Prediction rule to predict y from x

Active Learning

Given: $(x_i, \text{---} y_i \text{---})$

Interactive
Label Queries

Find: Prediction rule to predict y from x

Active Learning

Given: $(x_i, \text{---} y_i \text{---})$

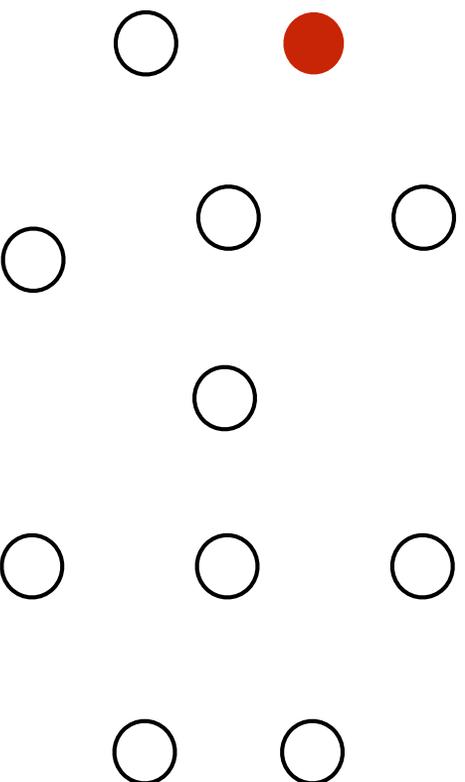
Interactive
Label Queries

Find: Prediction rule to predict y from x
using few label queries

Why Active Learning Helps?

Given: Unlabeled data, interactive label queries

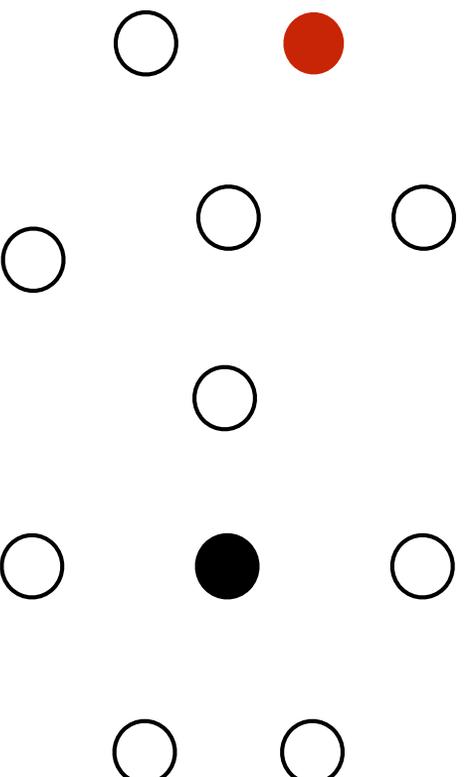
Find: Good prediction rule using few label queries



Why Active Learning Helps?

Given: Unlabeled data, interactive label queries

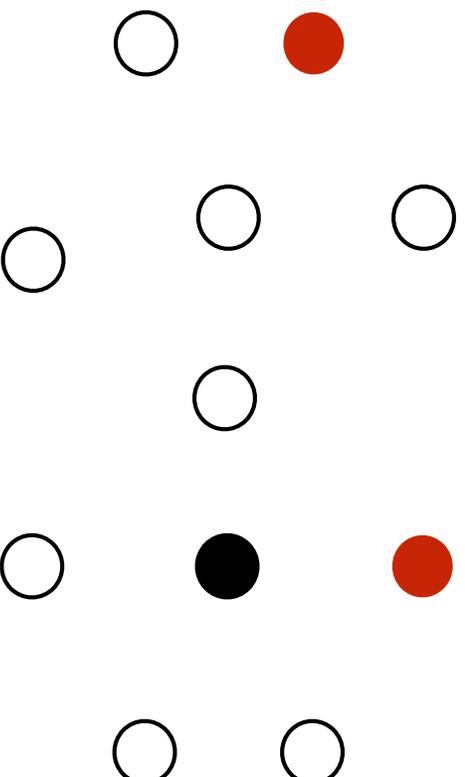
Find: Good prediction rule using few label queries



Why Active Learning Helps?

Given: Unlabeled data, interactive label queries

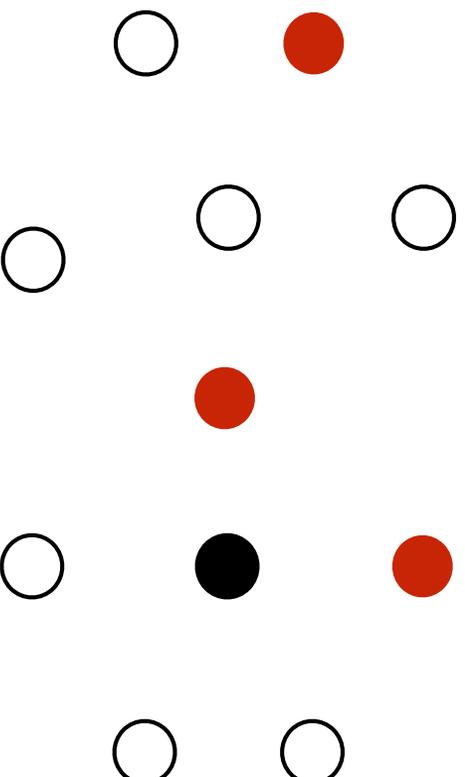
Find: Good prediction rule using few label queries



Why Active Learning Helps?

Given: Unlabeled data, interactive label queries

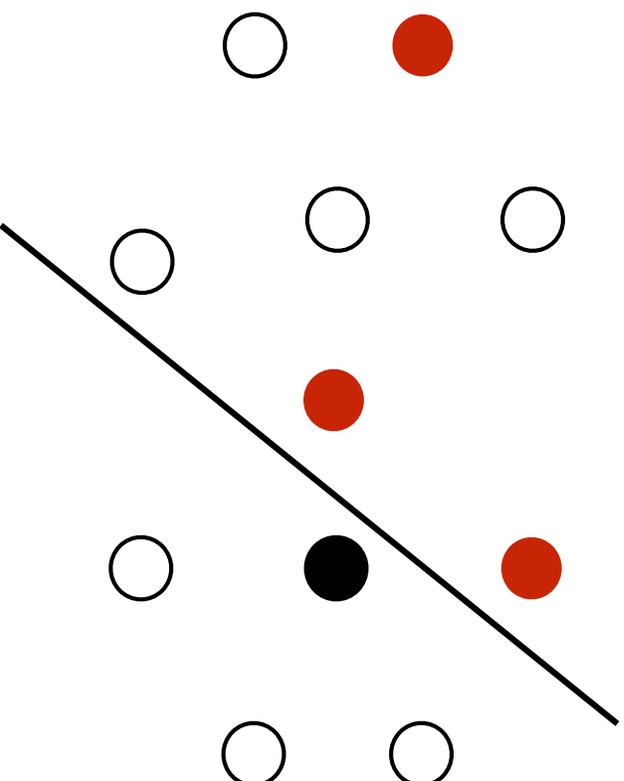
Find: Good prediction rule using few label queries



Why Active Learning Helps?

Given: Unlabeled data, interactive label queries

Find: Good prediction rule using few label queries



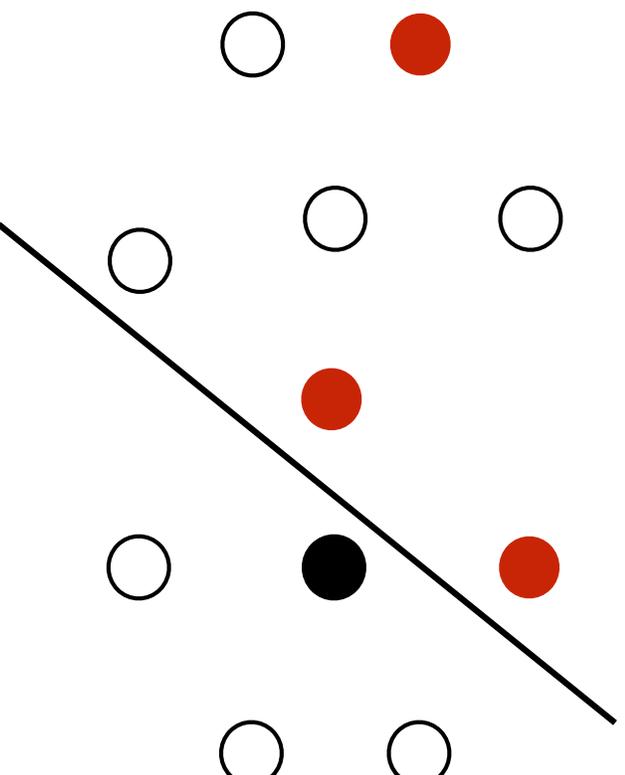
Challenge: “Incorrect” Responses

What makes *Active Learning* Hard?

Given: Unlabeled data, interactive label queries

No assumptions on data distribution

Find: Good prediction rule using few label queries

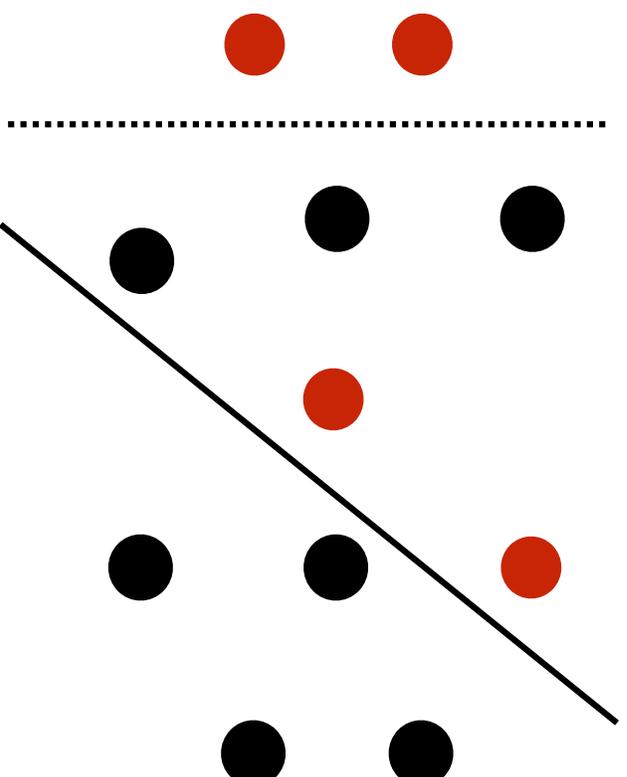


What makes *Active Learning* Hard?

Given: Unlabeled data, interactive label queries

No assumptions on data distribution

Find: Good prediction rule using few label queries



Statistically inconsistent!

Talk Agenda

Can other kinds of queries help active learning?

This talk:

1. Weak and strong labelers
2. Abstaining labelers

Talk Outline

I. Weak and Strong Labelers

- the model

Probably Approx. Correct (PAC) Model

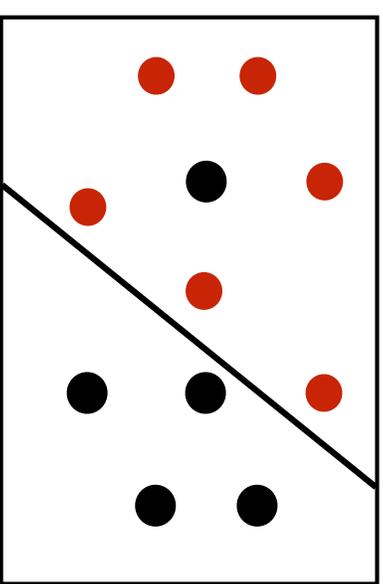
Given: Concept class C

Samples (x_i, y_i) from data distribution D

Example: $C =$ linear classifiers

Find: c in C with low

$$\Pr_{(x,y) \sim D} (c(x) \neq y)$$



Probably Approx. Correct (PAC) Model

Given: Concept class C

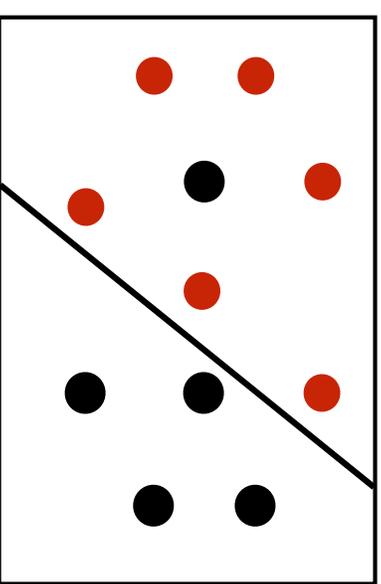
Samples (x_i, y_i) from data distribution D

Example: $C =$ linear classifiers

Find: c in C with low

$$\Pr_{(x,y) \sim D} (c(x) \neq y)$$

Error

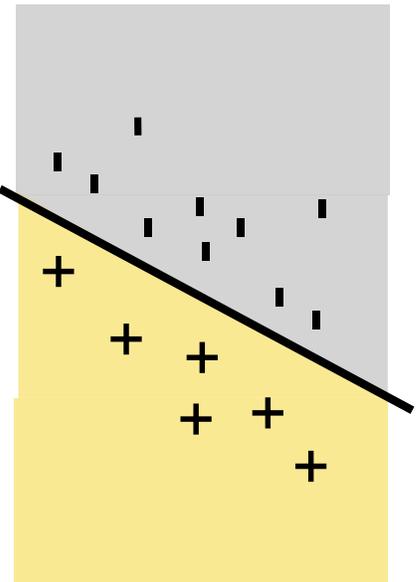


PAC Model: Realizable vs. Agnostic

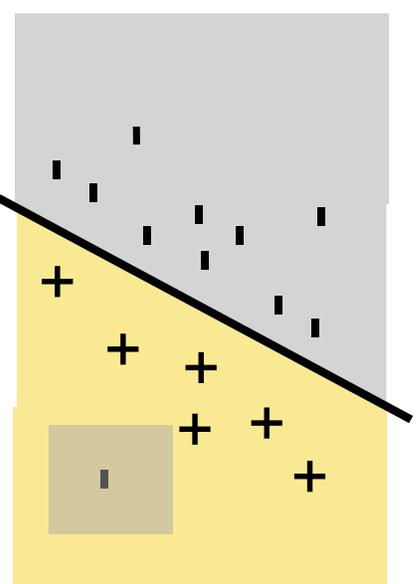
Given: Concept class C , Samples (x_i, y_i) from D

Find: c in C with low error

Realizable



Agnostic



$\exists c^* \in C$ such that

$$c^*(x) = y, \forall (x, y) \sim D$$

No Assumptions
on D

Agnostic Active Learning

Given: Concept class C (best c in C has error ν^*)

$(x_i, \text{---} y_i \text{---})$ drawn from D

Interactive
Label Queries

Find: c in C with error $\leq \nu^* + \epsilon$
using few label queries
with no assumptions on D

Methods for Agnostic Active Learning

- Disagreement-based Active Learning [CAL94, BBL06, H07, DHM07, many others]
- Margin/Confidence-based Active Learning [BZ07, BL13, ABL14, ZC14]
- Clustering-based Active Learning [DH08, UWBI3]

This work: based on disagreement-based active learning

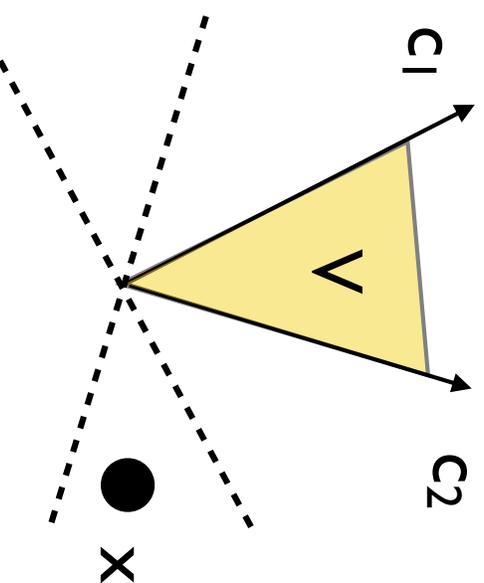
Disagreement-based Active Learning

1. Maintain candidate set V (that contains best c in C)
2. For unlabeled x , if there exist c_1, c_2 in V s.t

$$c_1(x) \neq c_2(x)$$

then, x is in **disagreement region** of V

Query label of x , and update V



[CAL94, BBL06, DHM07,
H07, BDL09, BHLZ10, ...]

What if we have auxiliary information?

..as an extra oracle

Oracle and Weak Labeler

Oracle:
expensive but correct



Weak labeler:
cheap, sometimes wrong



The Model

Given: $(x_i, \text{---} y_i)$

Interactive

Label Queries

The Model

Given: $(x_i, \text{---} y_i \text{---})$

Interactive
Label Queries to

Oracle O or
Weak Labeler W

The Model

Given: $(x_i, \text{---} y_i \text{---})$

Interactive
Label Queries to

Oracle O or
Weak Labeler W

Find: Prediction rule to predict y from x
using few label queries to O

Formal Model

Given: Concept class C (best c has error ν^* wrt \mathcal{O})

$(x_i, \text{---}y_i\text{---})$ drawn from D

Formal Model

Given: Concept class C (best c has error ν^* wrt O)

$(x_i, \text{---}y_i\text{---})$ drawn from D

Oracle O and Weak labeler W

Formal Model

Given: Concept class C (best c has error ν^* wrt \mathcal{O})

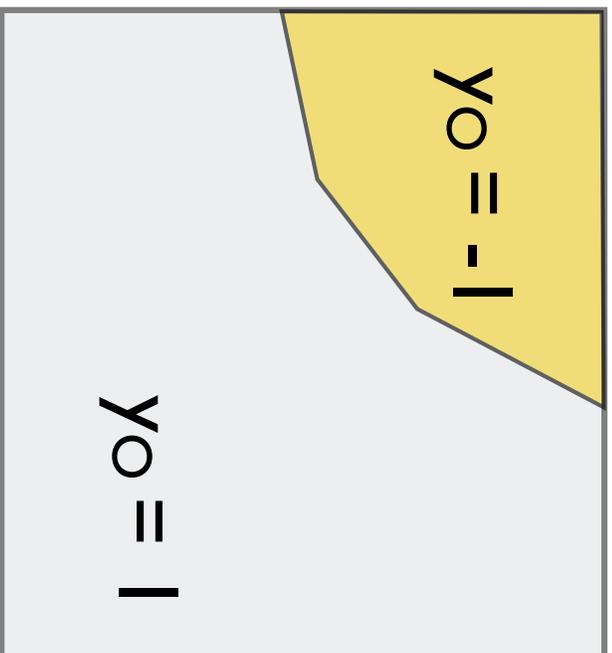
$(x_i, \text{---}y_i\text{---})$ drawn from D

Oracle \mathcal{O} and Weak labeler W

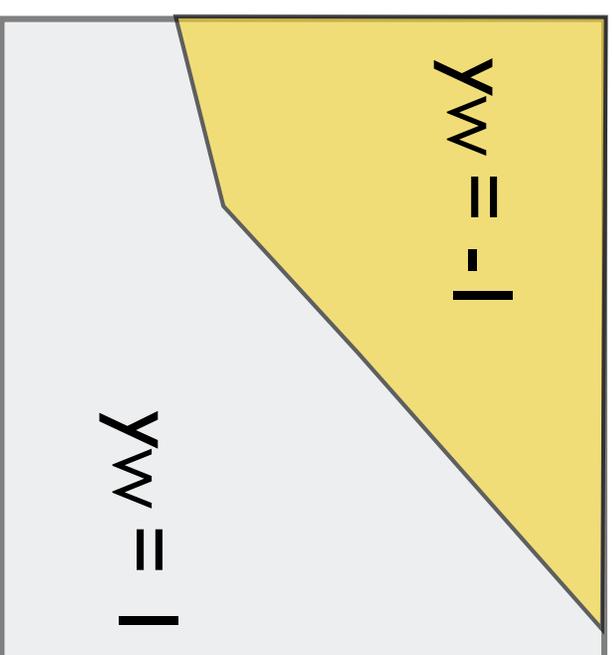
Find: c in C with error $\leq \nu^* + \epsilon$ wrt \mathcal{O}
using minimum label queries to \mathcal{O}

Formal Model Implications

Weak labeler W may be biased



Labels by O



Labels by W

Previous Work

[UBS12] Explicit assumptions on where W and O differ
(close to decision boundaries)

[MCR14] No explicit assumptions, but applies to online
selective classification and robust regression

This talk: General learning strategy from W and O
with no explicit assumptions

Talk Outline

I. Weak and Strong Labelers

- the model
- algorithm

How to learn in this model?

Main Ideas:

Learn a **difference classifier** h to predict
when O and W differ

How to learn in this model?

Main Ideas:

Learn a **difference classifier** h to predict when O and W differ

Use h with standard active learning to decide if we should query O or W

Algorithm Outline

1. Draw x_1, \dots, x_m . For each x_i , query O and W . Set:

$$y_{i,D} = 1 \quad \text{if} \quad y_{i,O} \neq y_{i,W}$$

Algorithm Outline

1. Draw x_1, \dots, x_m . For each x_i , query O and W . Set:

$$y_{i,D} = 1 \quad \text{if} \quad y_{i,O} \neq y_{i,W}$$

2. Train **difference classifier** h in H on $\{(x_i, y_{i,D})\}$

Algorithm Outline

1. Draw x_1, \dots, x_m . For each x_i , query O and W . Set:

$$y_{i,D} = 1 \quad \text{if} \quad y_{i,O} \neq y_{i,W}$$

2. Train **difference classifier** h in H on $\{ (x_i, y_{i,D}) \}$

3. Run standard disagreement based active learning algorithm A . If A queries the label of x then:
if $h(x) = 1$, query O , else query W

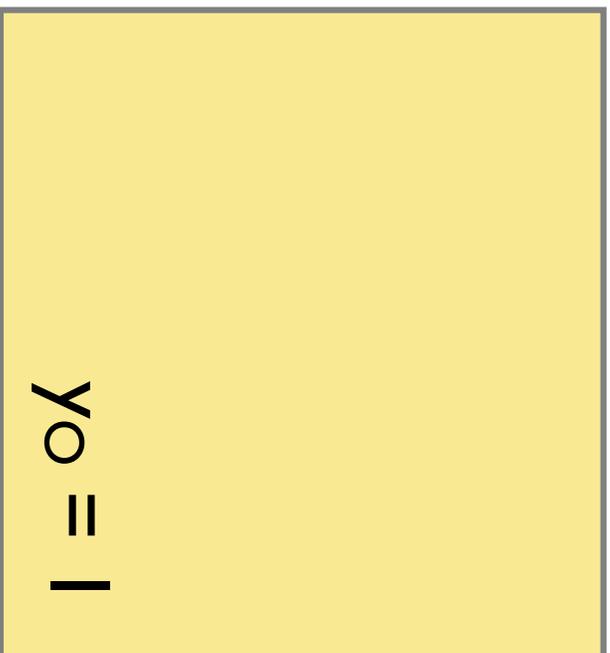
Algorithm Outline

1. Draw x_1, \dots, x_m . For each x_i , query O and W . Set:
$$y_{i,D} = 1 \quad \text{if} \quad y_{i,O} \neq y_{i,W}$$
2. Train **difference classifier** h in H on $\{ (x_i, y_{i,D}) \}$
3. Run standard disagreement based active learning algorithm A . If A queries the label of x then:
if $h(x) = 1$, query O , else query W

Is this statistically consistent?

Key Observation I

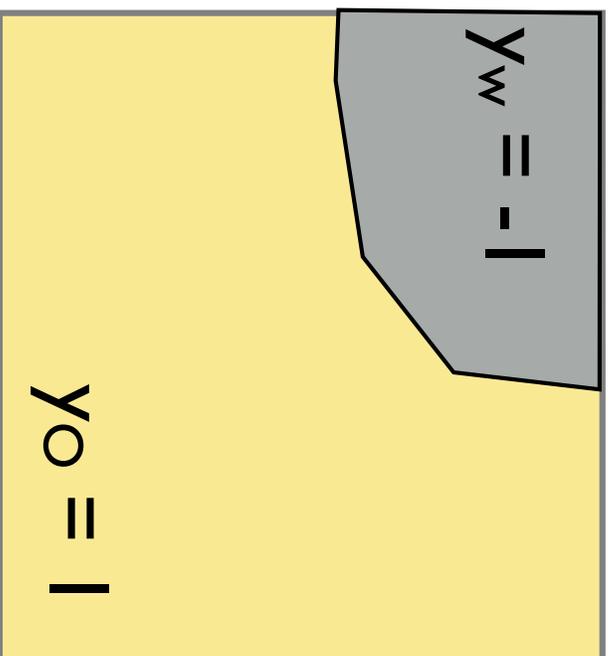
Directly learning difference classifier may lead to inconsistent annotation on target task



Actual Labels

Key Observation I

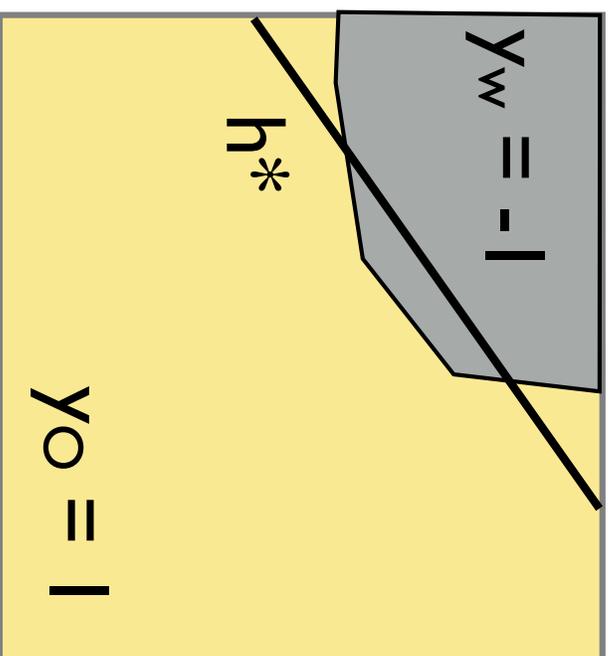
Directly learning difference classifier may lead to inconsistent annotation on target task



Actual Labels

Key Observation I

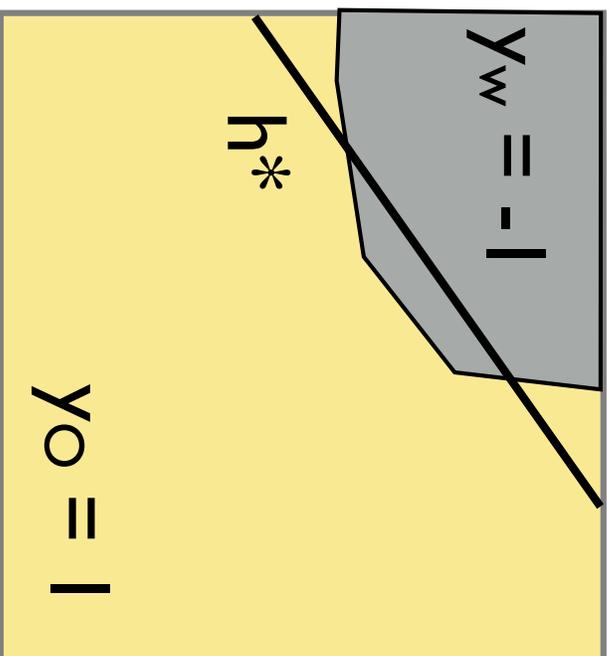
Directly learning difference classifier may lead to inconsistent annotation on target task



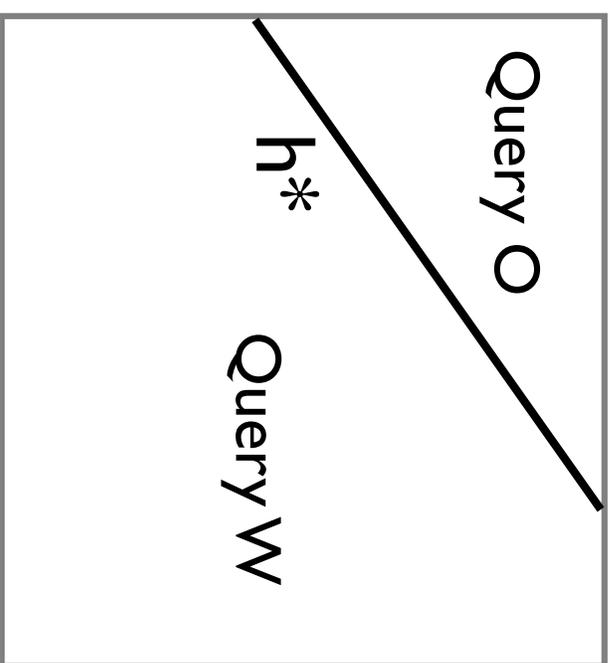
Actual Labels

Key Observation I

Directly learning difference classifier may lead to inconsistent annotation on target task



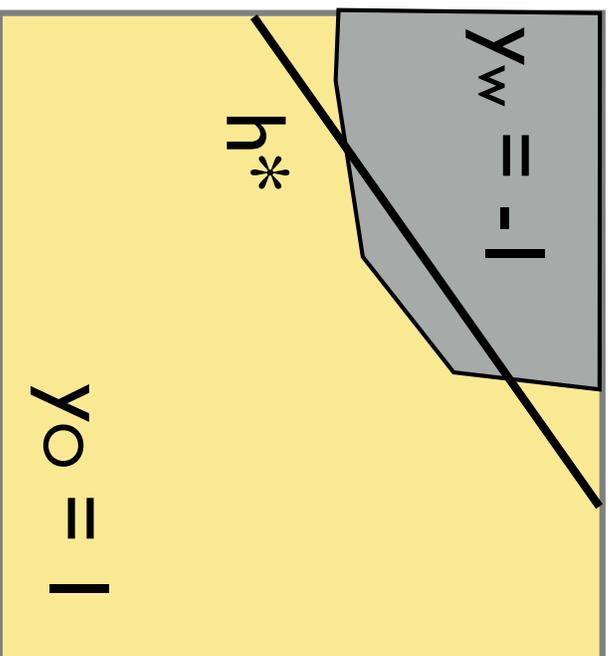
Actual Labels



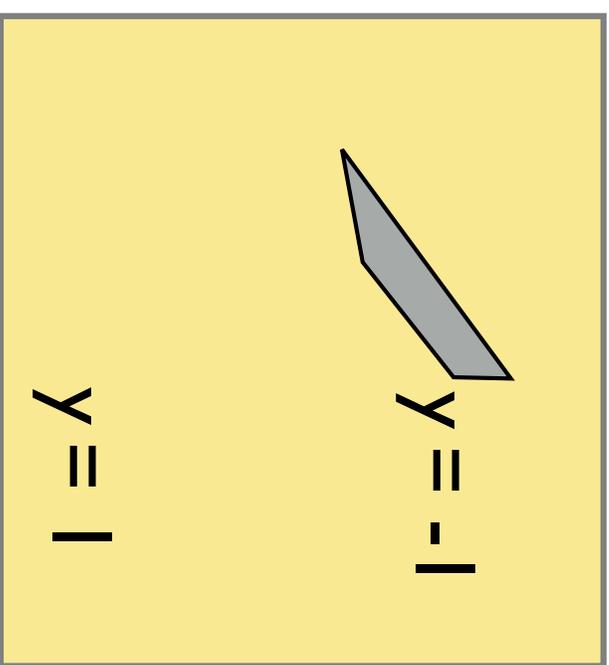
Annotation using h^*
as difference classifier

Key Observation I

Directly learning difference classifier may lead to inconsistent annotation on target task



Actual Labels

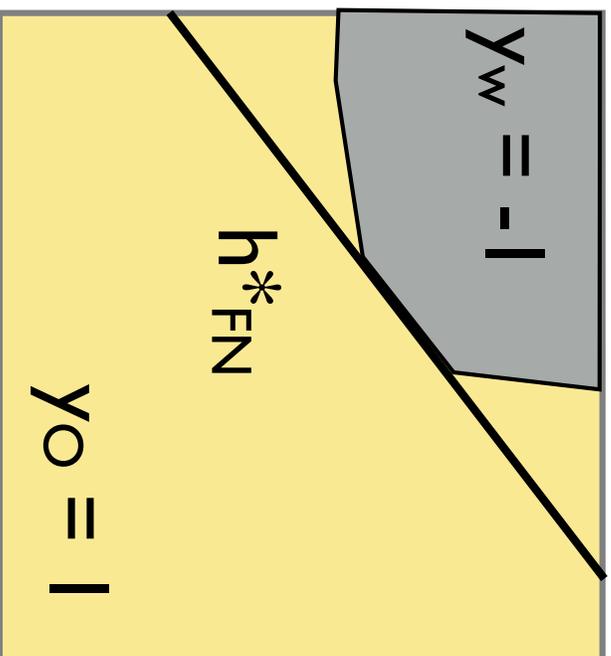


Annotation using h^*
as difference classifier

Solution

Train a **cost-sensitive** difference classifier

Constrain False Negative (FN) rate as very low

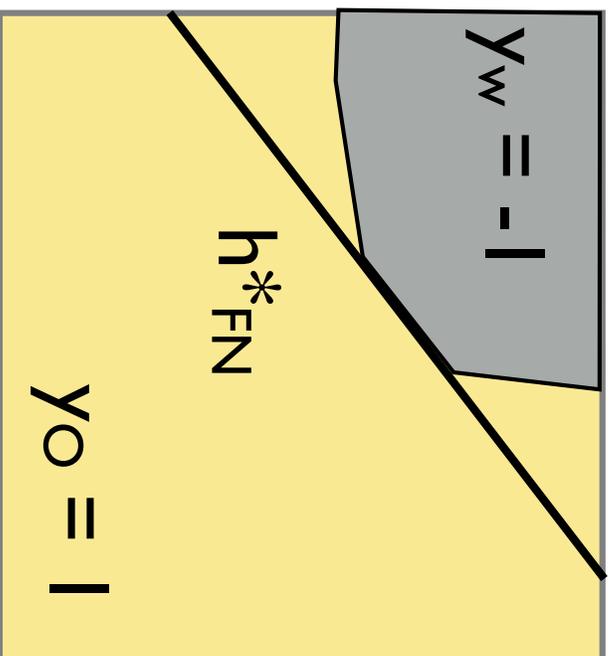


Actual Labels

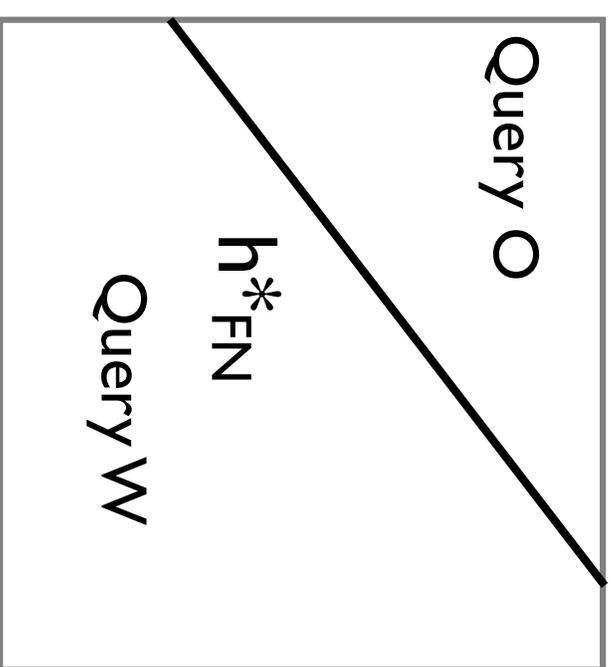
Solution

Train a **cost-sensitive** difference classifier

Constrain False Negative (FN) rate as very low



Actual Labels

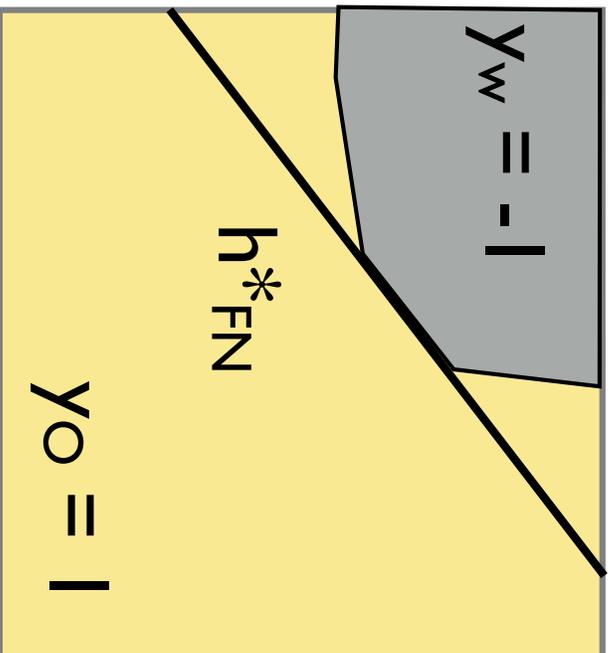


Annotation using h^*_{FN}
as difference classifier

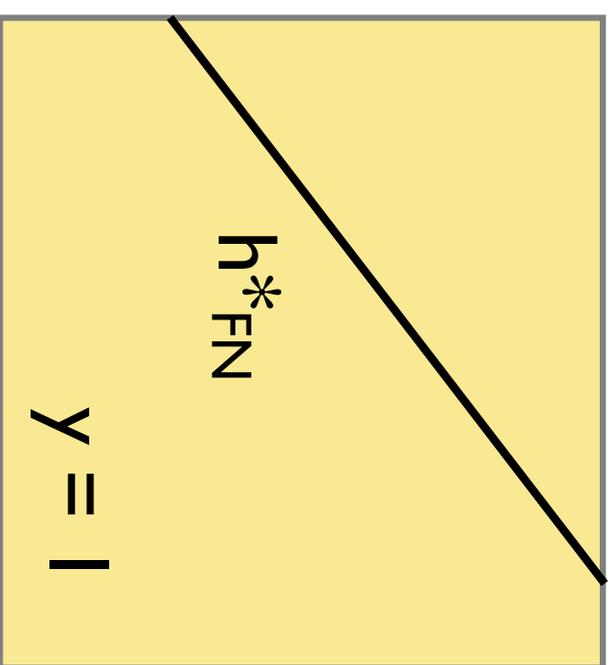
Solution

Train a **cost-sensitive** difference classifier

Constrain False Negative (FN) rate as very low



Actual Labels



Annotation using h_{FN}^*
as difference classifier

Algorithm Outline

1. Draw x_1, \dots, x_m . For each x_i , query O and W . Set:

$$y_{i,D} = 1 \quad \text{if} \quad y_{i,O} \neq y_{i,W}$$

2. Train difference classifier h in H on $\{(x_i, y_{i,D})\}$ with false negative (FN) rate $\leq \epsilon$

3. Run standard disagreement based active learning algorithm A . If A queries the label of x then:
if $h(x) = 1$, query O , else query W

Theorem: This is statistically consistent

Talk Outline

I. Weak and Strong Labelers

- the model
- algorithm
- analysis

What about label complexity?

Label complexity = #label queries to \mathcal{O}

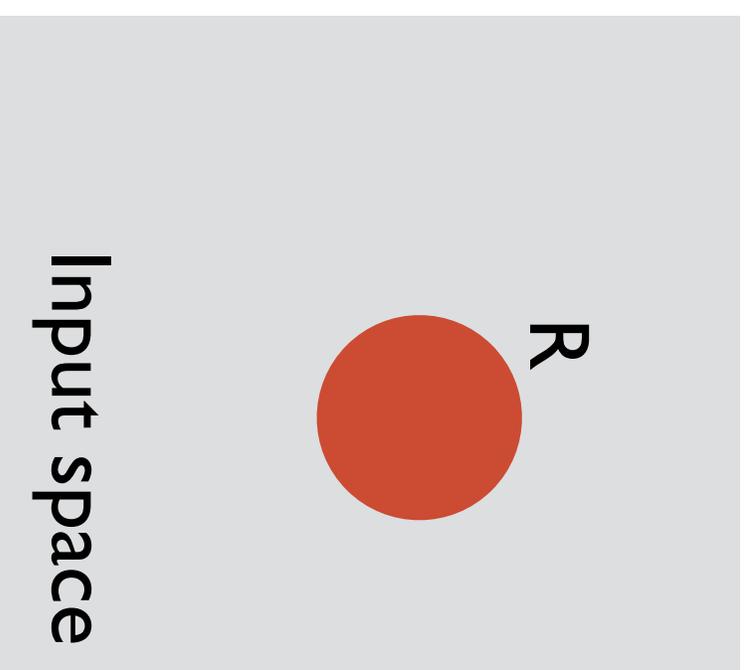
#labels to train difference classifier $\approx \tilde{O}\left(\frac{d'}{\epsilon}\right)$

(d' = VCdim(H), ϵ = target excess error)

Can we do better?

Key Observation 2

R = disagreement region of current confidence set

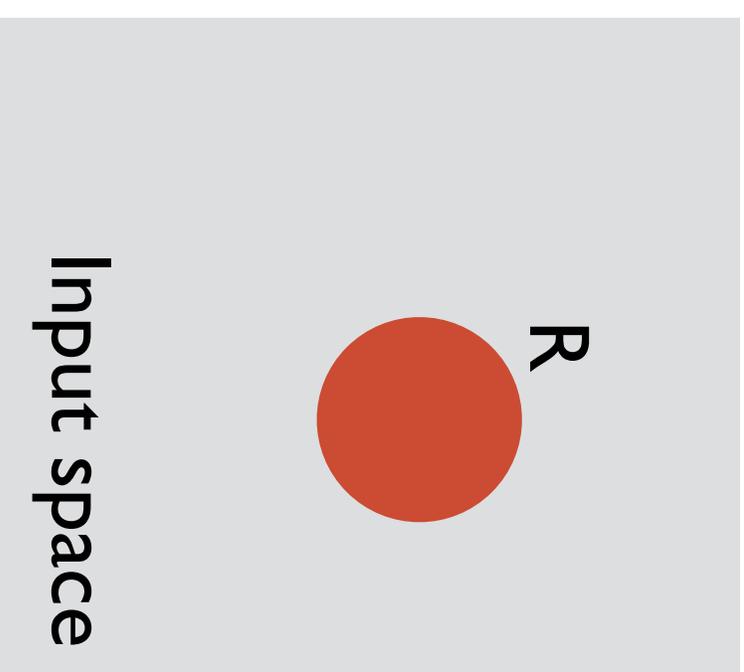


Key Observation 2

R = disagreement region of current confidence set

Need to learn difference
classifier with FN rate

$$\leq \epsilon / \Pr(R) \text{ over } R$$



Input space

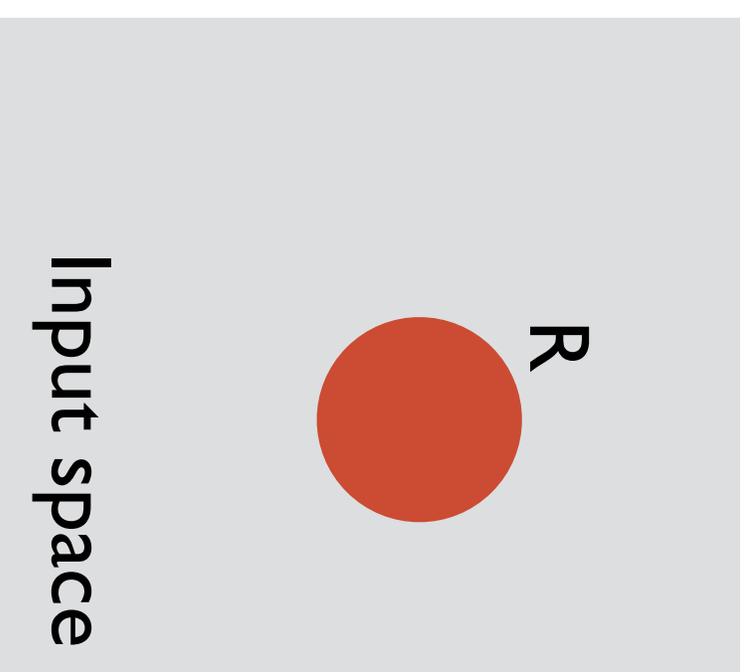
Key Observation 2

R = disagreement region of current confidence set

Need to learn difference classifier with FN rate

$\leq \epsilon / \Pr(R)$ over R

Need $\approx \tilde{O}\left(\frac{d' \Pr(R)}{\epsilon}\right)$ labels



Key Observation 2

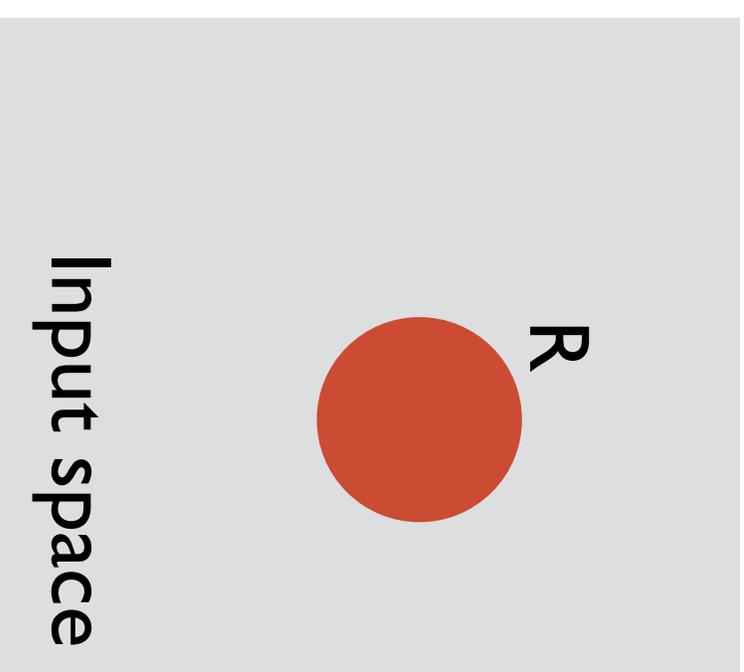
R = disagreement region of current confidence set

Need to learn difference classifier with FN rate

$\leq \epsilon / \Pr(R)$ over R

Need $\approx \tilde{O}\left(\frac{d' \Pr(R)}{\epsilon}\right)$ labels

Problem: R keeps changing, so have to retrain



Full Algorithm

H = difference concept class, $d' = VCdim(H)$

For epochs $1, 2, 3, \dots$

Full Algorithm

H = difference concept class, $d' = VCdim(H)$

For epochs $1, 2, 3, \dots$

Epoch k : target excess error $\epsilon_k \approx 1/2^k$

Confidence set V_k , with disagreement region $DIS(V_k)$

Full Algorithm

H = difference concept class, $d' = VCdim(H)$

For epochs $1, 2, 3, \dots$

Epoch k : target excess error $\epsilon_k \approx 1/2^k$

Confidence set V_k , with disagreement region $DIS(V_k)$

Draw $\tilde{O}(d' \Pr(DIS(V_k)) / \epsilon_k)$ samples x_1, \dots, x_m from $DIS(V_k)$.

Query O and W for each x_i and train a difference classifier h .

Full Algorithm

H = difference concept class, $d' = VCdim(H)$

For epochs $1, 2, 3, \dots$

Epoch k : target excess error $\epsilon_k \approx 1/2^k$

Confidence set V_k , with disagreement region $DIS(V_k)$

Draw $\tilde{O}(d' \Pr(DIS(V_k)) / \epsilon_k)$ samples x_1, \dots, x_m from $DIS(V_k)$.

Query O and W for each x_i and train a difference classifier h .

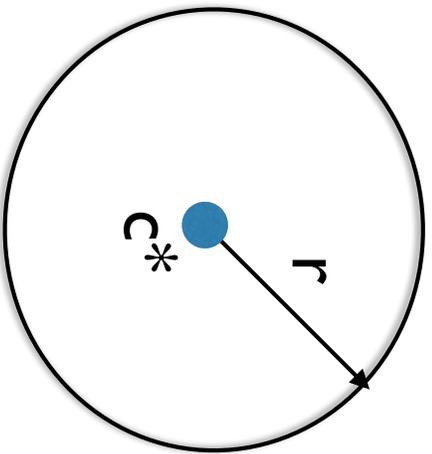
Run disagreement based active learning algorithm A to target excess error ϵ_k . If A queries the label of x then:

if $h(x) = 1$, query O , else query W

Label Complexity: Definitions

Disagreement Region $DIS(V)$ of a set V :

All x such that there exist c_1 and c_2 in V s.t. $c_1(x) \neq c_2(x)$



$B_D(c^*, r)$

Disagreement Coefficient:

$$\theta(r) = \sup_{r' \geq r} \frac{\Pr(DIS(B_D(c^*, r'))) }{r'}$$

(Rate of change of disagreement region as r changes)

Label Complexity

Total #labels to train difference classifier $\approx \tilde{O} \left(\frac{d'_{\theta}(v^* + \epsilon)}{\epsilon} \right)$

How many labels for the rest of active learning?

Label Complexity: Assumptions

For any r, t , there is a h in H such that:

$$\Pr(h(x) = -1, x \in DIS(B(c^*, r), y_0 \neq y_W)) \leq t$$

(Low FN over disagreement region)

$$\Pr(h(x) = 1, x \in DIS(B(c^*, r))) \leq \alpha(r, t)$$

(Low positives)

Note: $\alpha(r, t) \leq \Pr(DIS(B(c^*, r)))$

Label Complexity

#labels to train difference classifier $\approx \tilde{O}\left(\frac{d_{\theta}(v^* + \epsilon)}{\epsilon}\right)$

#labels for active learning $\approx \tilde{O}\left(\frac{d_{\sigma}(v^*)^2}{\epsilon^2}\right)$

$$\text{where: } \sigma \approx \frac{\alpha(2v^* + \epsilon, O(\epsilon))}{2v^* + \epsilon} \leq \theta$$

Compare:

#labels for disagreement based active learning: $\approx \tilde{O}\left(\frac{d_{\theta}(v^*)^2}{\epsilon^2}\right)$

Talk Outline

1. Weak and Strong Labelers

- the model
- algorithm
- analysis

2. Abstentions

- the model



x



Labeler abstains on more difficult examples



x

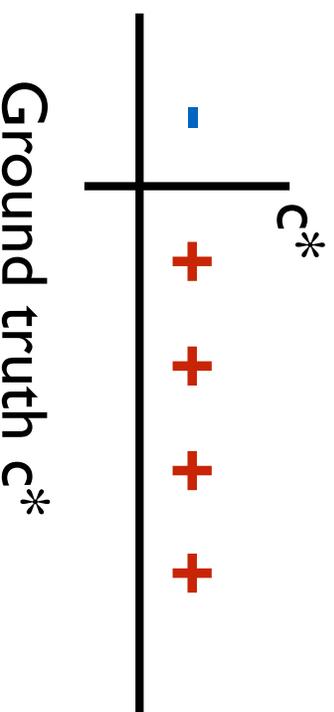


Labeler abstains on more difficult examples

Can we exploit abstentions to learn better?

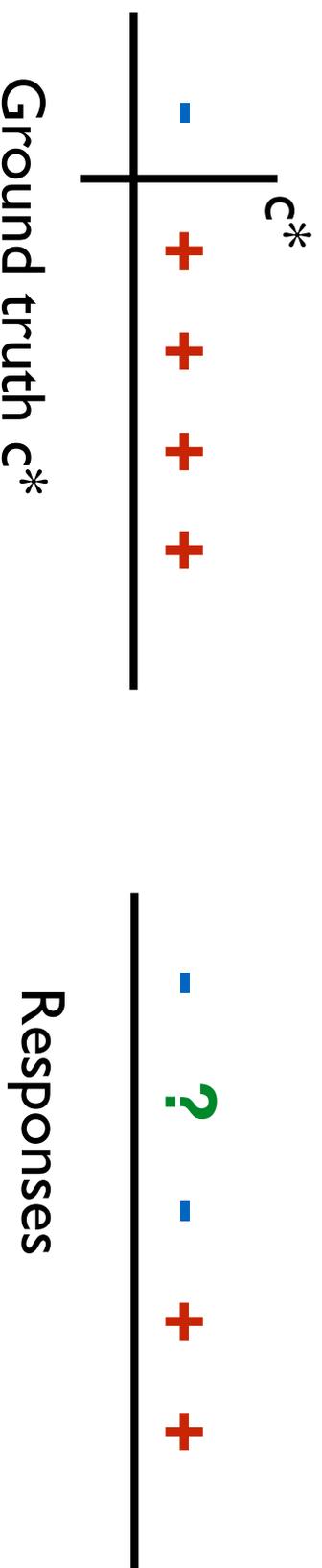
Example: Learning Thresholds

Concept class $C =$ thresholds, instance space $X = [0, 1]$



Example: Learning Thresholds

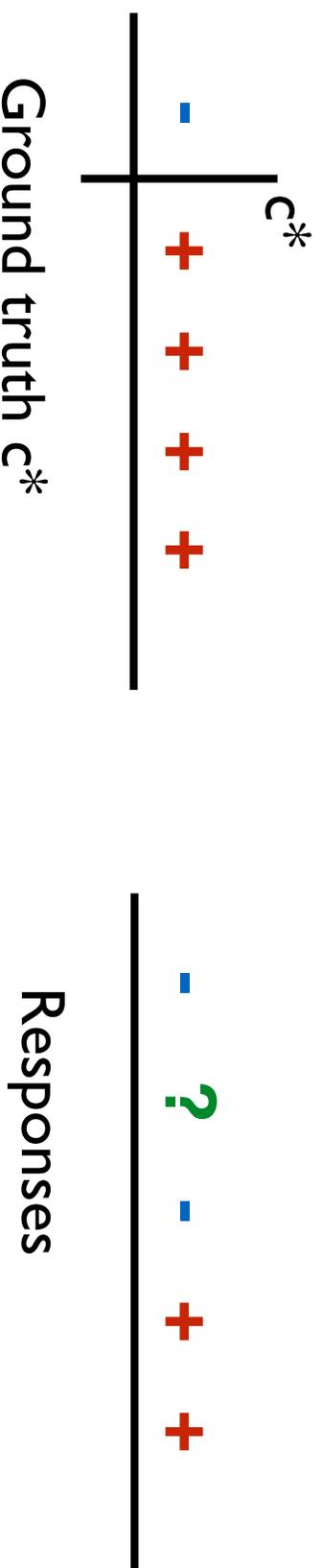
Concept class $C =$ thresholds, instance space $X = [0, 1]$



Learner can query any x in X

Example: Learning Thresholds

Concept class $C =$ thresholds, instance space $X = [0, 1]$

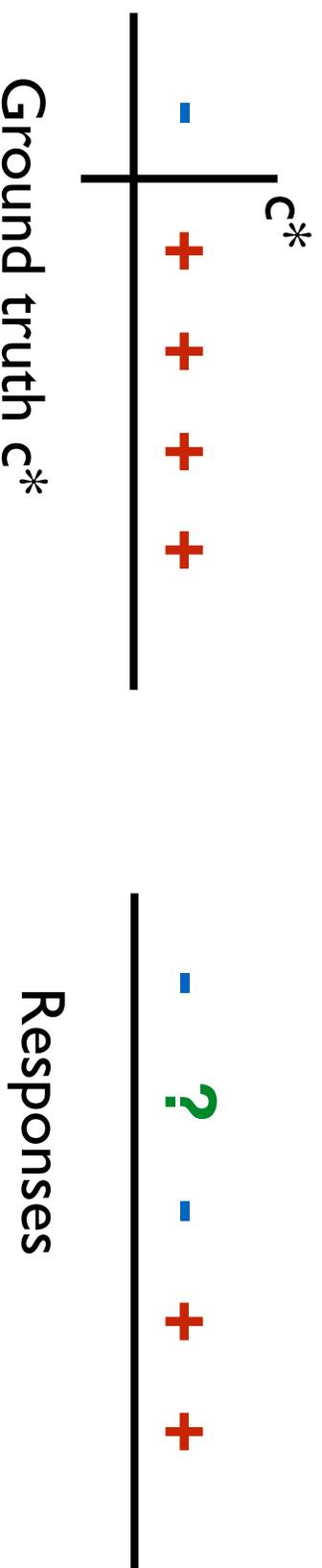


Learner can query any x in X

Responses $+$, $-$, $?$ drawn from unknown $P(Y|x)$

Example: Learning Thresholds

Concept class $C =$ thresholds, instance space $X = [0, 1]$



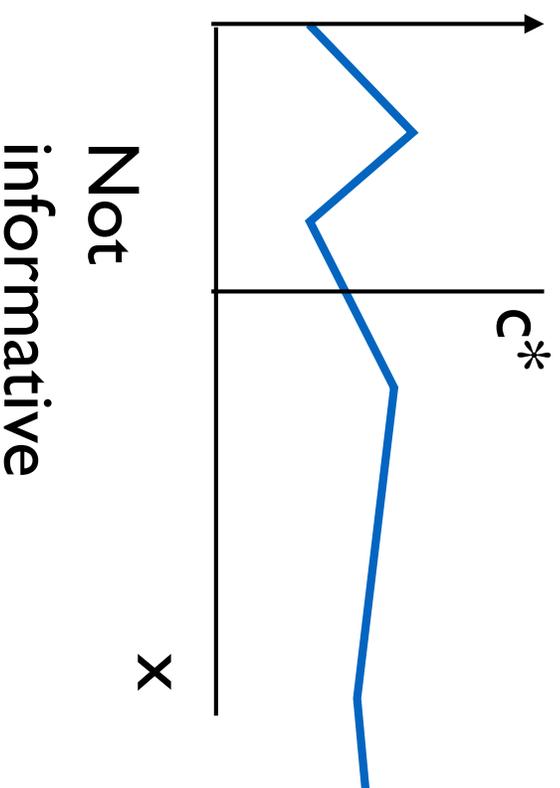
Learner can query any x in X

Responses $+$, $-$, $?$ drawn from unknown $P(Y|x)$

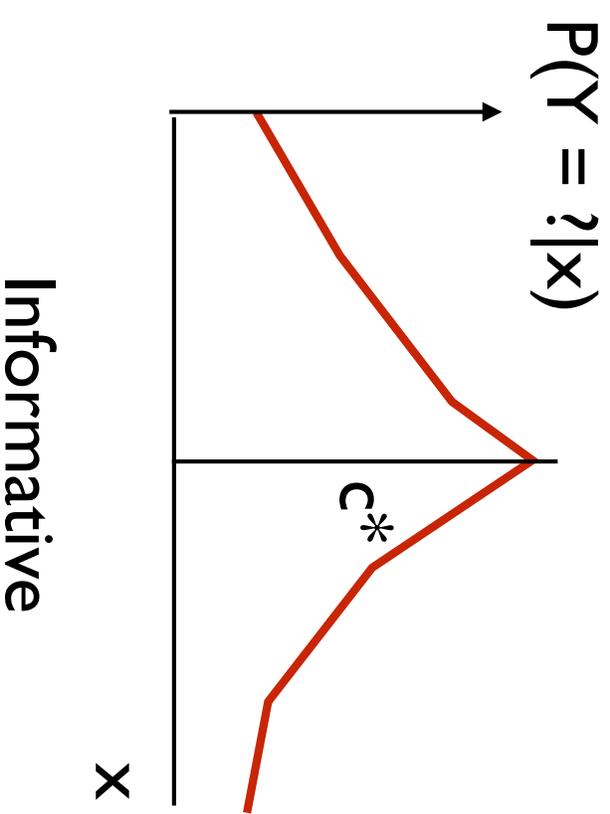
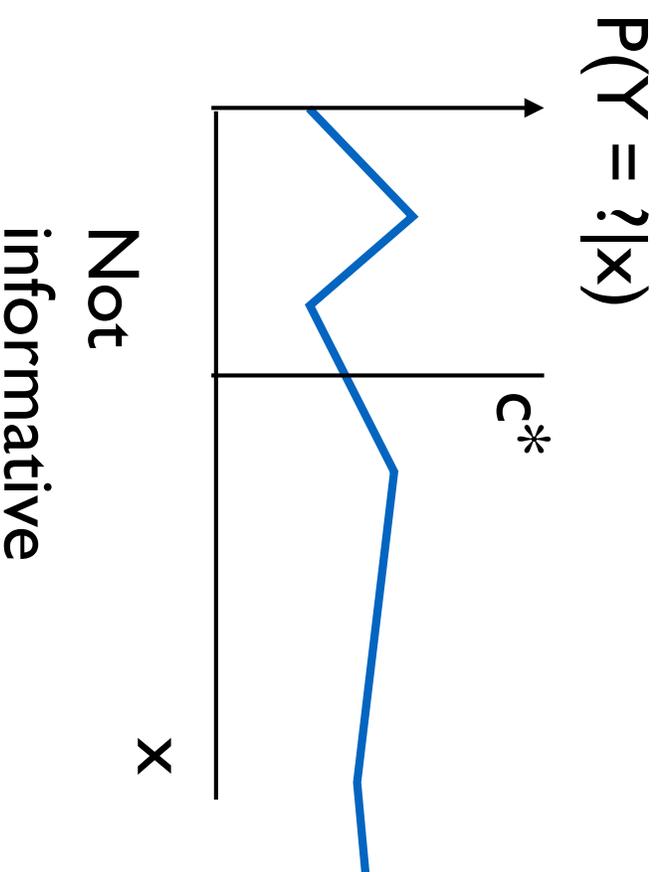
Goal: Find c s.t. $|c - c^*| \leq \epsilon$ with min # queries

When can abstentions help?

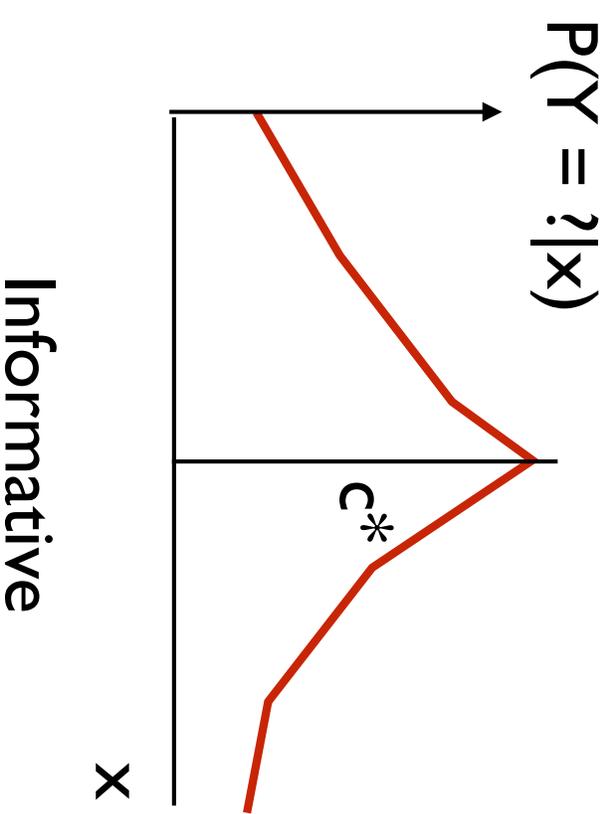
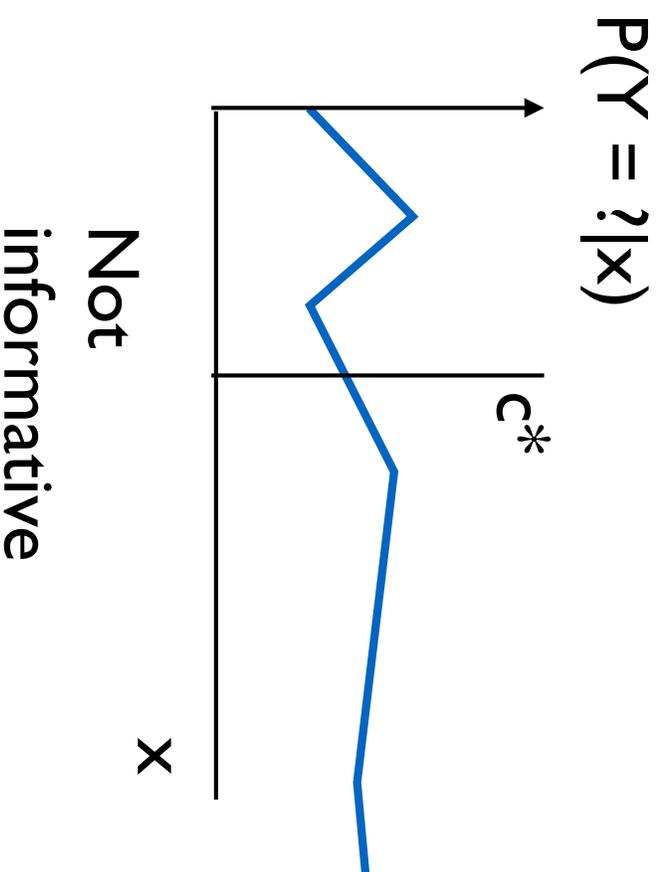
$$P(Y = ?|x)$$



When can abstentions help?



When can abstentions help?



When abstention rates increase
close to decision boundary

Talk Outline

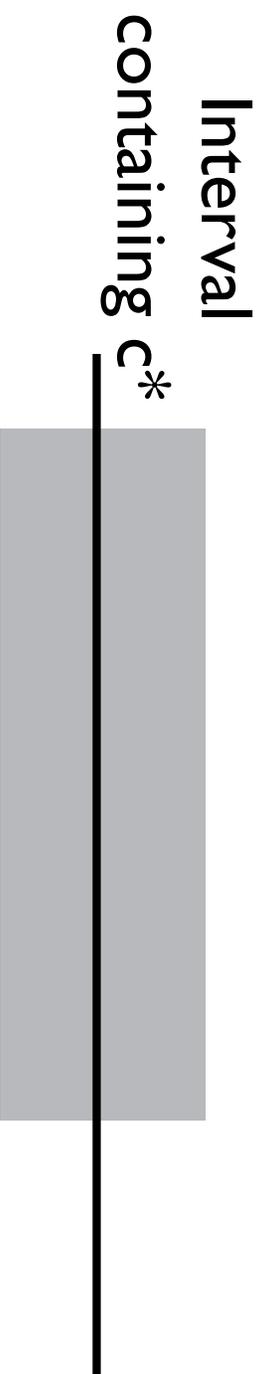
1. Weak and Strong Labelers

- the model
- algorithm
- analysis

2. Abstentions

- the model
- algorithm

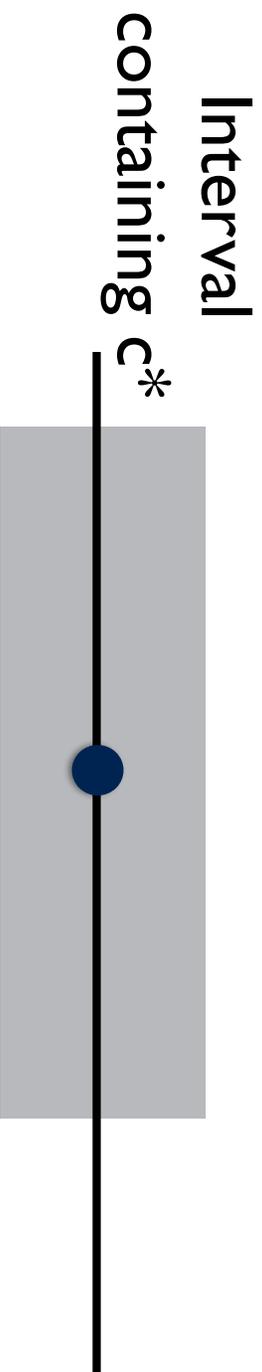
Basic Algorithm: Binary Search



Assume: Correct response

Divide plausible interval containing c^* by half per query

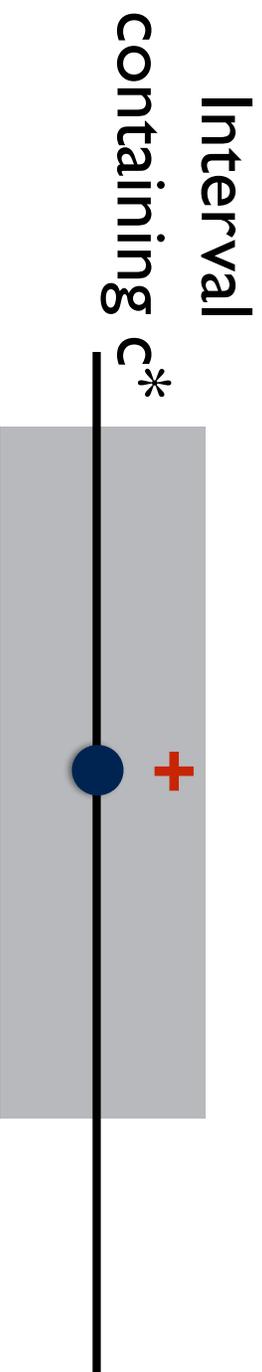
Basic Algorithm: Binary Search



Assume: Correct response

Divide plausible interval containing c^* by half per query

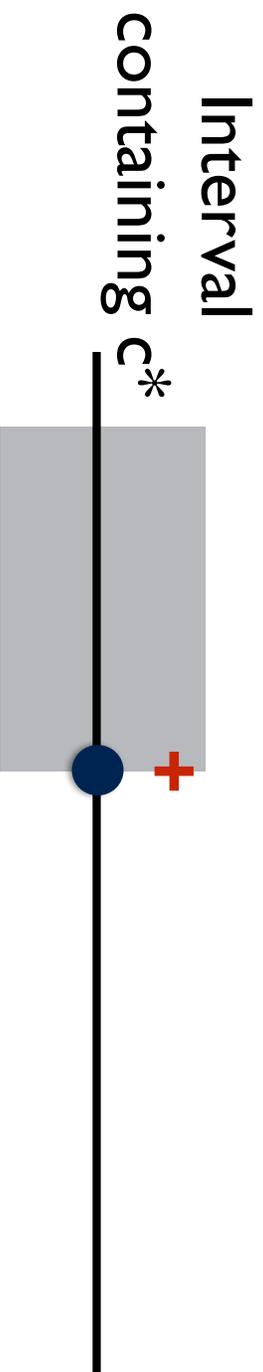
Basic Algorithm: Binary Search



Assume: Correct response

Divide plausible interval containing c^* by half per query

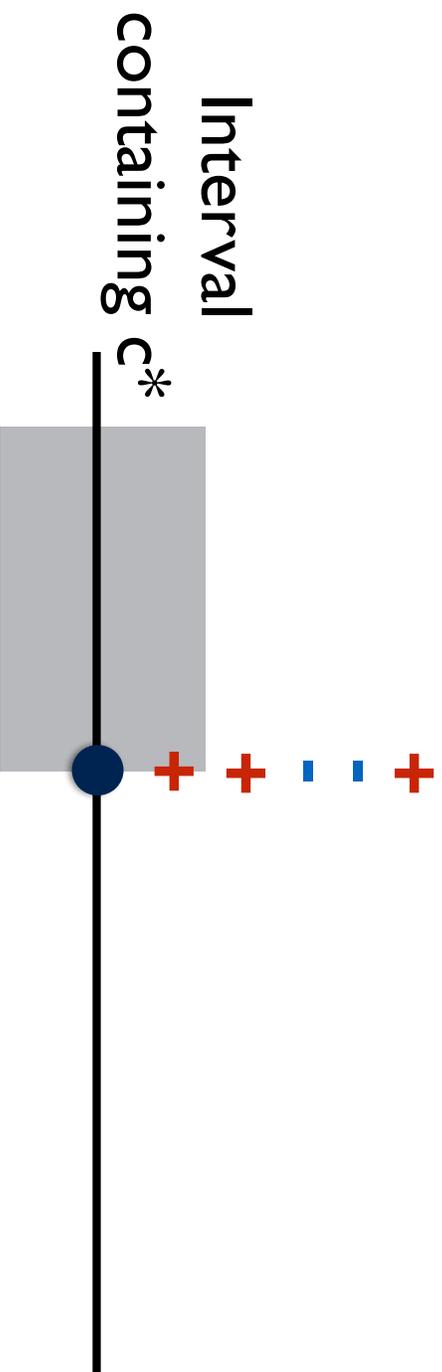
Basic Algorithm: Binary Search



Assume: Correct response

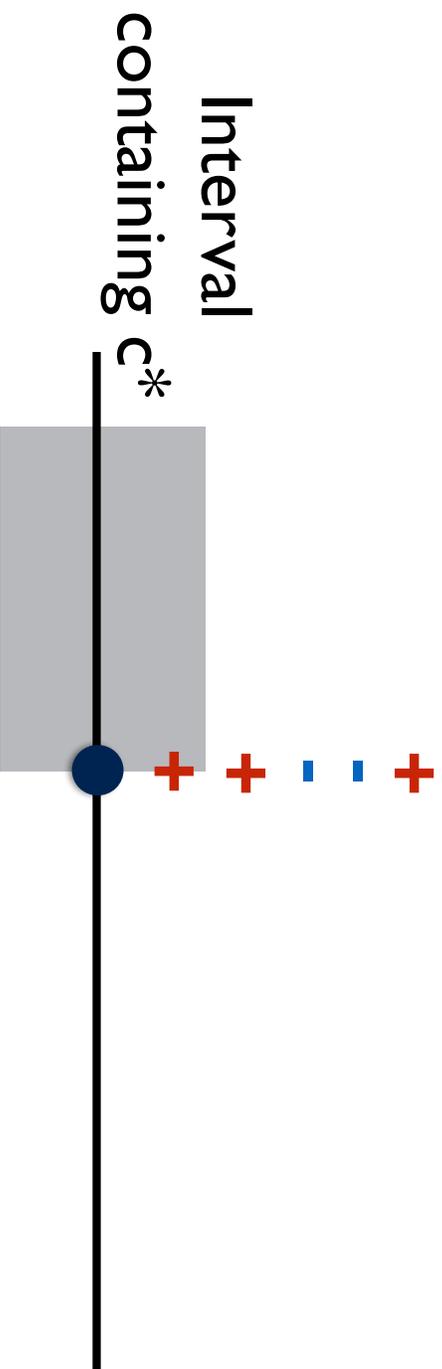
Divide plausible interval containing c^* by half per query

Basic Algorithm: Binary Search



Noisy Response: Query multiple times, average to
get ground truth label with high confidence

Basic Algorithm: Binary Search

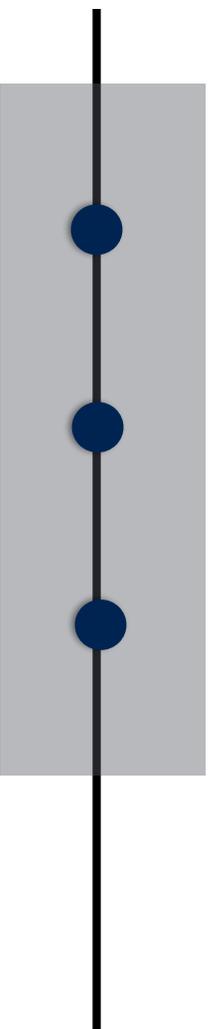


Noisy Response: Query multiple times, average to get ground truth label with high confidence

Increasing noise rate: Make an adaptive #queries till high confidence [BR16]

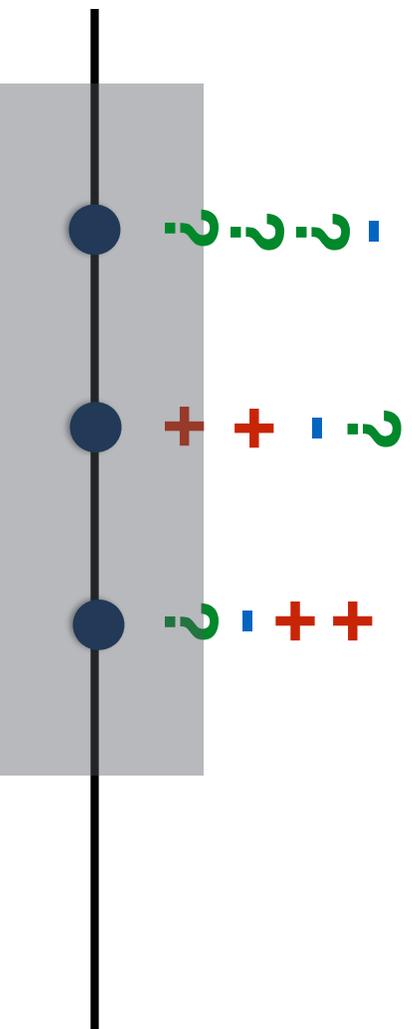
How to handle abstentions?

Modified Binary Search



Query: quartiles of interval

Modified Binary Search

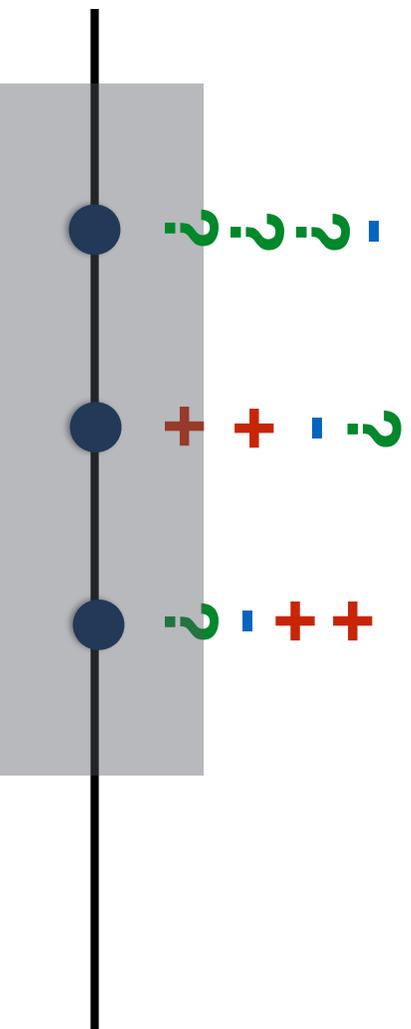


Query: quartiles of interval

After each query, determine if:

- We are confident in the label at any point

Modified Binary Search

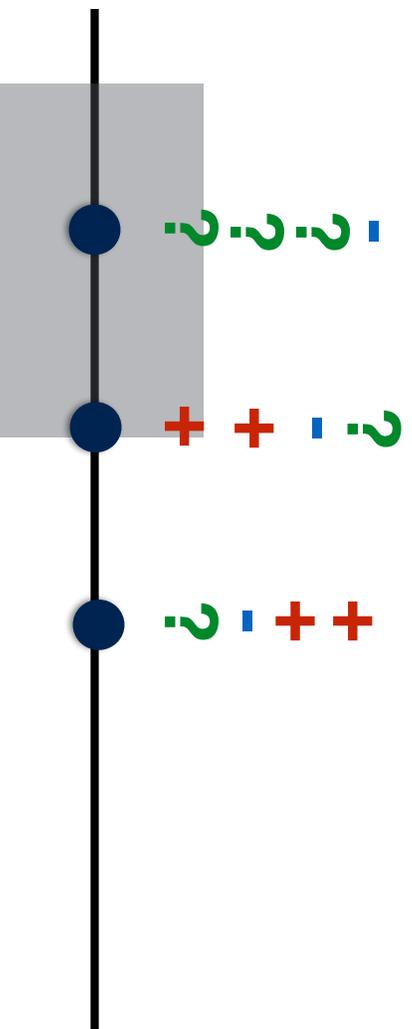


Query: quartiles of interval

After each query, determine if:

- We are confident in the label at any point
- or, if the abstention rate is increasing in some direction

Modified Binary Search



Query: quartiles of interval

After each query, determine if:

- We are confident in the label at any point
- or, if the abstention rate is increasing in some direction

Reduce interval correspondingly

Performance Guarantees

Completely adaptive - algorithm does not know response parameters

Performance Guarantees

Completely adaptive - algorithm does not know response parameters

Statistically consistent so long as abstention rate does not decrease closer to boundary

Performance Guarantees

Completely adaptive - algorithm does not know response parameters

Statistically consistent so long as abstention rate does not decrease closer to boundary

What about #queries?

Example: An Informative Response Model

Response Model:

$$\Pr(Y = ? | x) = 1 - C_0 |x - c^*|^\alpha$$

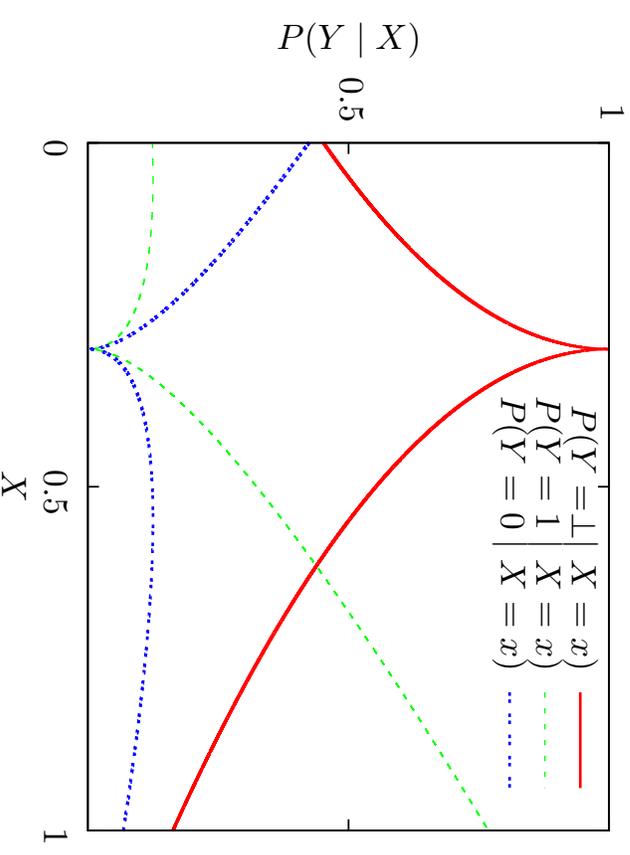
$$\Pr(Y \neq c^*(x)) \leq \frac{1}{2} - C_1 |x - c^*|^\beta$$

$$\alpha, \beta \geq 1$$

#Queries to get $|c - c^*| \leq \epsilon$

$$O(\epsilon^{-\alpha}) \quad (\text{our method})$$

$$O(\epsilon^{-\alpha-2\beta}) \quad (\text{use only labels})$$



Summary

Abstentions may help if rate of abstentions increase close to decision boundary

Algorithms for thresholds and smooth boundary fragments [CN08]

Work in Progress: PAC model

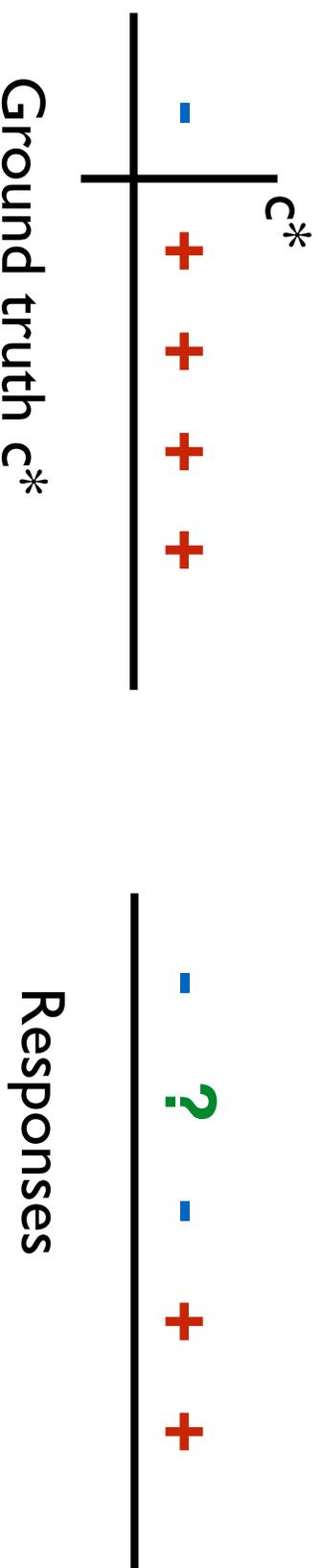
Conclusion

- More complex feedback helps active learning under certain conditions
- Need more sophisticated algorithms

Thank You!

Example: Learning Thresholds

Concept class $C =$ thresholds, instance space $X = [0, 1]$



Learner can query any x in X

Responses $+, -, ?$ drawn from unknown $P(Y|x)$

Goal: Find c close to c^* with min #queries