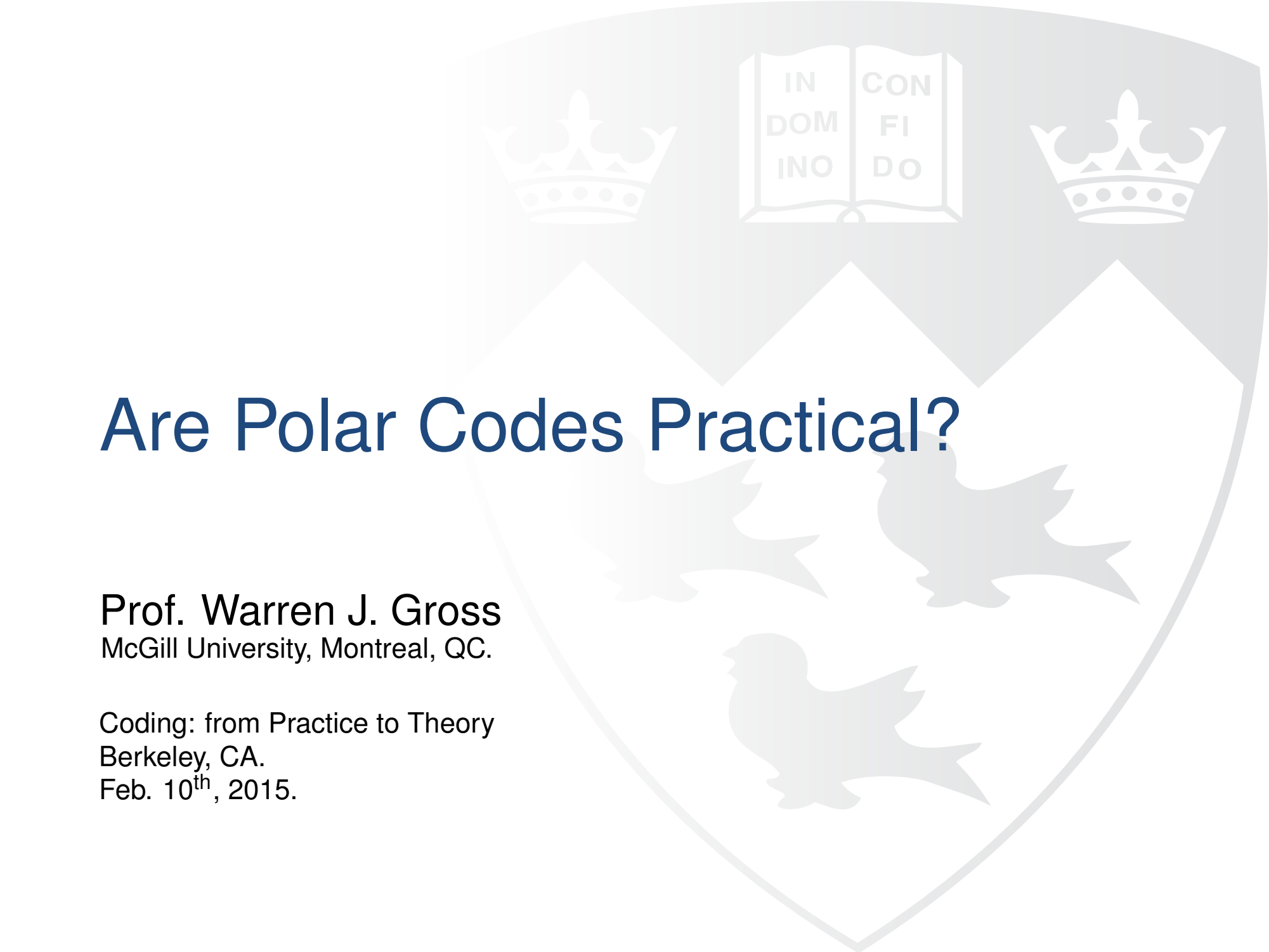
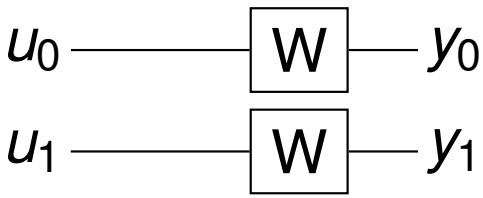


Are Polar Codes Practical?

Prof. Warren J. Gross
McGill University, Montreal, QC.

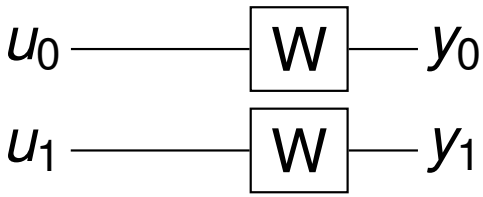
Coding: from Practice to Theory
Berkeley, CA.
Feb. 10th, 2015.

Channel Polarization

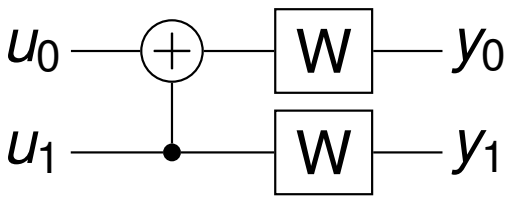


$$I^0 = I(W) = I^1$$

Channel Polarization

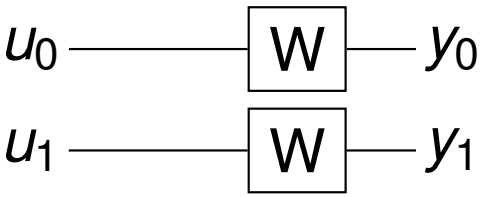


$$I^0 = I(W) = I^1$$

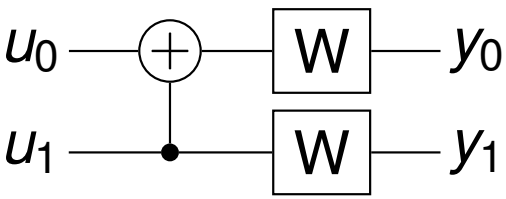


$$I^0 < I(W) < I^1$$

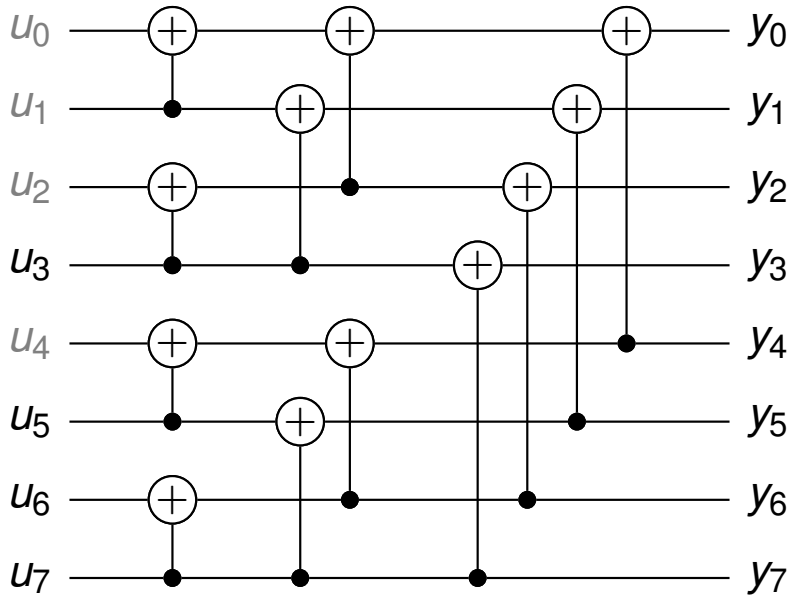
Channel Polarization



$$I^0 = I(W) = I^1$$

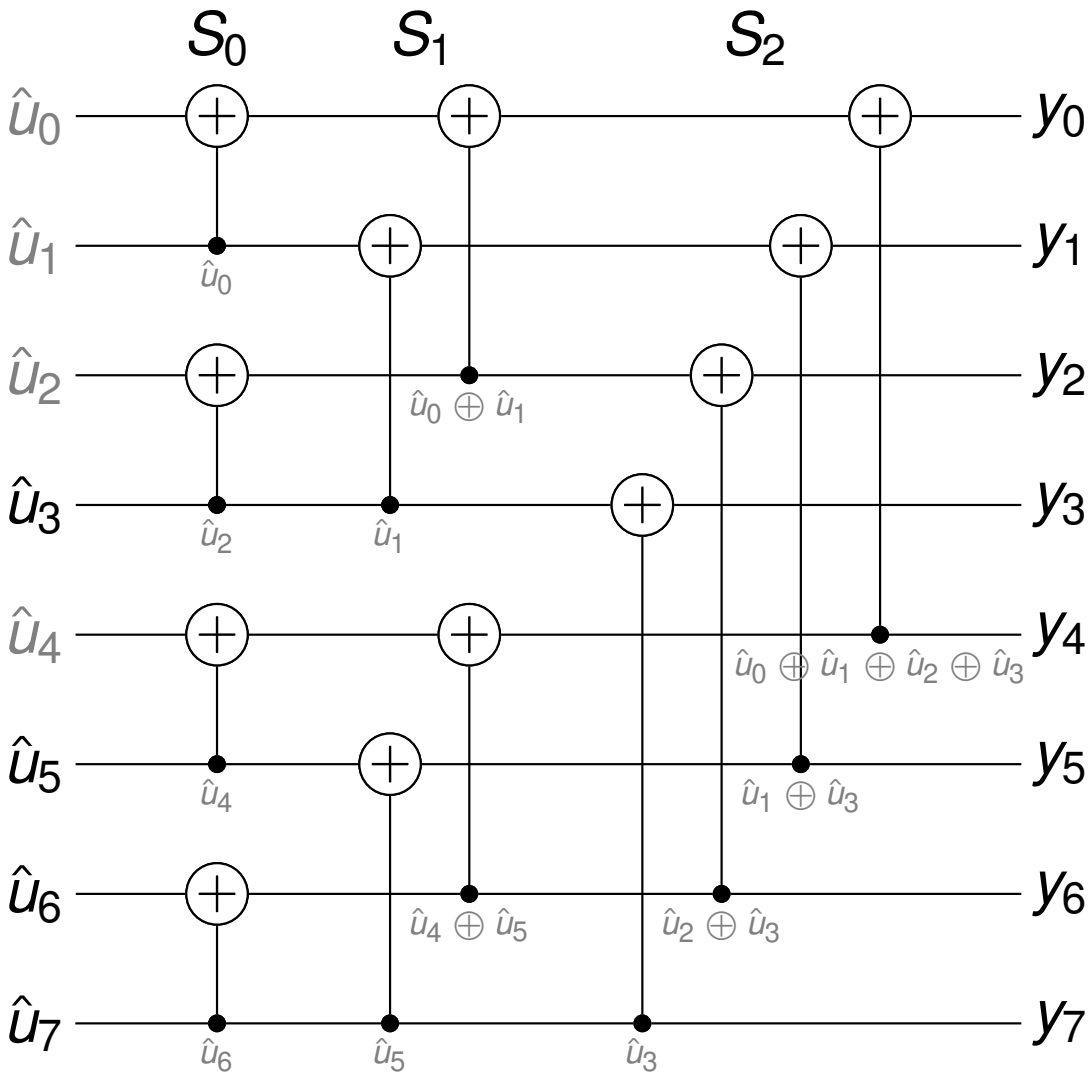


$$I^0 < I(W) < I^1$$

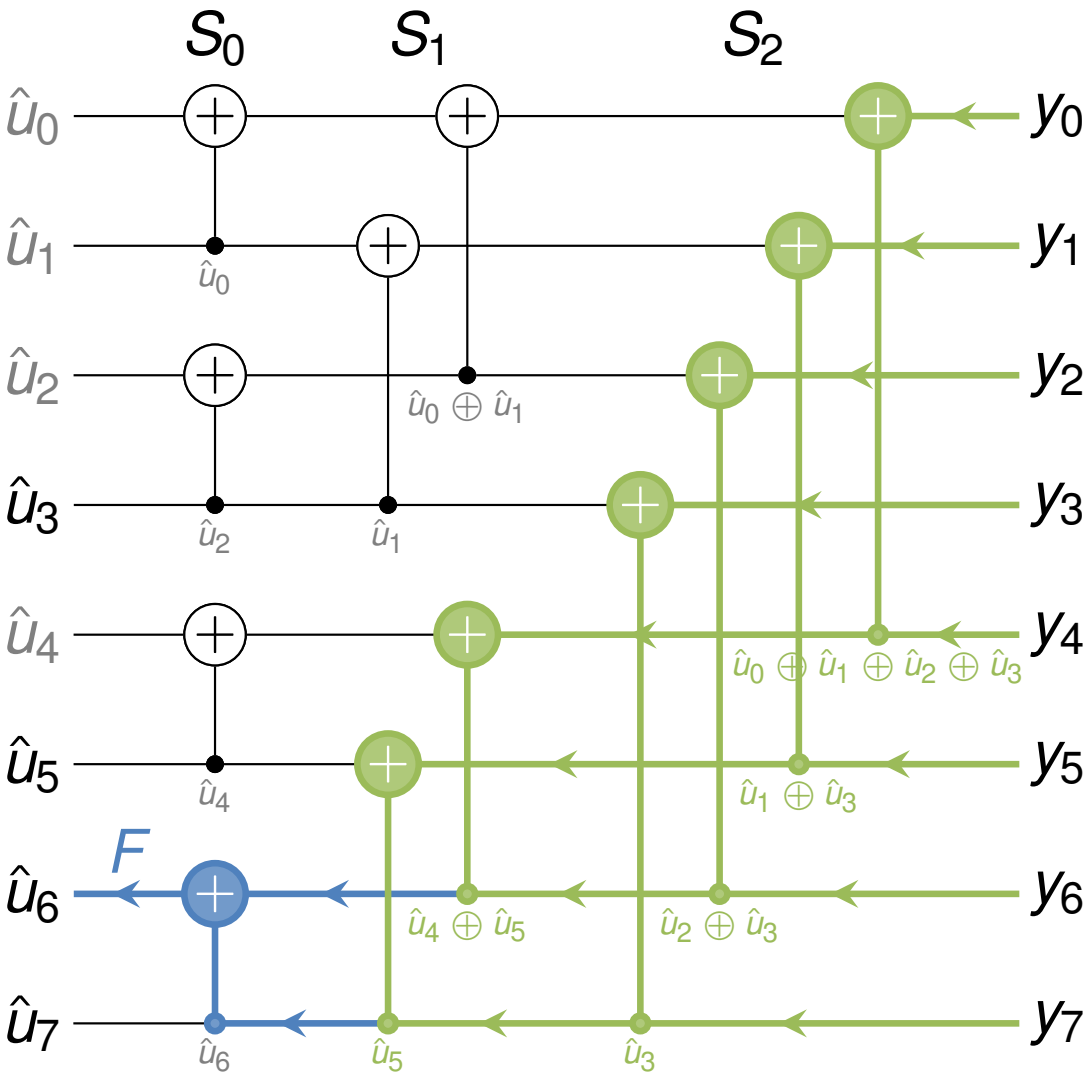


Proportion of reliable bits $\to I(W)$.

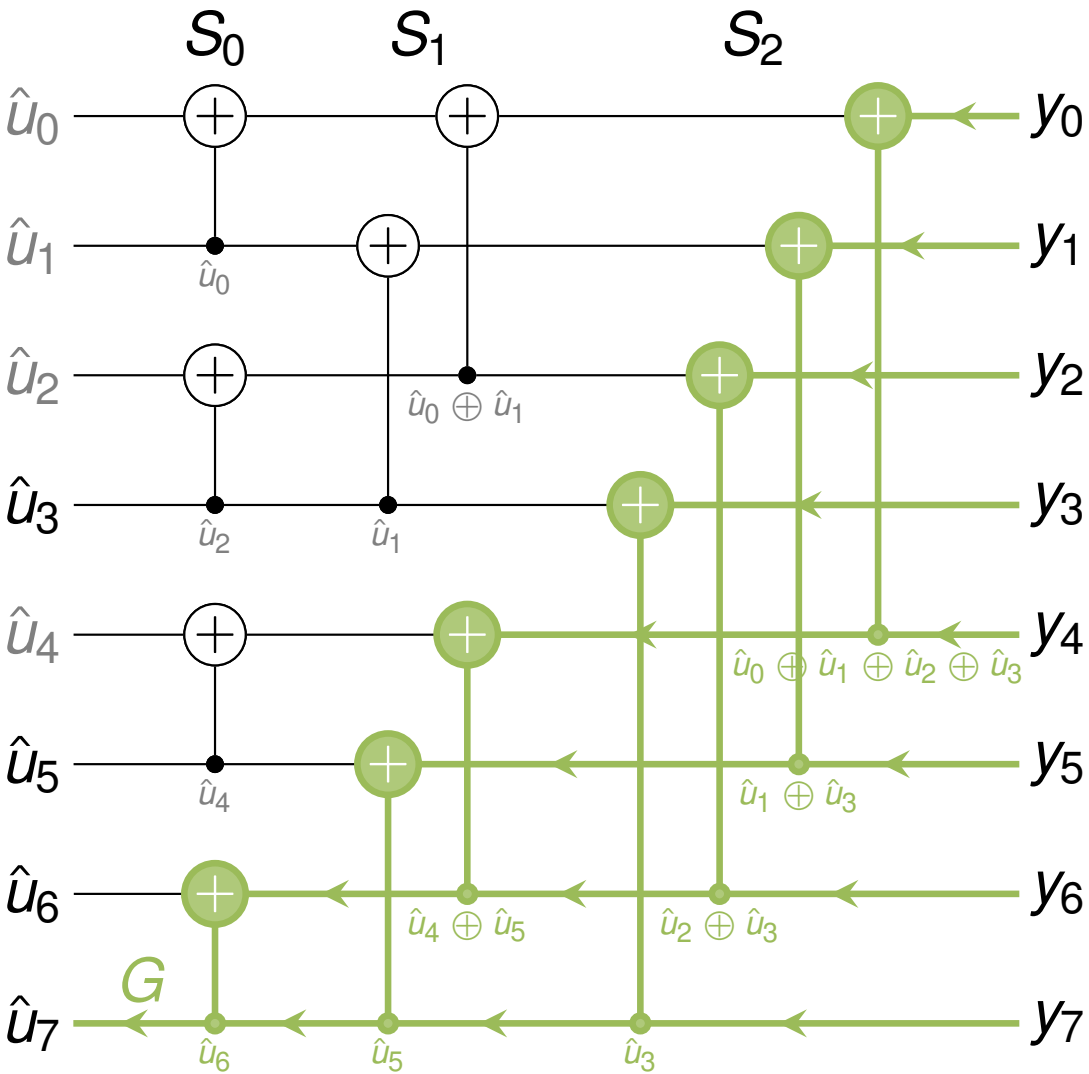
Successive Cancellation Decoding



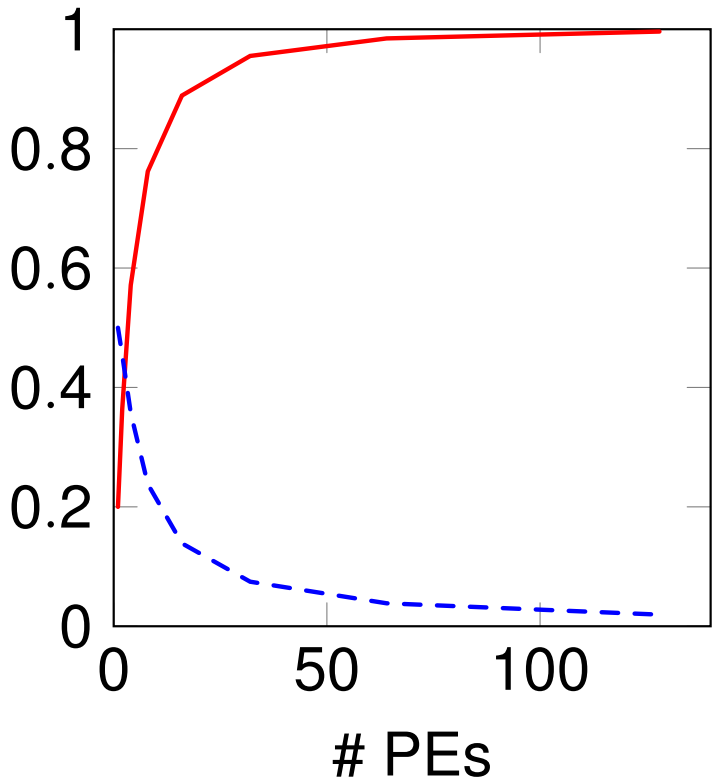
Successive Cancellation Decoding



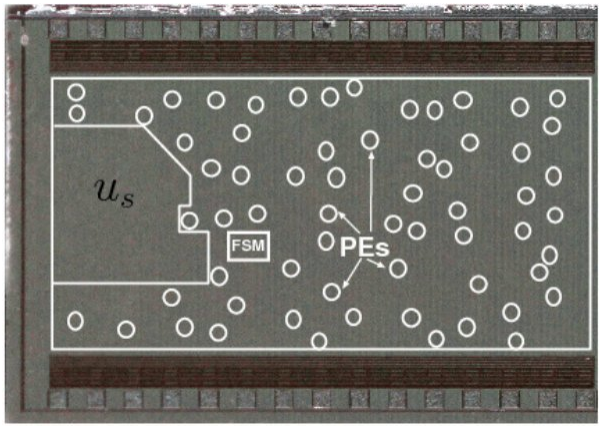
Successive Cancellation Decoding



Semi-Parallel SC Decoder Implementation



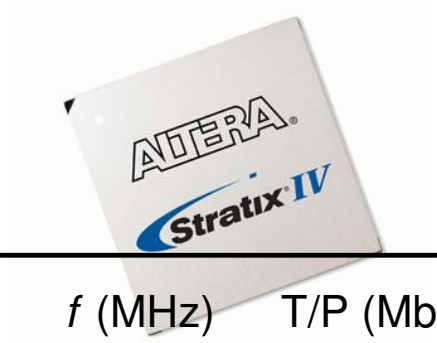
$>$ 95% speed with 64 PEs.



First polar decoder ASIC.

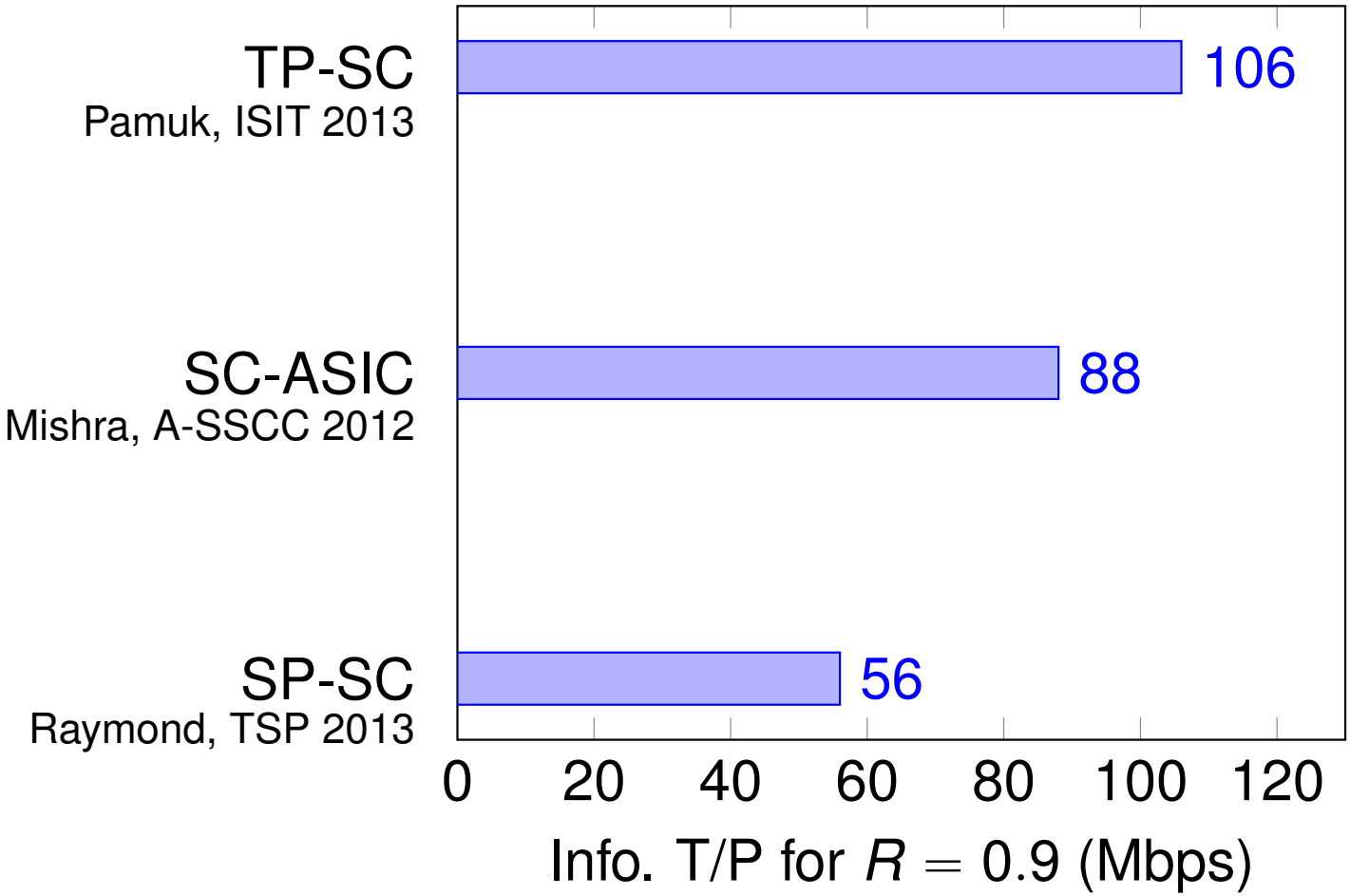
Code	(1024, 512)
Technology	180 nm
Area	1.72 mm^2
Frequency	150 MHz
Info. T/P	49 Mbps
Power	67 mW

FPGA Implementation



N	LUT	FF	RAM (bits)	f (MHz)	T/P (Mbps)
2^{15}	3,263	1,304	411,648	167	$62R$
2^{16}	3,414	1,316	821,248	157	$57R$
2^{18}	3,548	1,349	3,278,848	140	$51R$
2^{20}	5,956	1,366	13,109,248	102	$38R$

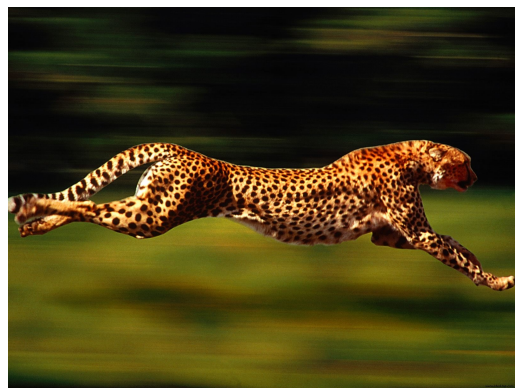
Throughput of SC Decoders



Improving Throughput

100 Mbps
SC

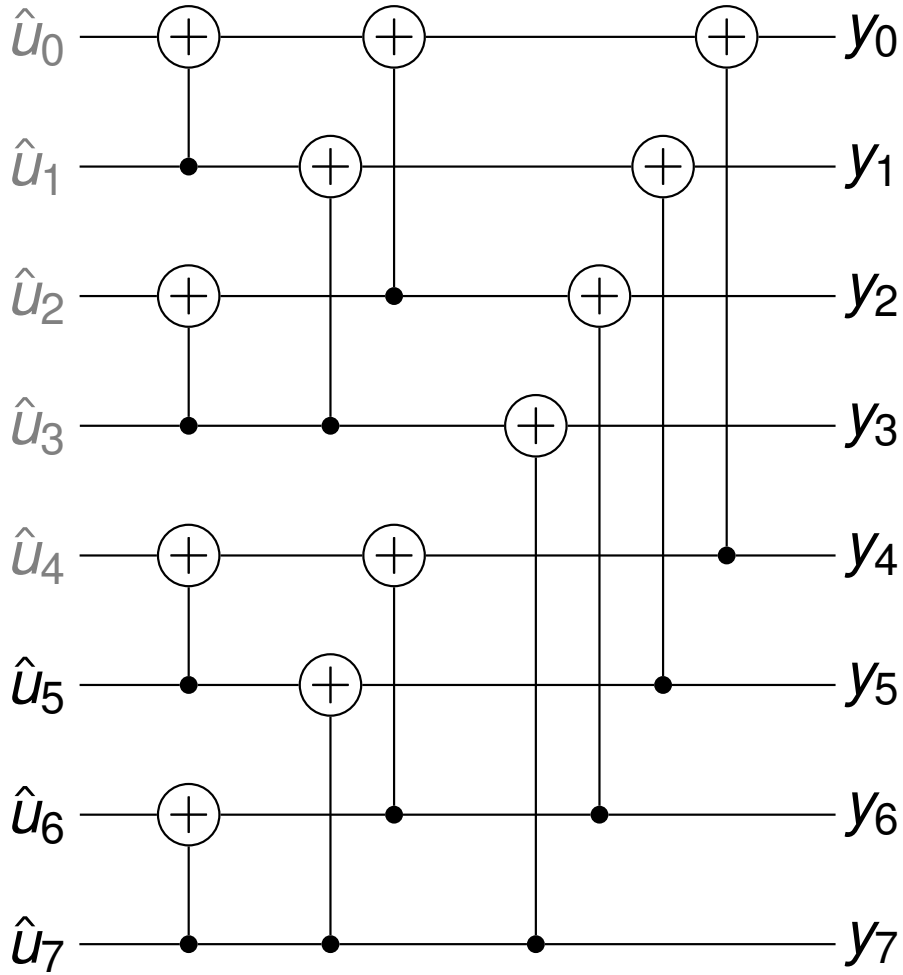
1000×



100 Gbps
Unrolled

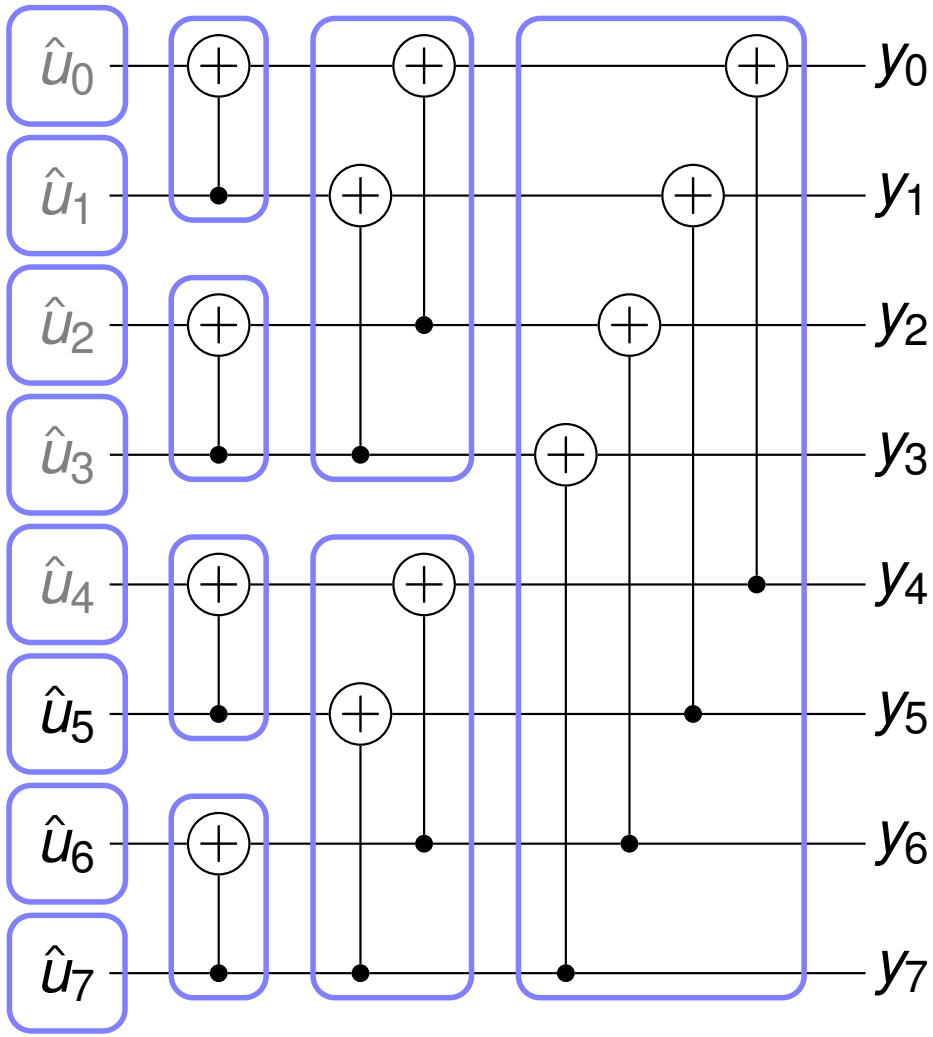
Successive Cancellation Tree

- View the SC decoder graph as a tree.



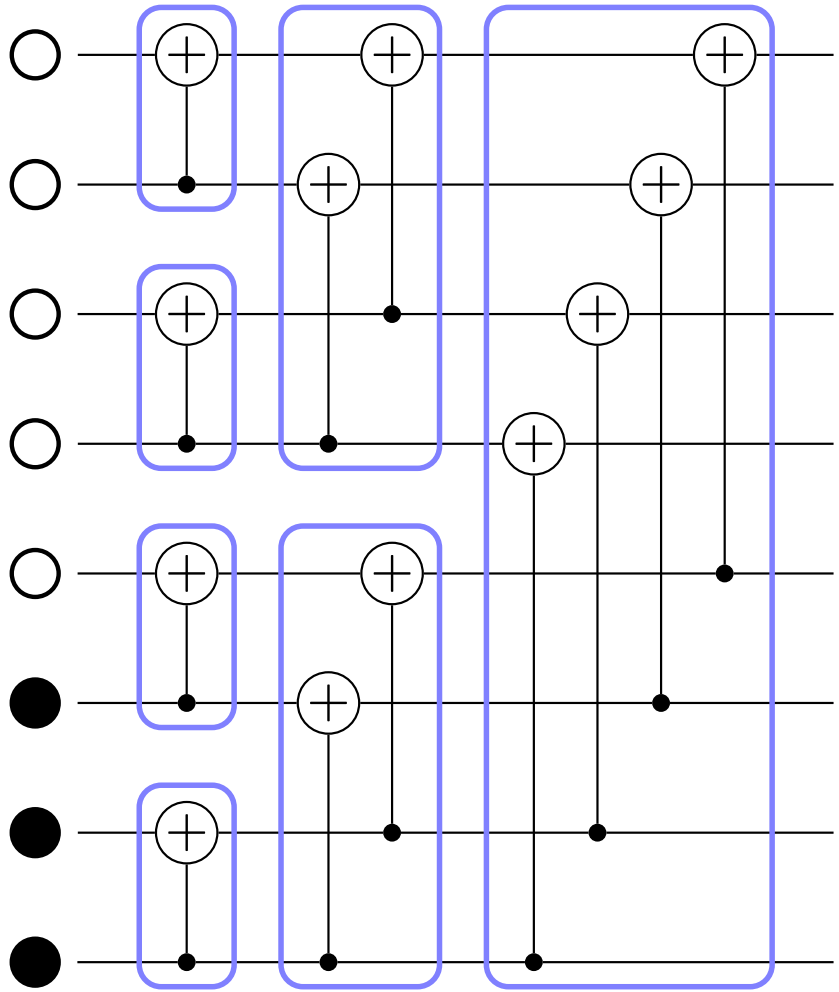
Successive Cancellation Tree

- View the SC decoder graph as a tree.



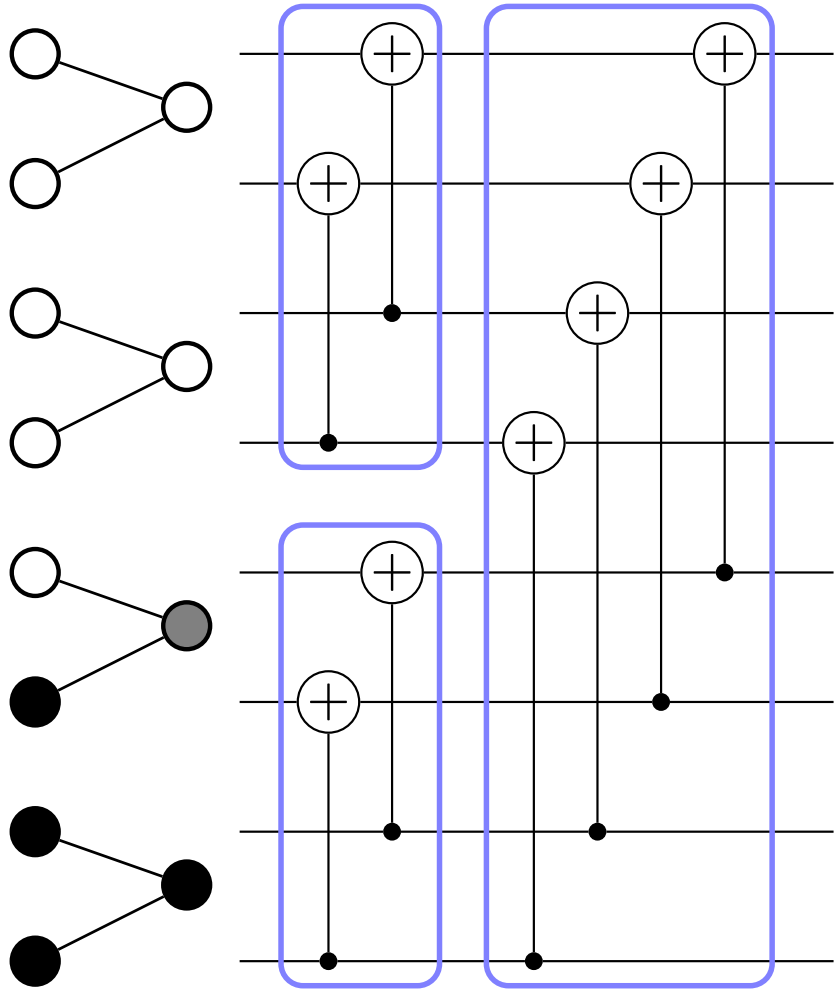
Successive Cancellation Tree

- View the SC decoder graph as a tree.



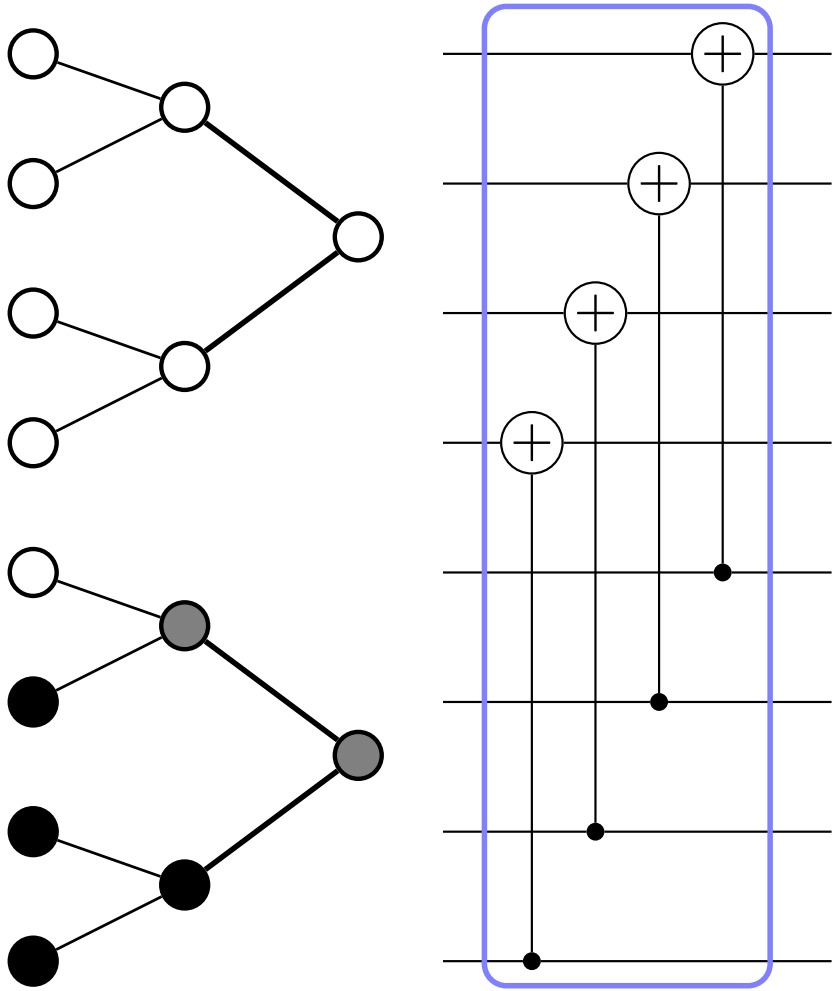
Successive Cancellation Tree

- View the SC decoder graph as a tree.



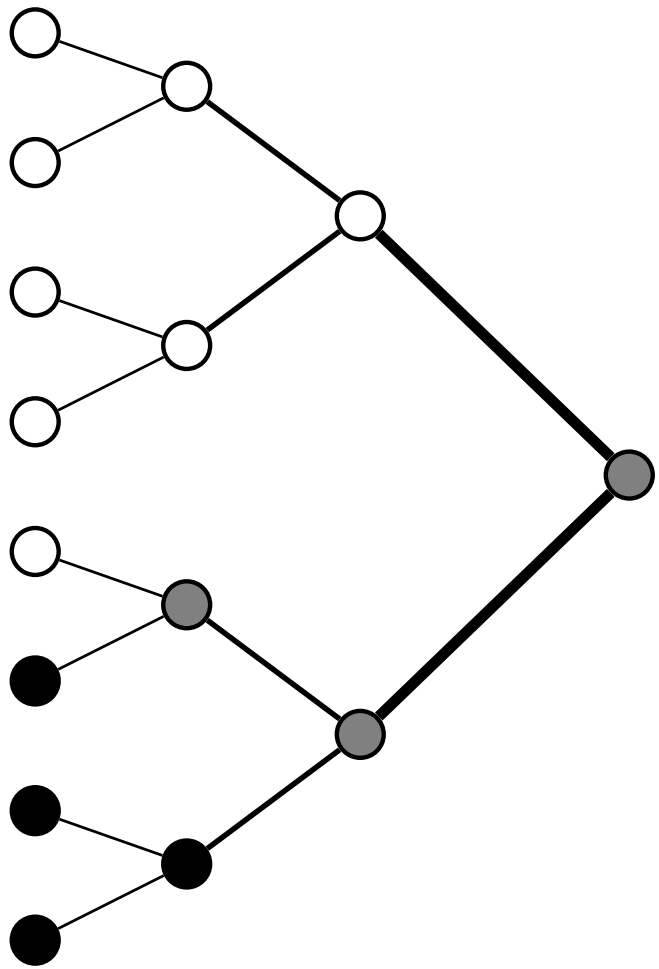
Successive Cancellation Tree

- View the SC decoder graph as a tree.

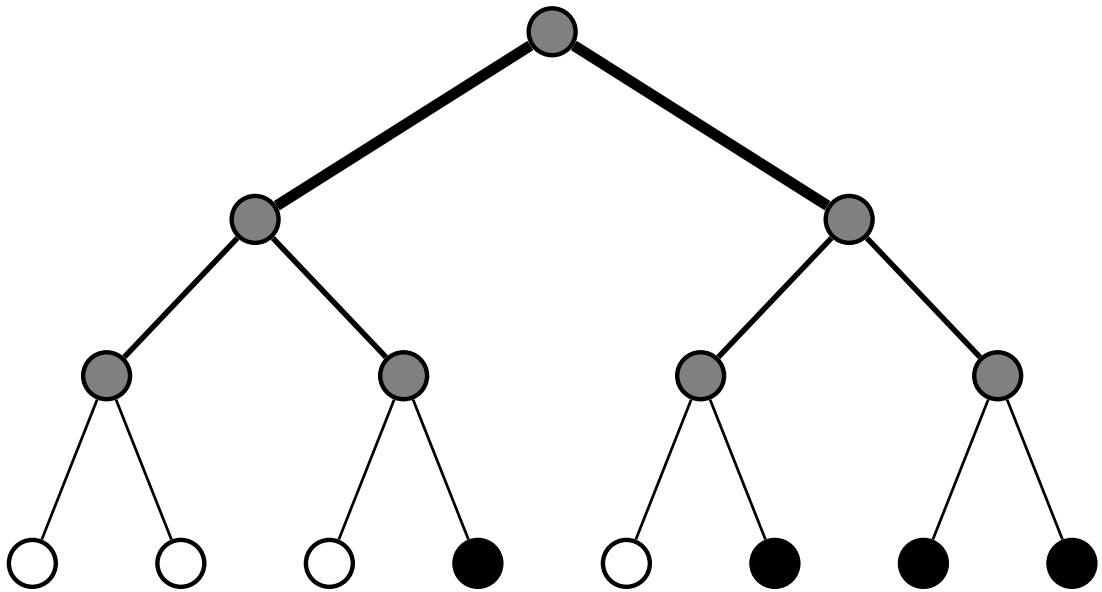


Successive Cancellation Tree

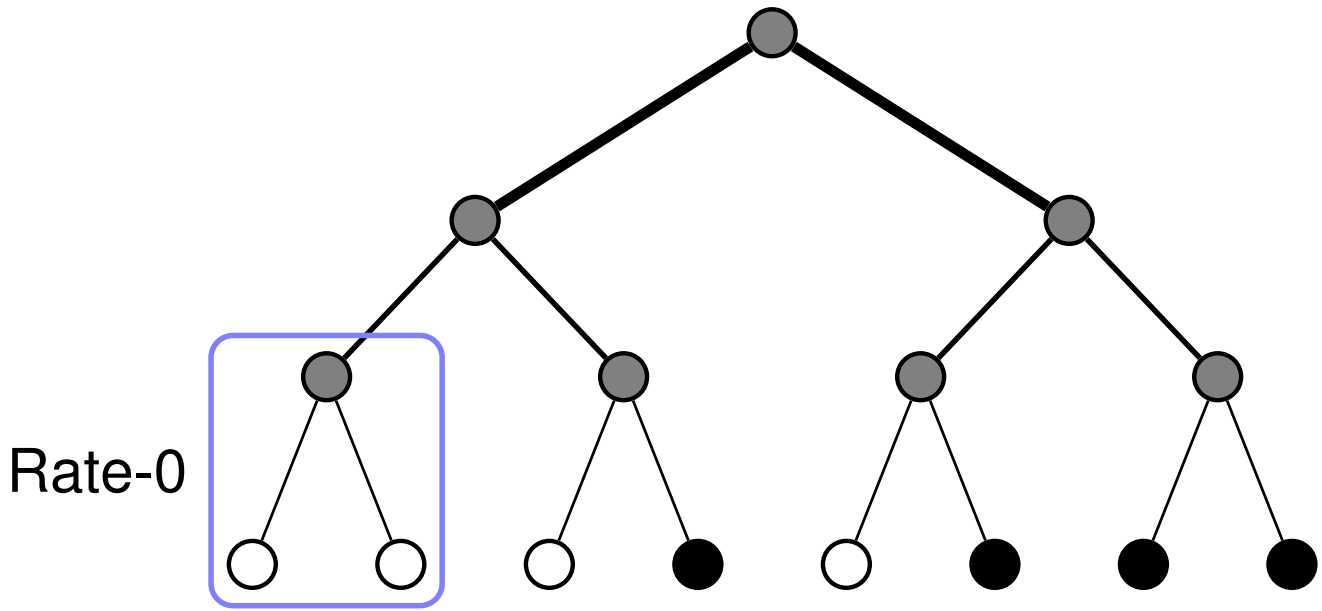
- View the SC decoder graph as a tree.



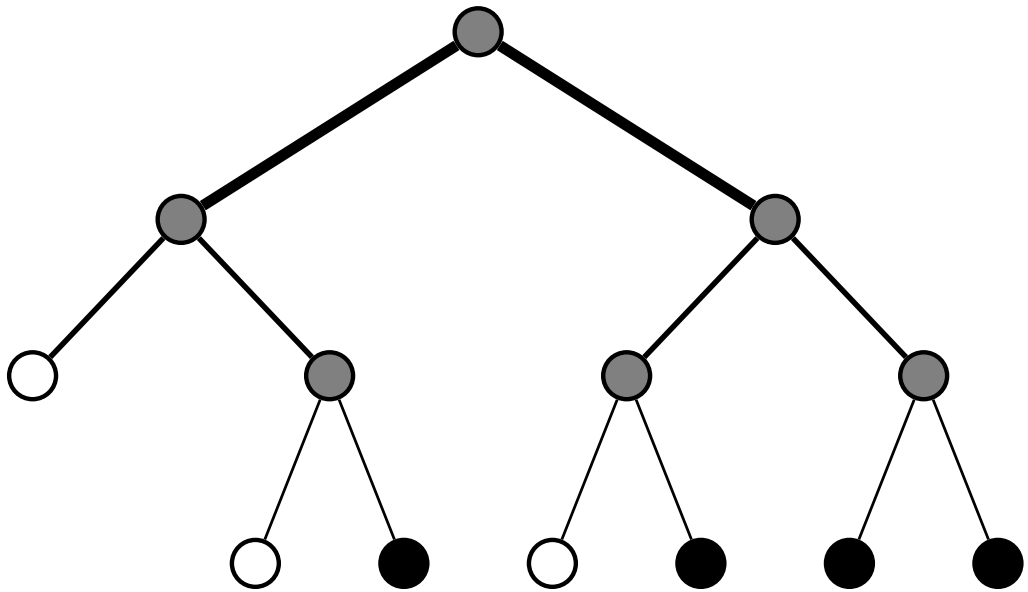
Simplified Successive-Cancellation Decoding



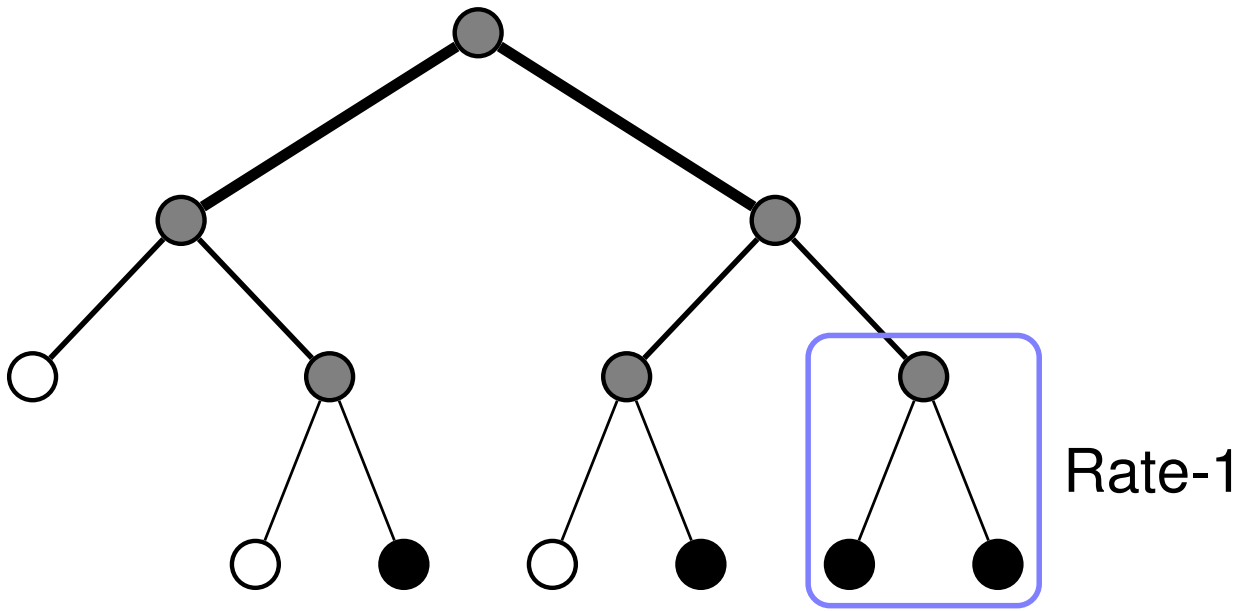
Simplified Successive-Cancellation Decoding



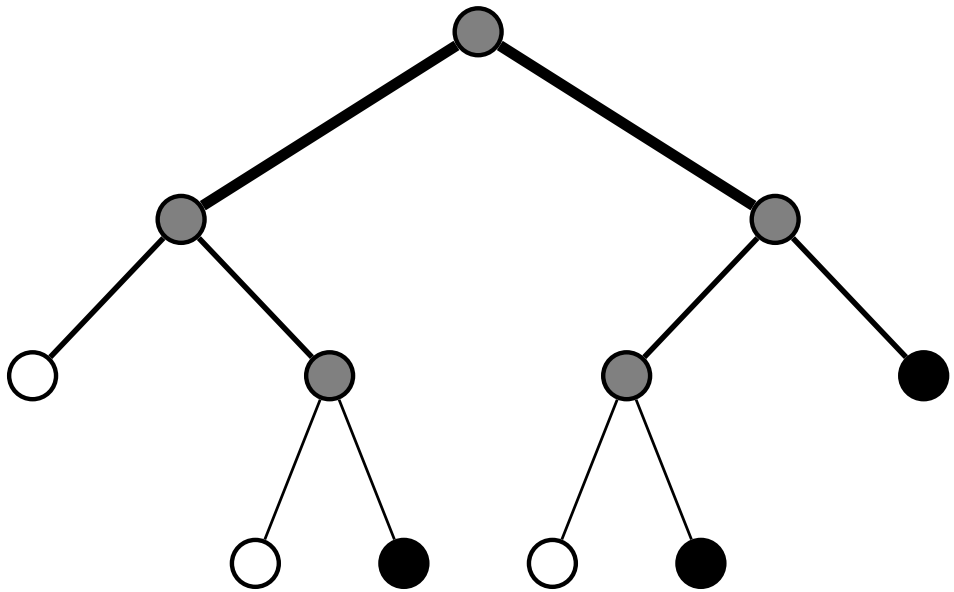
Simplified Successive-Cancellation Decoding



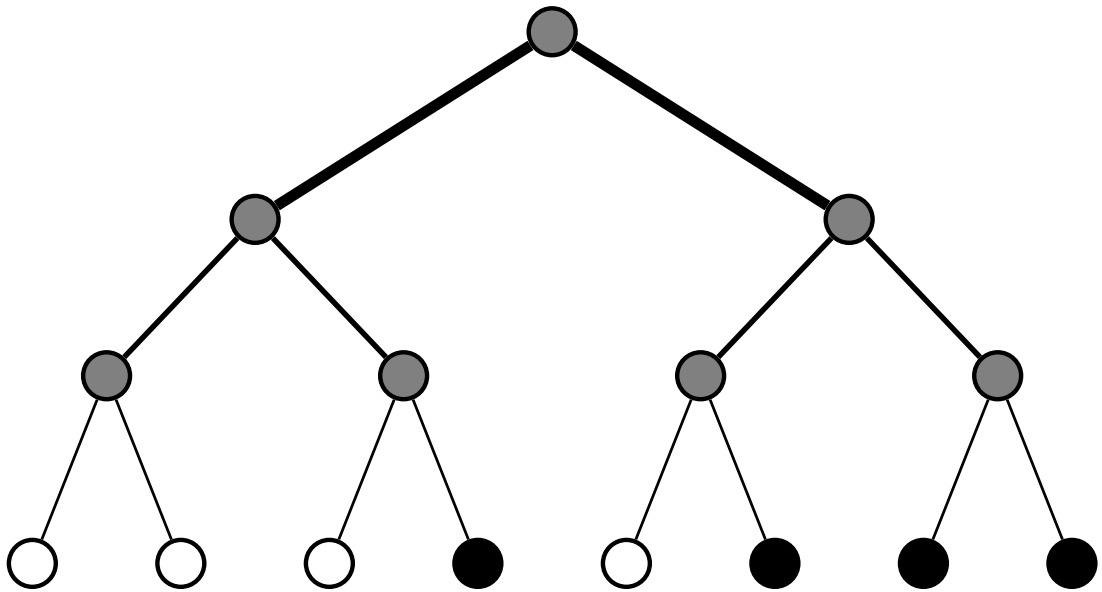
Simplified Successive-Cancellation Decoding



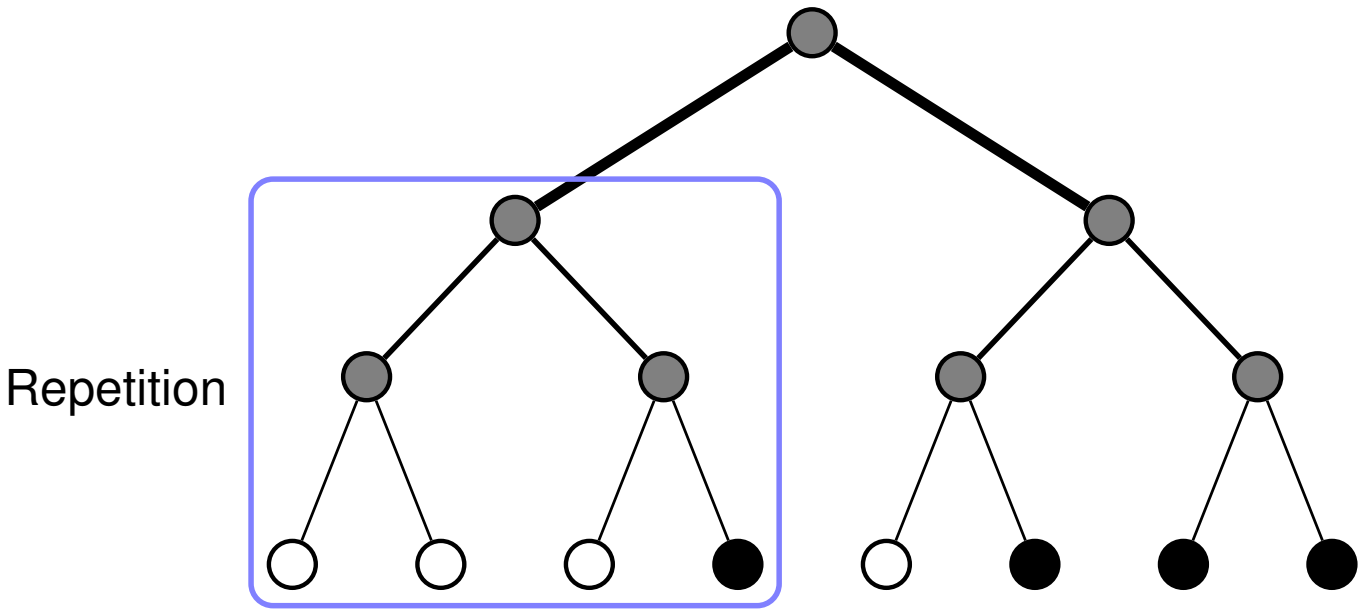
Simplified Successive-Cancellation Decoding



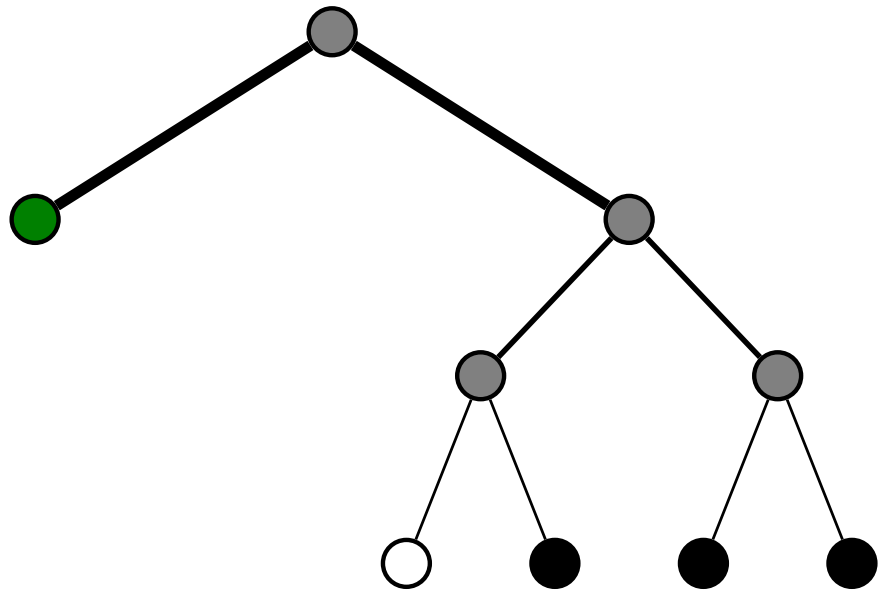
Fast-SSC Decoding



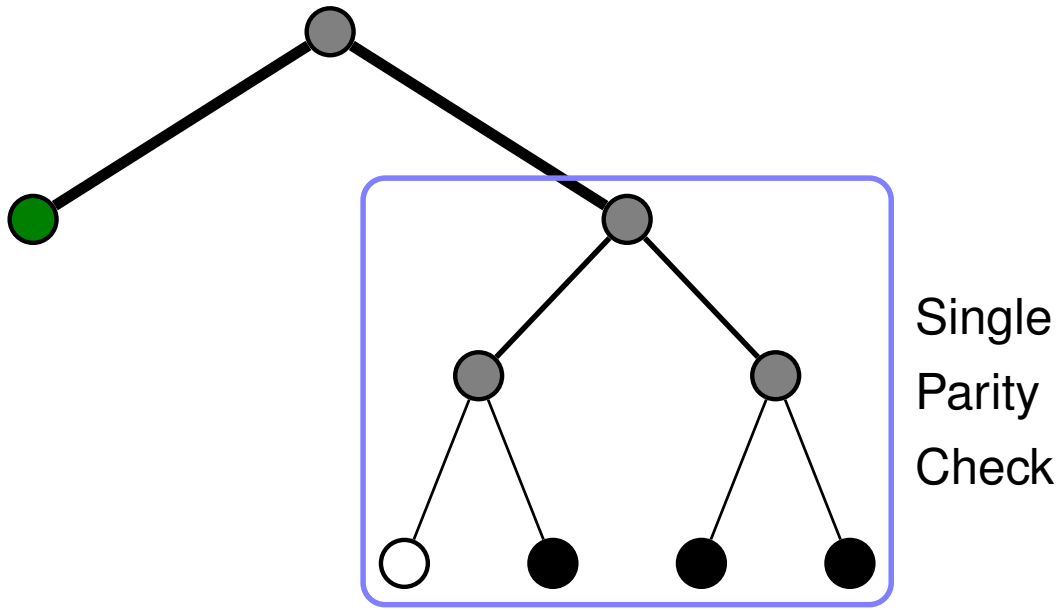
Fast-SSC Decoding



Fast-SSC Decoding

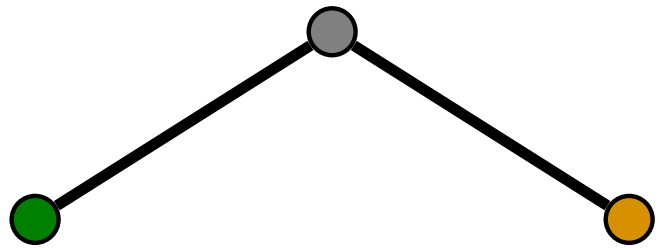


Fast-SSC Decoding

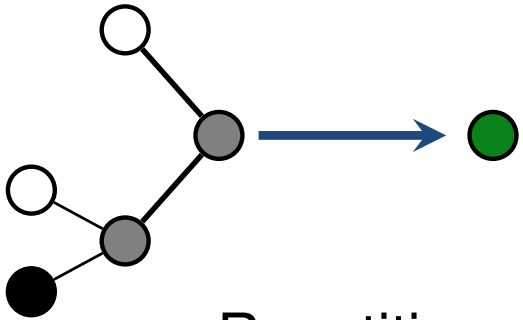


Sarkis et al., “Fast Polar Decoders: Algorithm and Implementation,” IEEE JSAC, 2014.

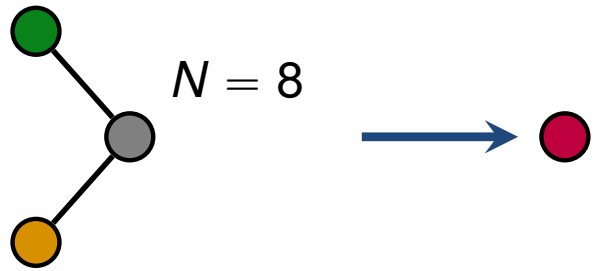
Fast-SSC Decoding



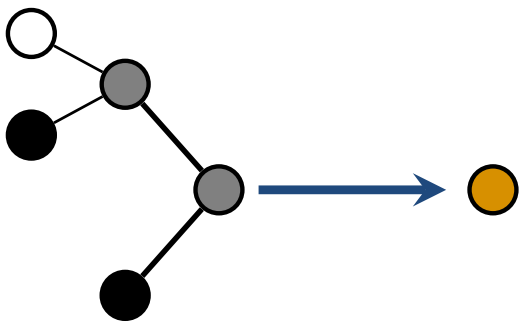
Fast-SSC Decoding—New Nodes



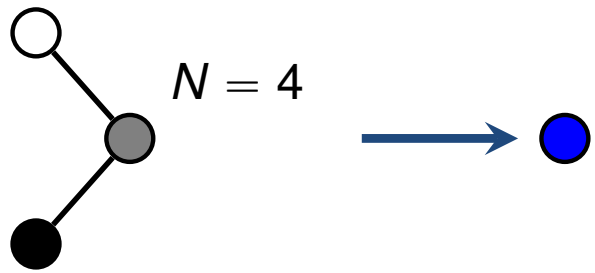
Repetition



Rep-SPC

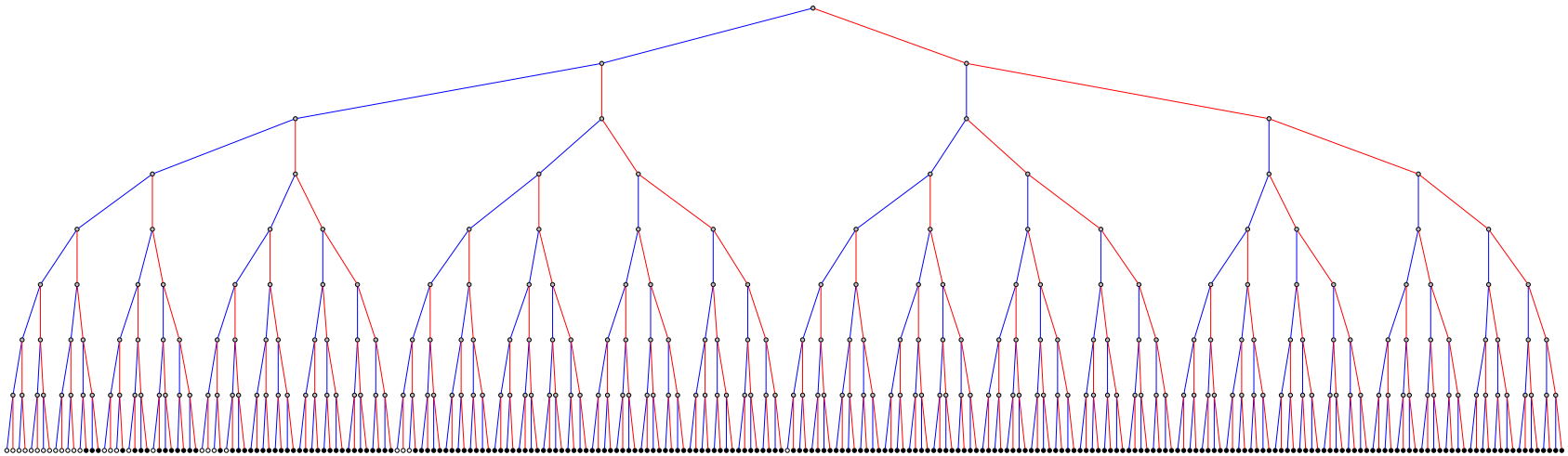


SPC

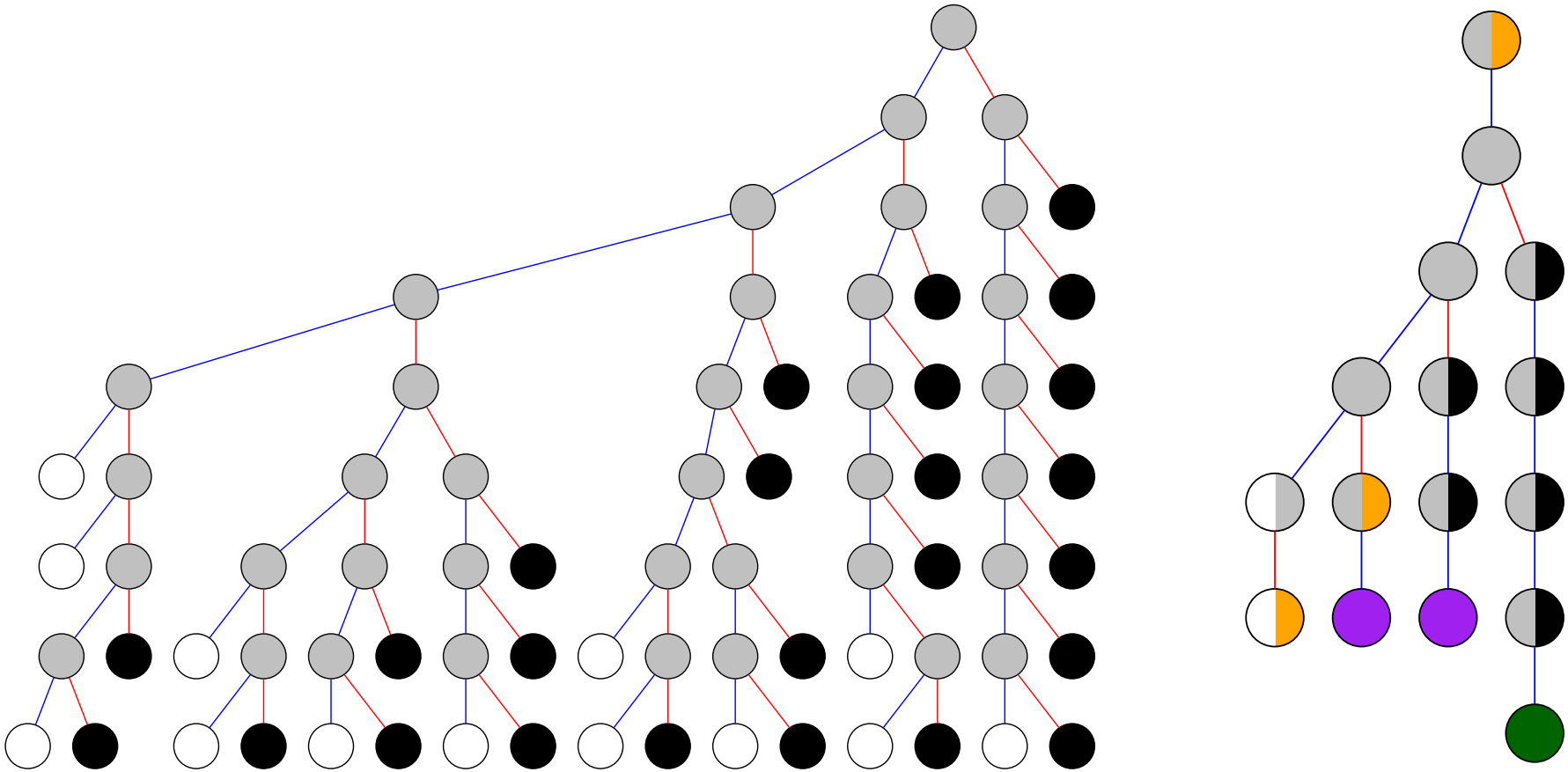


ML-0011

SC Tree—(256, 230)

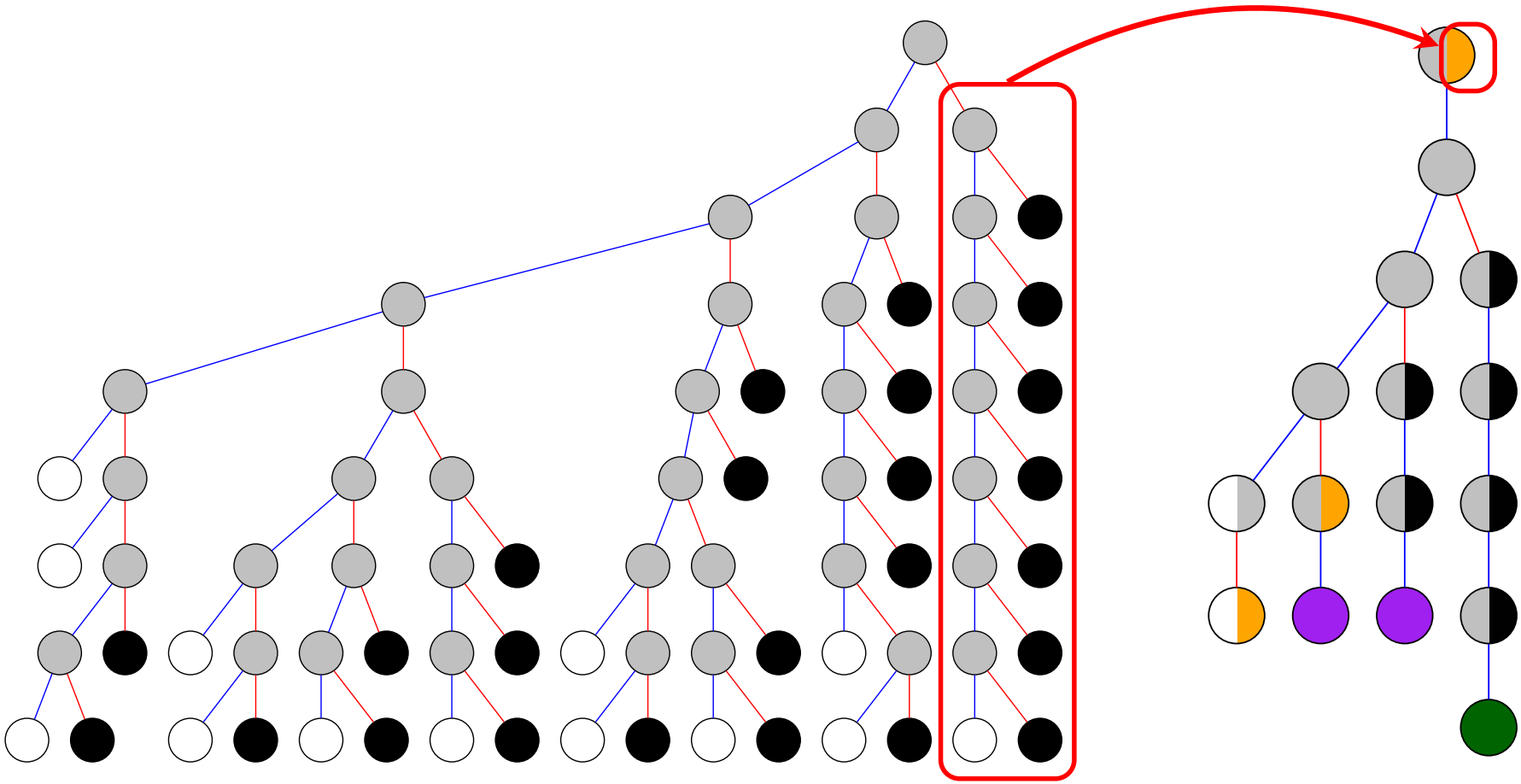


SSC and Fast-SSC Trees—(256, 230)



Developed a compiler to convert the graph to instructions.

SSC and Fast-SSC Trees—(256, 230)



Developed a compiler to convert the graph to instructions.

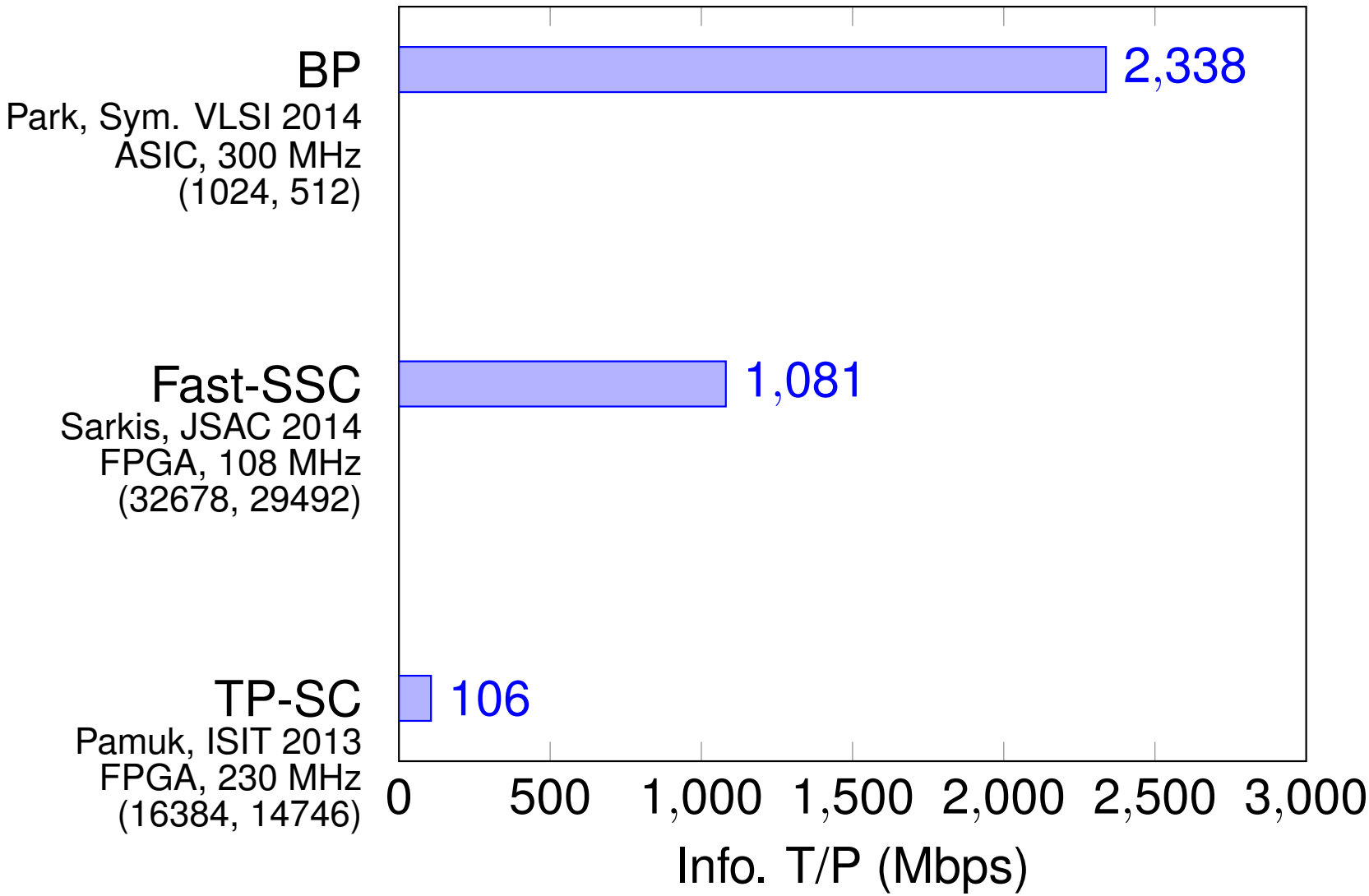
Fast-SSC Decoder Implementation

R	LUT	FF	RAM (bits)	f (MHz)	T/P (Mbps)
Fast-SSC					
0.83	25,866	7,209	536,126	108	791
0.90					1,081
SSC					
0.90					276

For any code of length = 32,768.

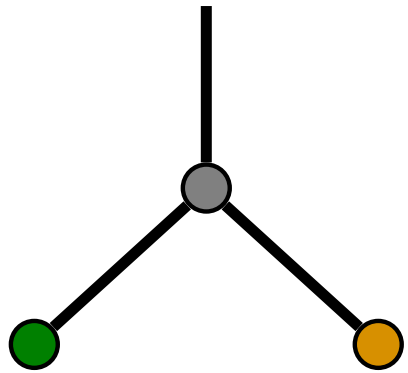
Sarkis et al. “Fast polar decoders: algorithm and implementation,” IEEE JSAC, 2014.

Throughput of Hardware Decoders



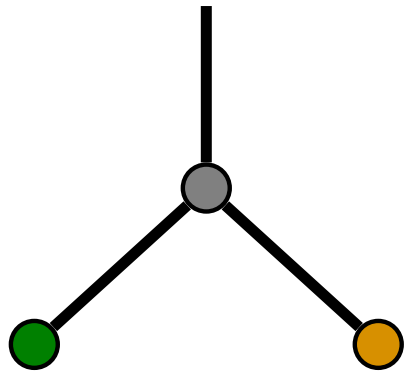
The Unrolled Decoder

- (8, 4) polar code:

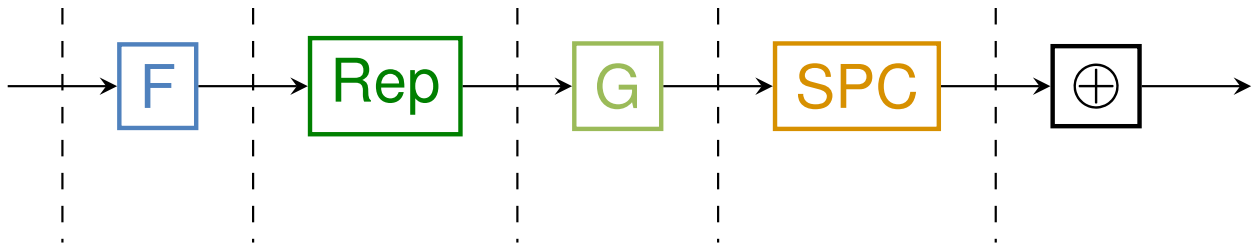


The Unrolled Decoder

- (8, 4) polar code:

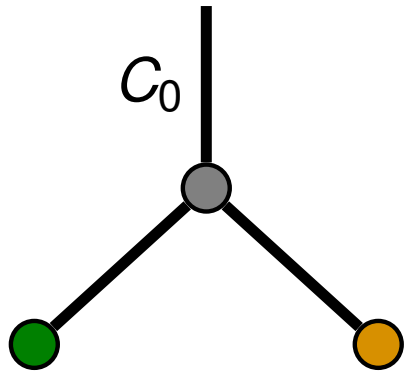


- Unroll and pipeline all operations.

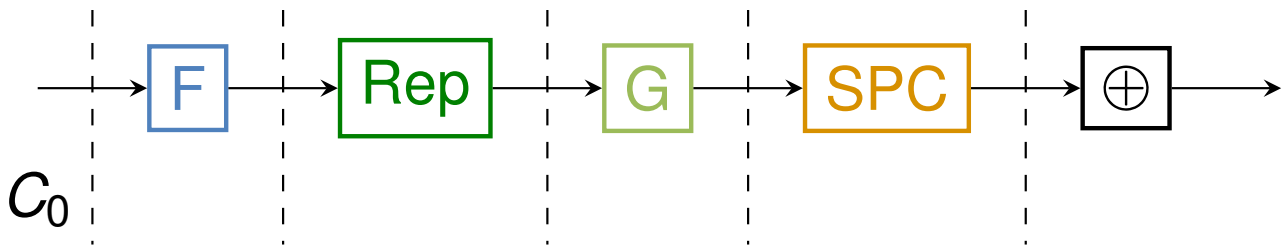


The Unrolled Decoder

- (8, 4) polar code:

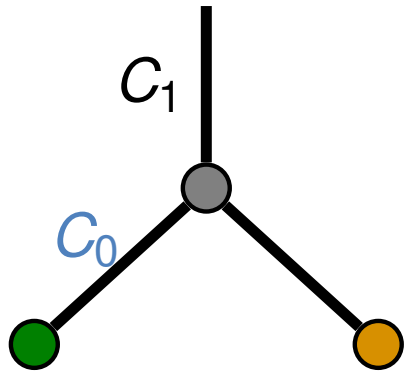


- Unroll and pipeline all operations.

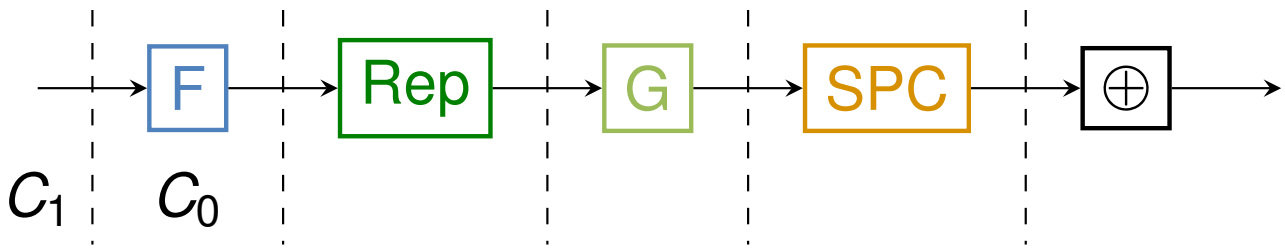


The Unrolled Decoder

- (8, 4) polar code:

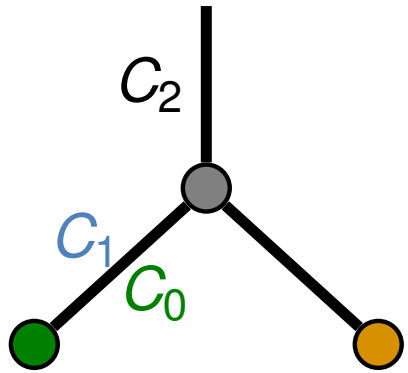


- Unroll and pipeline all operations.

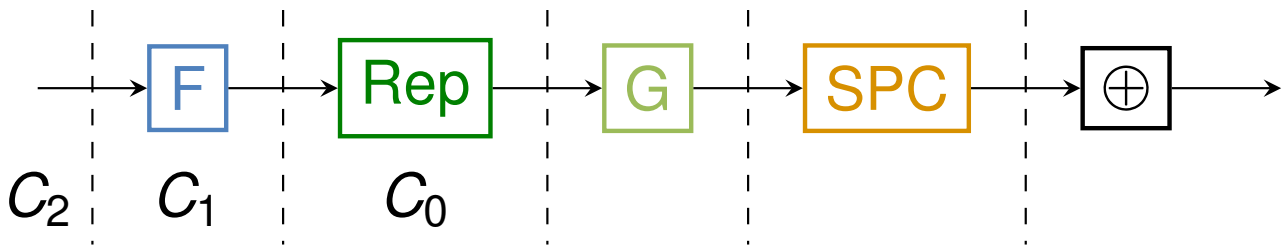


The Unrolled Decoder

- (8, 4) polar code:

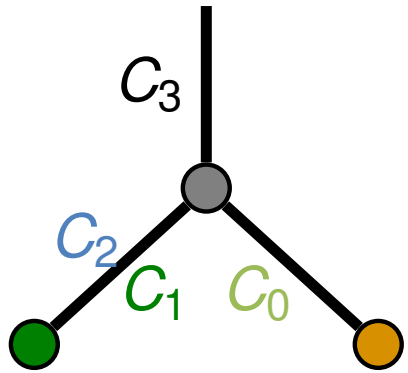


- Unroll and pipeline all operations.

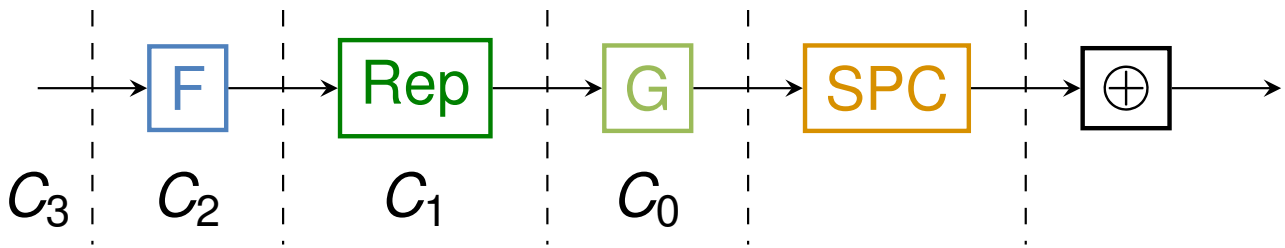


The Unrolled Decoder

- (8, 4) polar code:

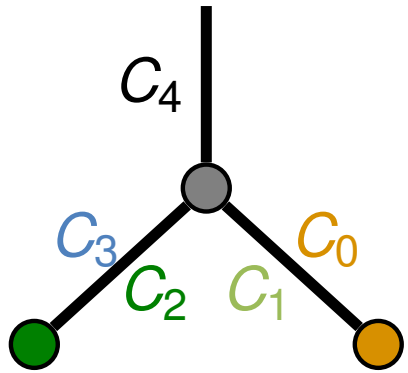


- Unroll and pipeline all operations.

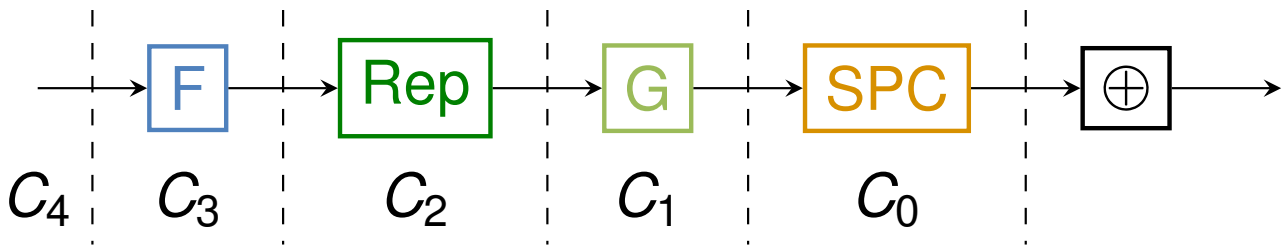


The Unrolled Decoder

- (8, 4) polar code:

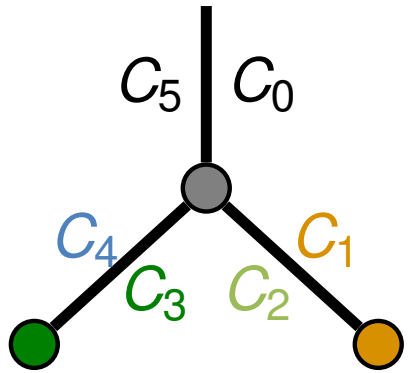


- Unroll and pipeline all operations.

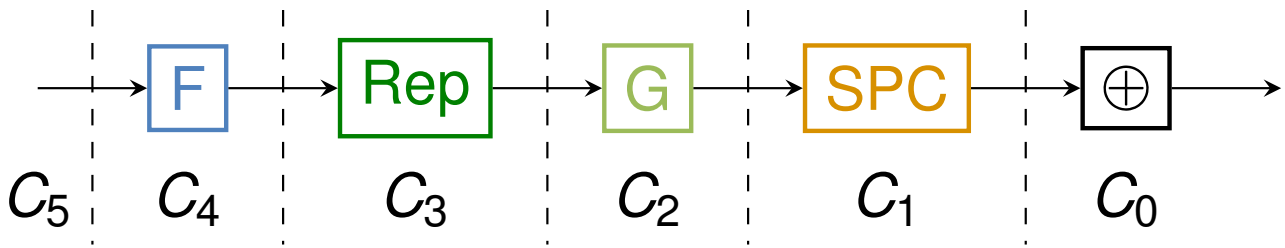


The Unrolled Decoder

- (8, 4) polar code:



- Unroll and pipeline all operations.

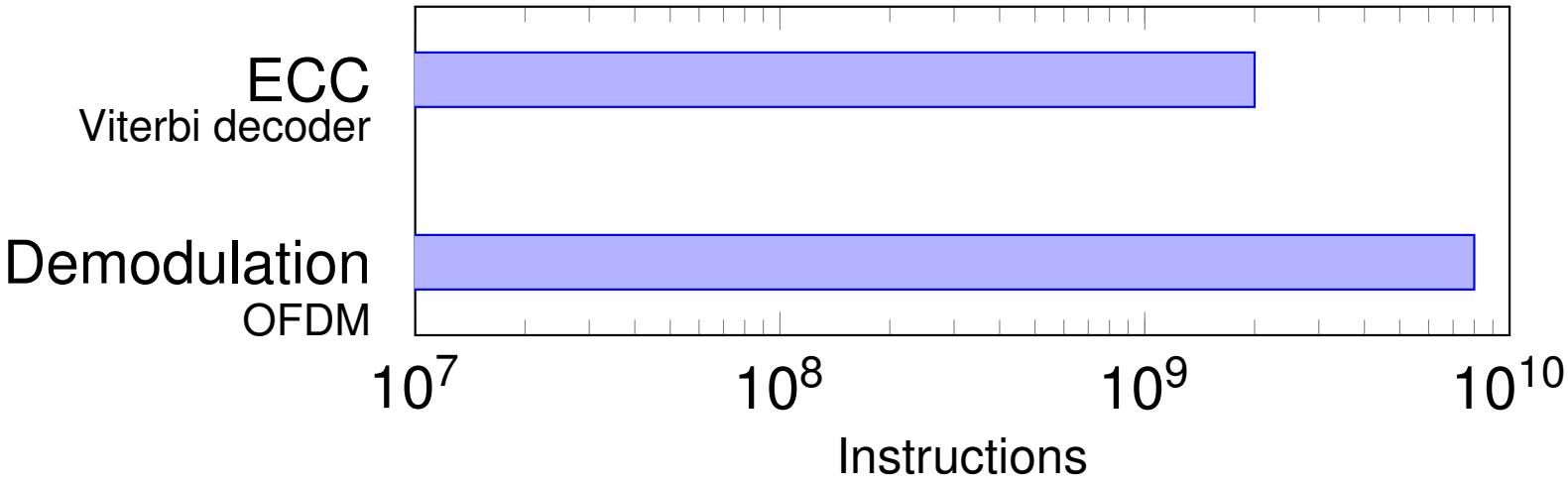


The Unrolled Decoder Implementation

LUT	FF	RAM (bits)	f (MHz)	Info. T/P (Gbps)
SP-SC				
4,130	1,388	11,904	196	0.04
Unrolled				
155,858	158,185	285,120	231	118.5
BP (ASIC)				
			300	2.3

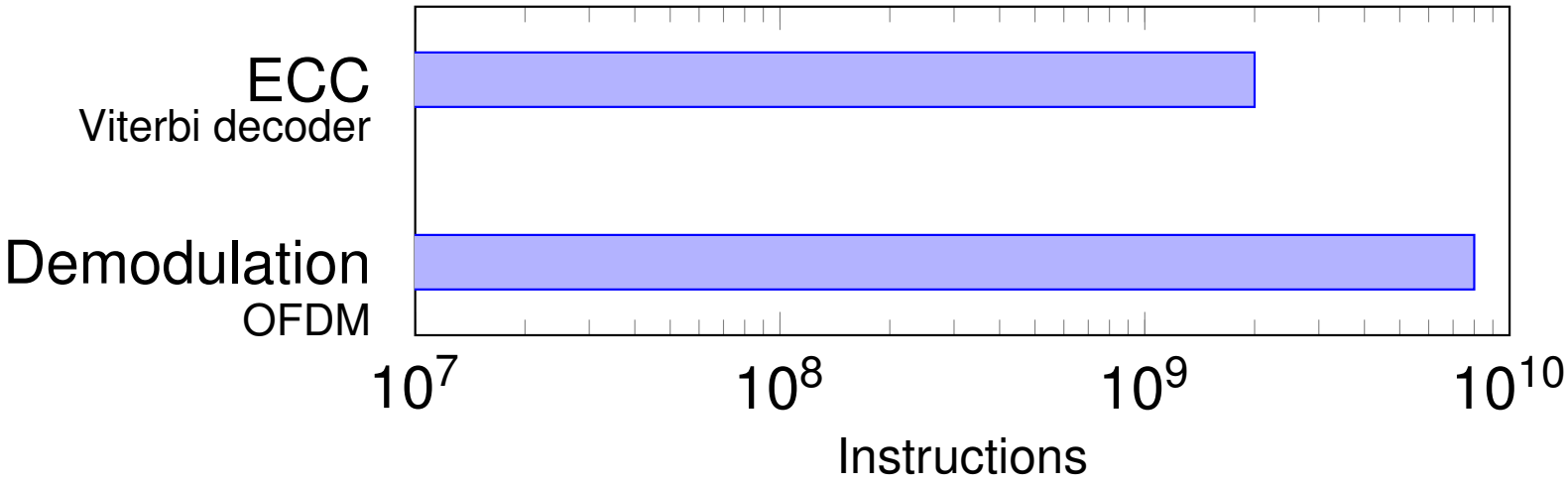
For a (1024, 512) polar code.

SDR and Modern Software ECC



Demel et al. “A LTE Receiver Framework Using GNU Radio,” JSPS, 2015.

SDR and Modern Software ECC



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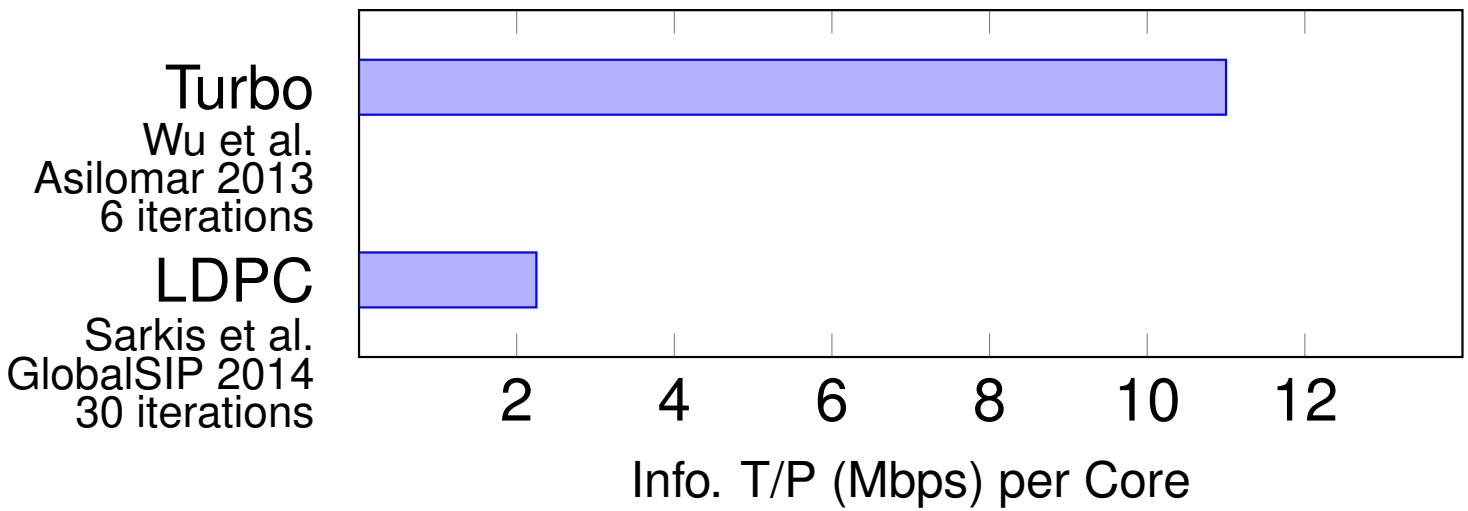

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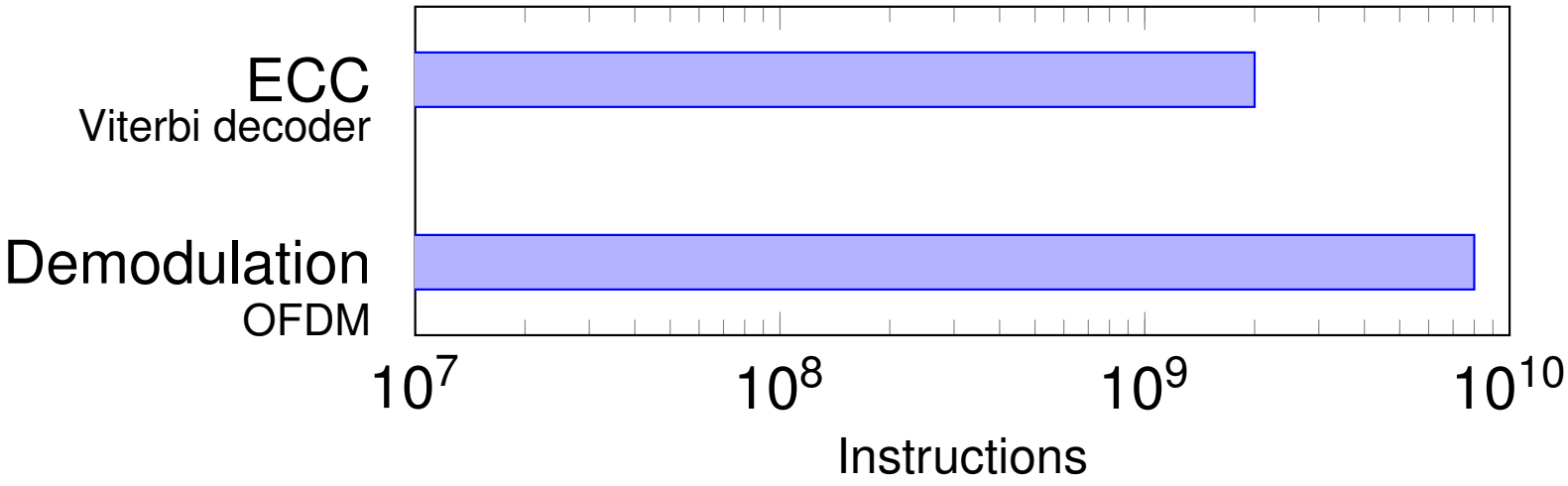

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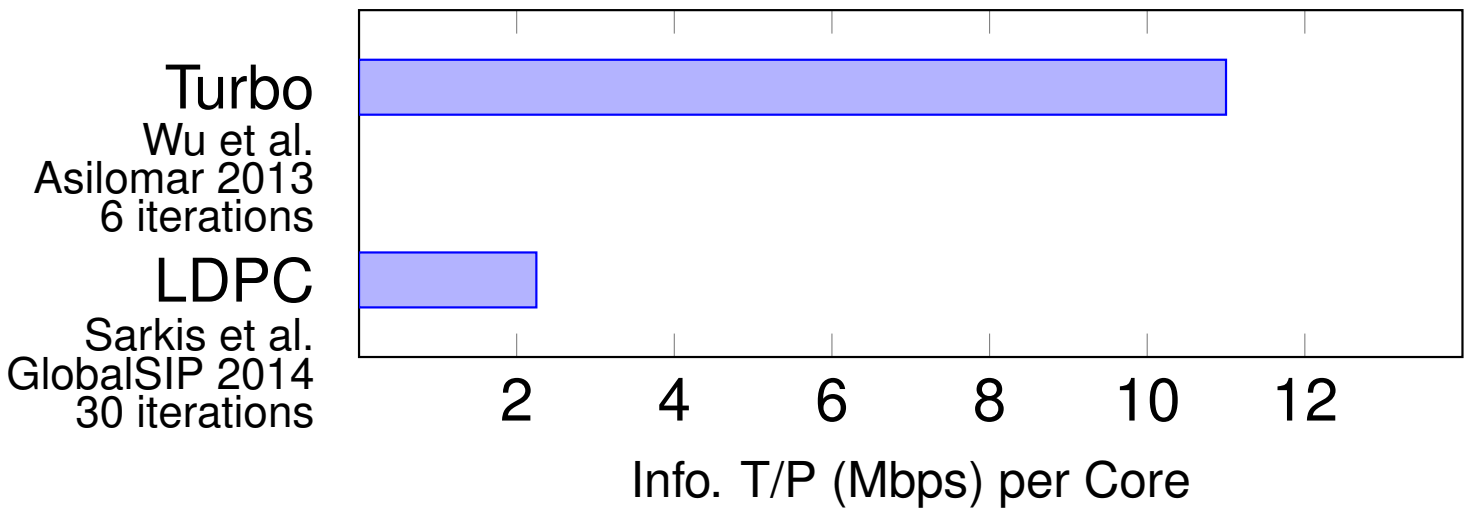
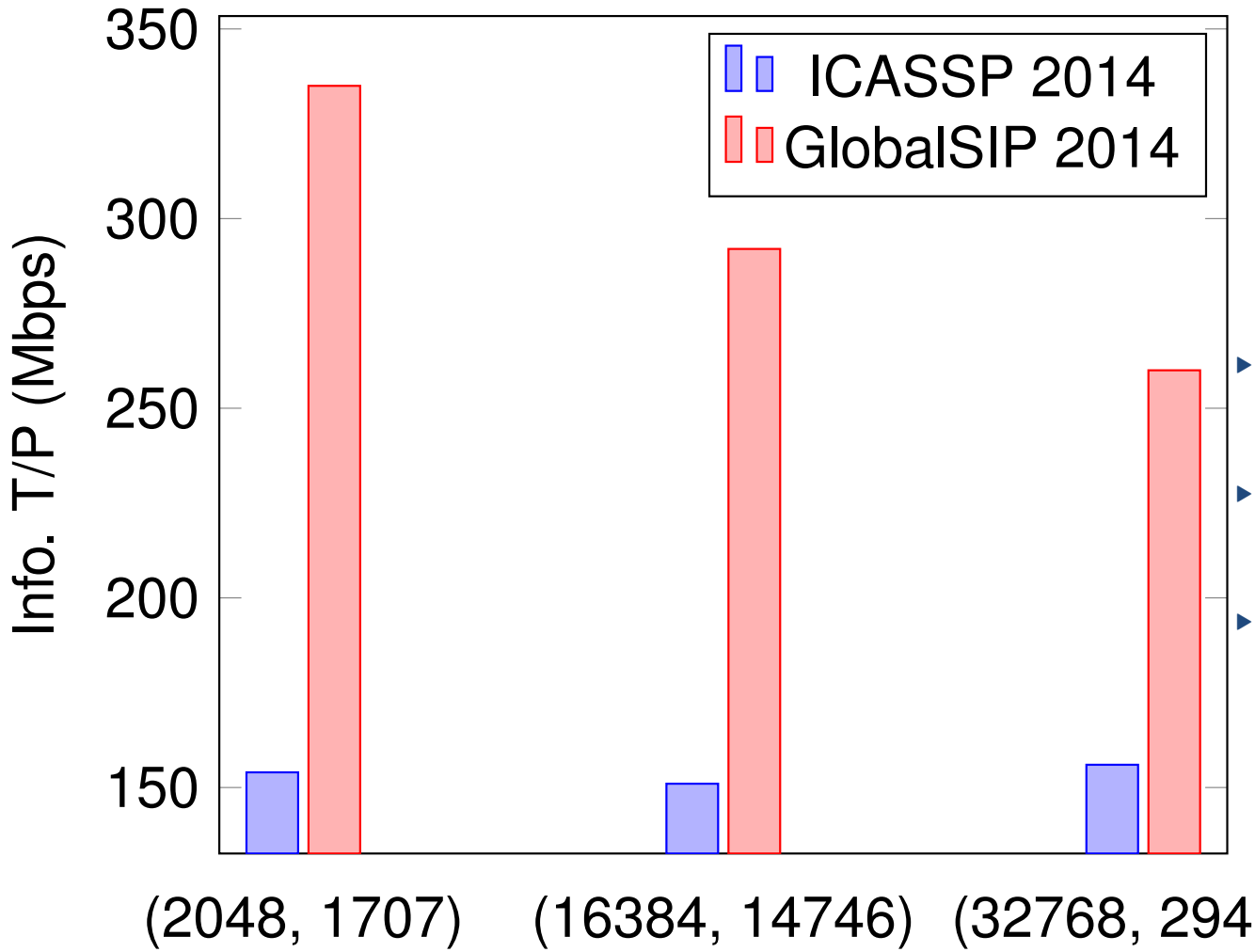


Goal: 50Mbps!

Floating-Point Throughput



- SIMD.
- Branchless.
- Single core.

Giard et al. “Fast Software Polar Decoders,” ICASSP 2014.
Sarkis et al. “Autogenerating Software Polar Decoders,” GlobalSIP 2014.

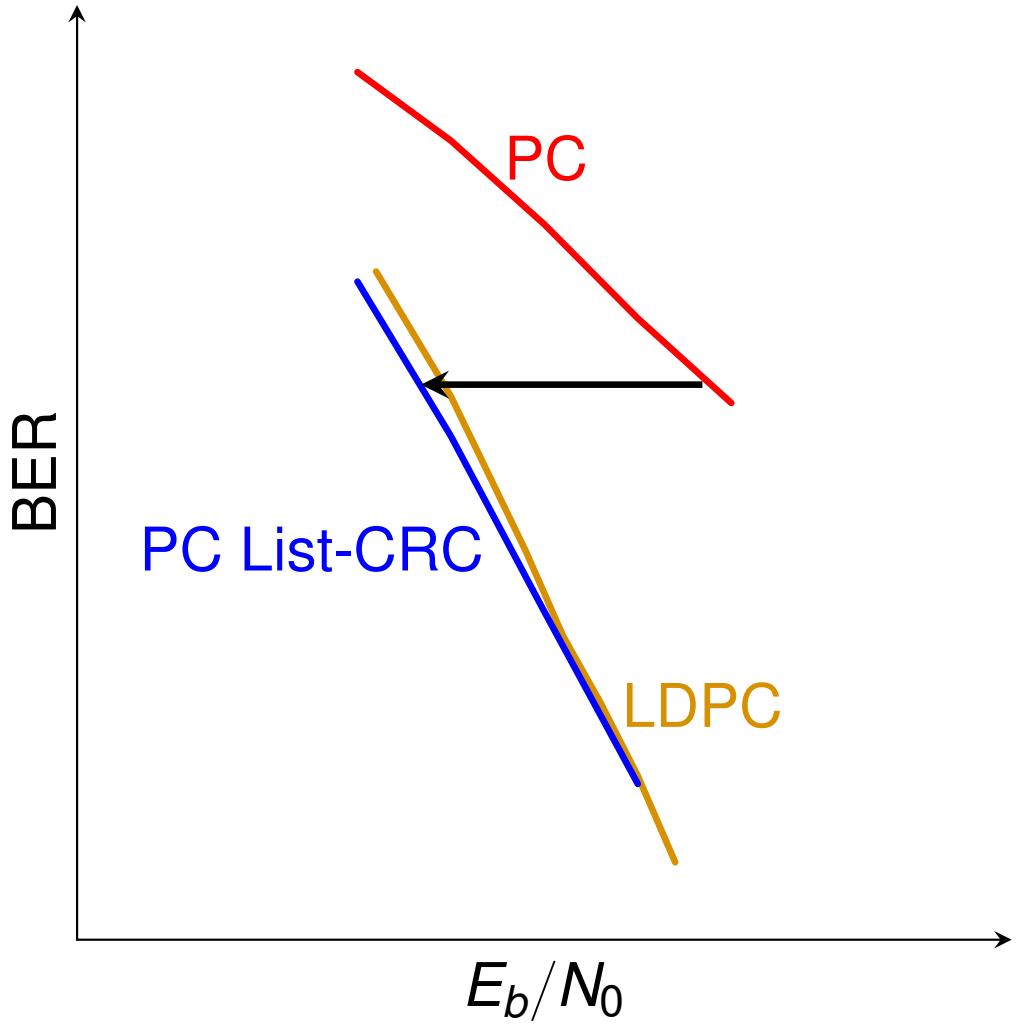
Fixed-Point Software Polar Decoders

Decoder	$f(GHz)$	Info. T/P (Mbps)	Latency μs
Le Gal et al.	3.6+	1,557	605
Fast-SSC-`int8`	3.1+	1,412	21

(32768, 29492) polar code.

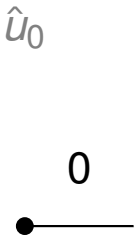
Le Gal et al. “Multi-Gb/s Software decoding of Polar Codes,” TSP 2015.
Giard et al. “Low-latency Software Polar Decoders,” *in preparation*.

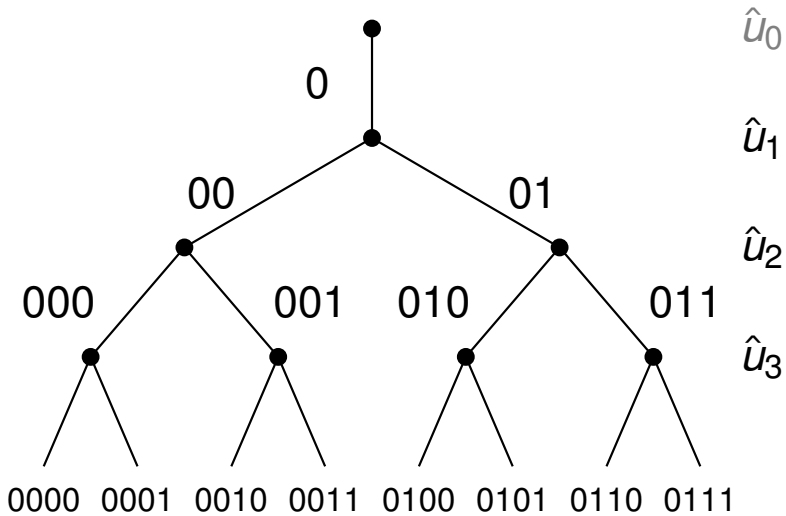
Improving Finite-Length Error-Correction Performance



List Decoding

- For each information bit, continue decoding assuming both 0 and 1.





- Select paths according to reliability values.

List Decoding

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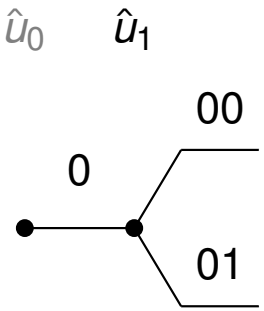

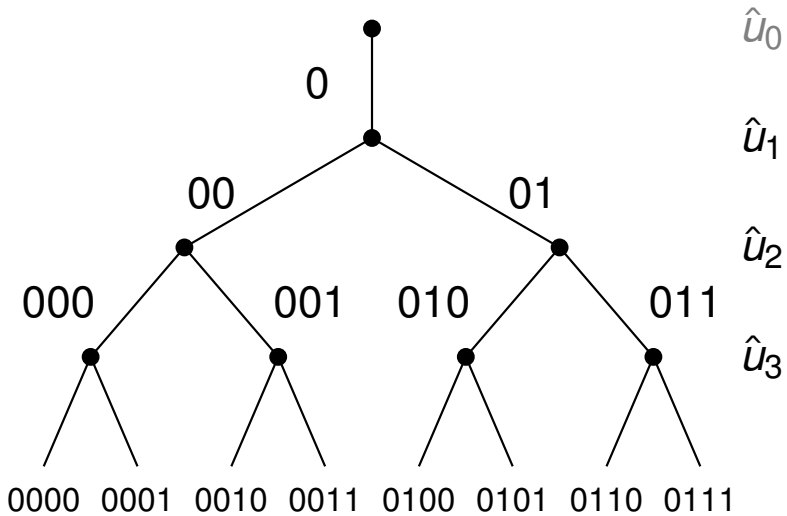

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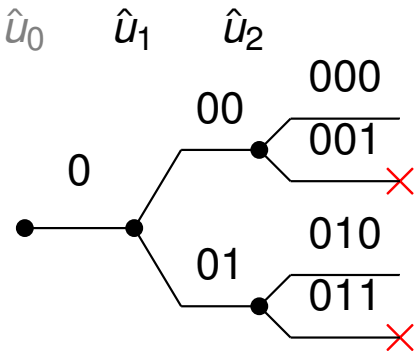

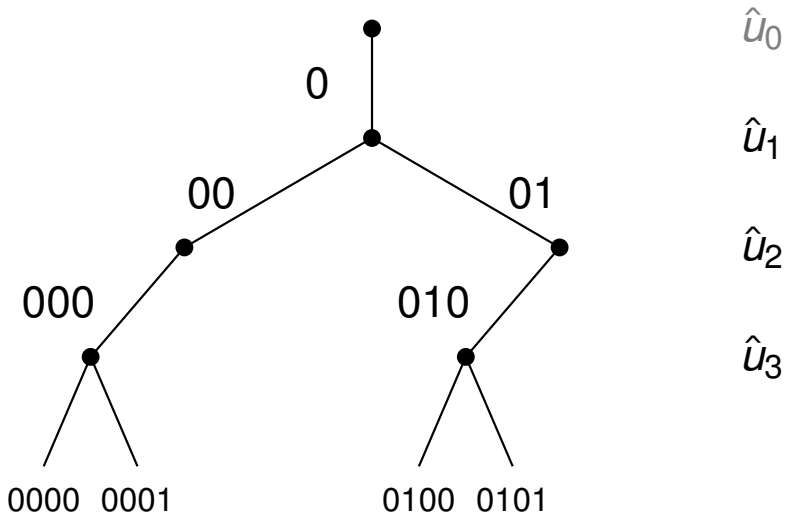

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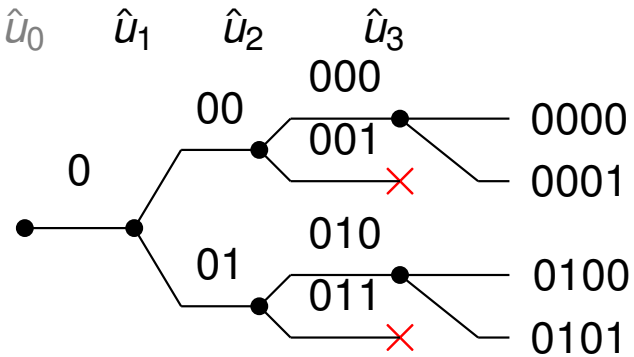

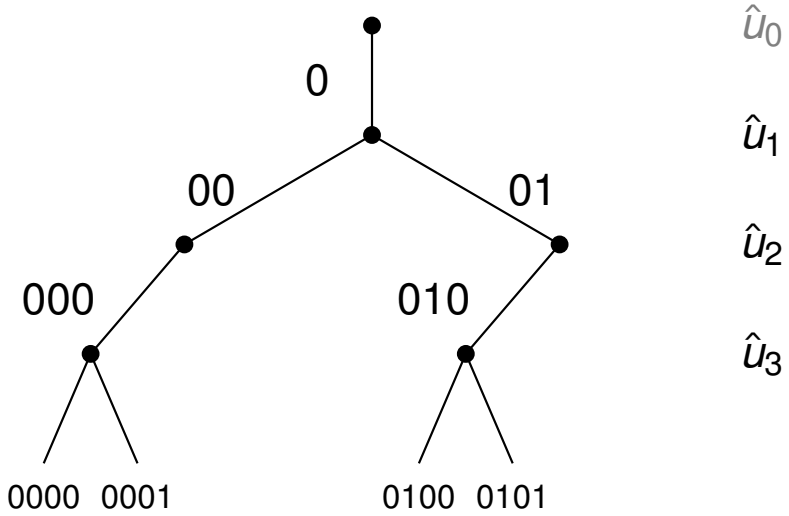

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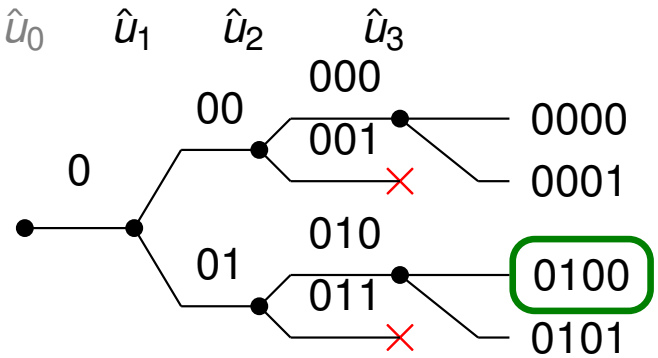

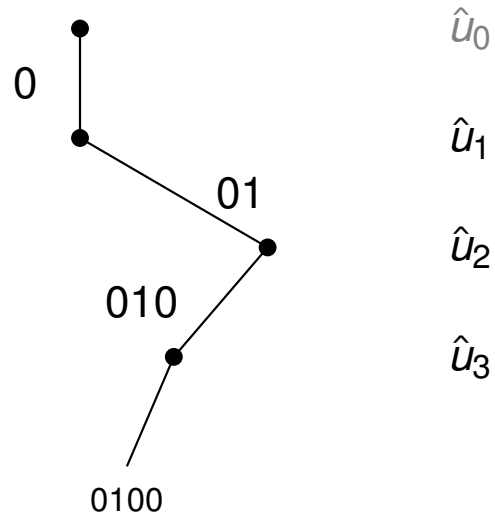

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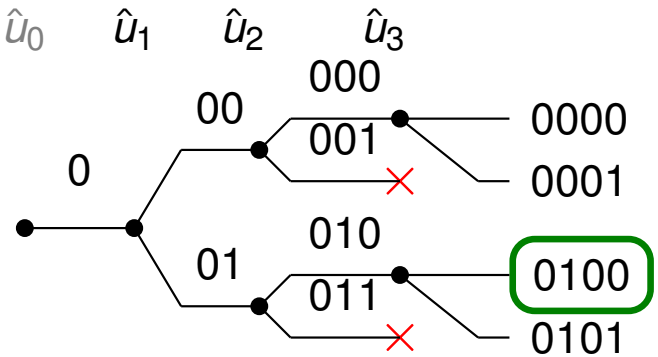
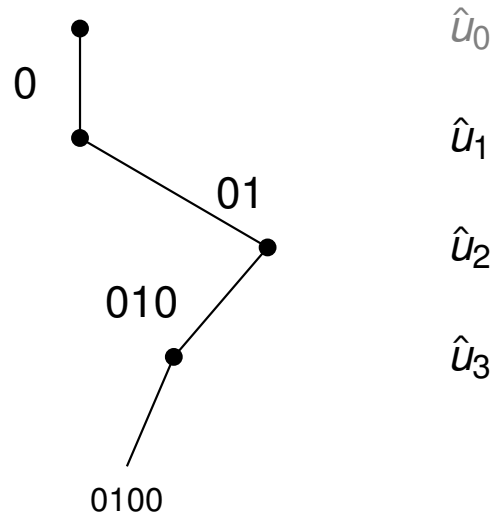
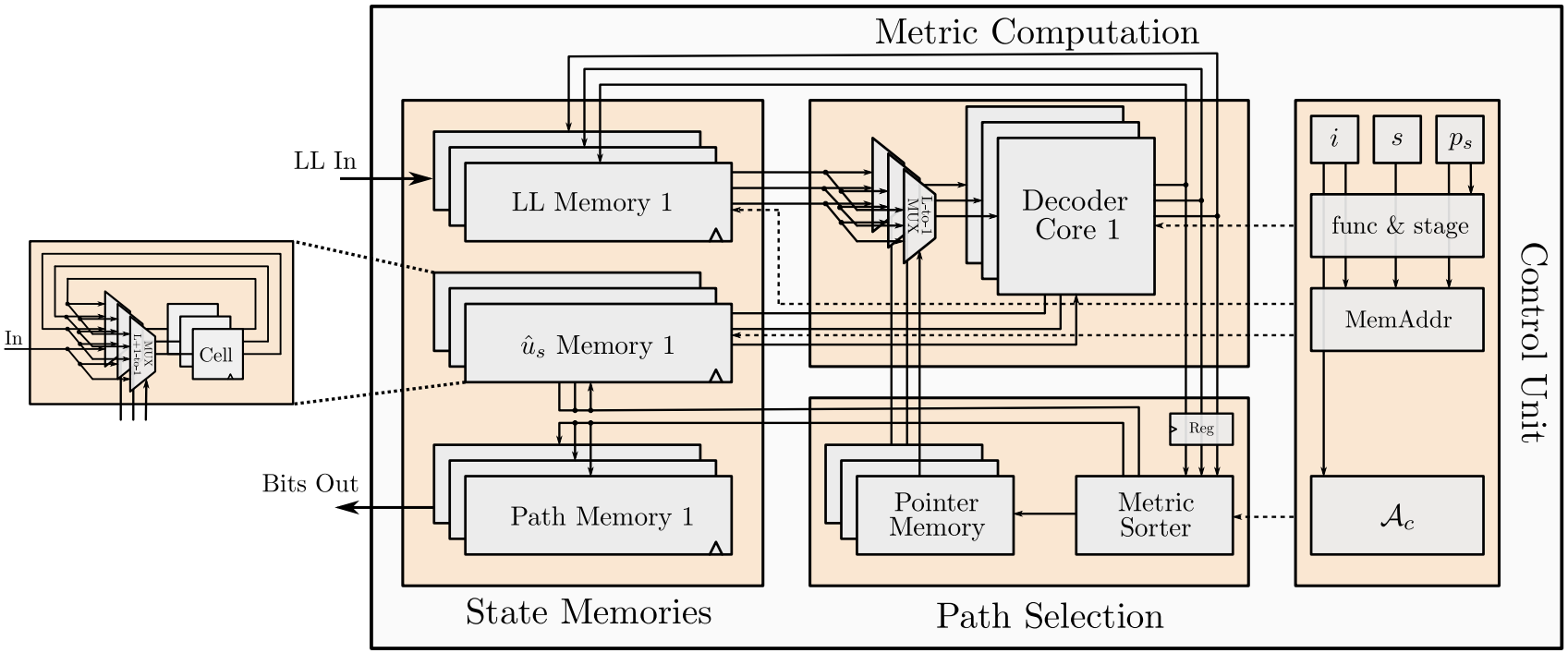




- Select paths according to reliability values.
- Using a CRC to select the output yields a significant improvement.

ASIC Implementation



- Synthesis results for $N = 1024$ using UMC 90nm:

L	Area (mm^2)	f (MHz)	T/P (Mbps)
2	1.60	459	$181R$
4	3.53	314	$89R$

Two-Step SW List Decoder

- List decoders are slower than Fast-SSC decoders.
- List have better error-correction performance than Fast-SSC decoders.

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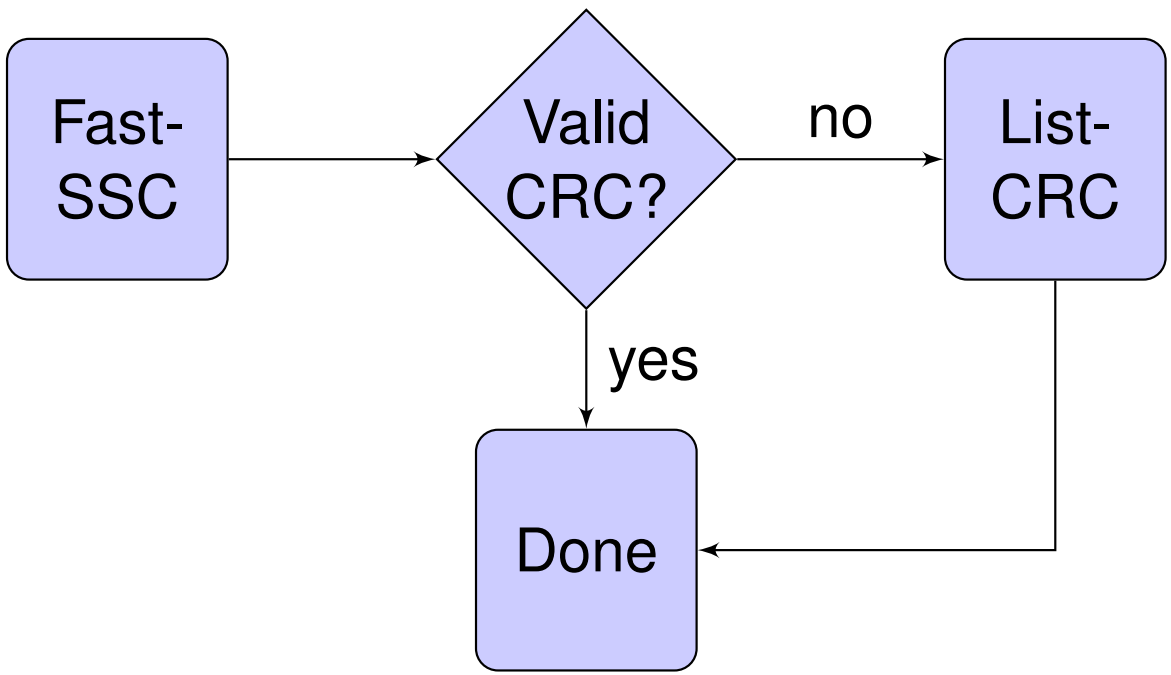
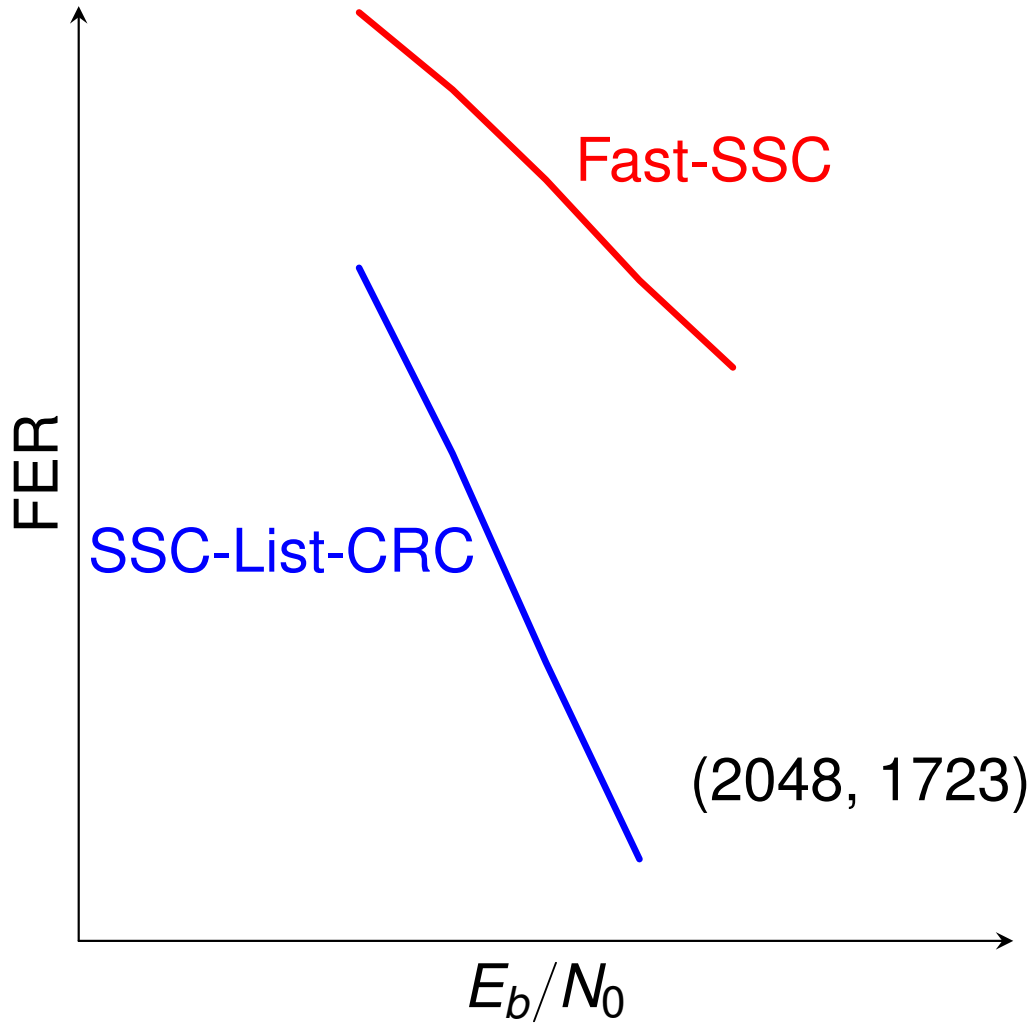
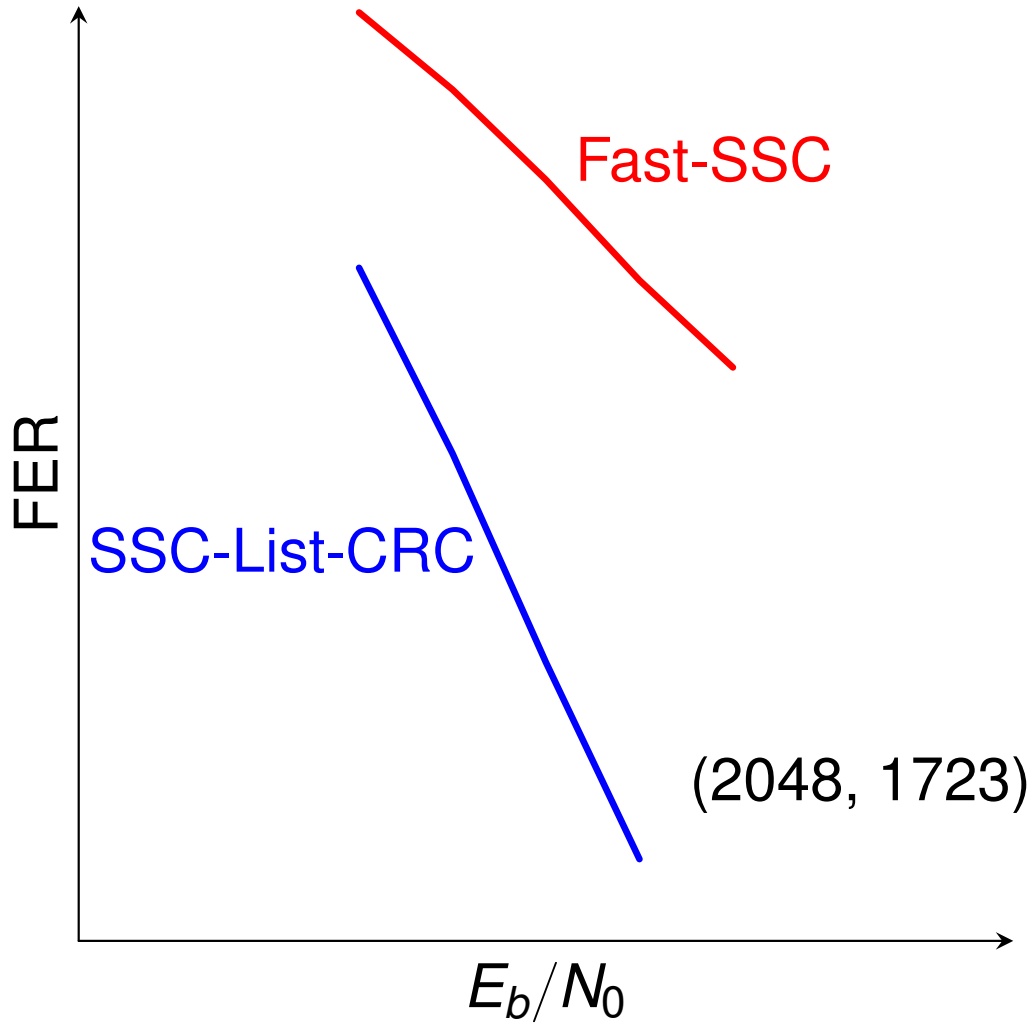
- List have better error-correction performance than Fast-SSC decoders.
- Combine both:



Two-Step SW List Decoder

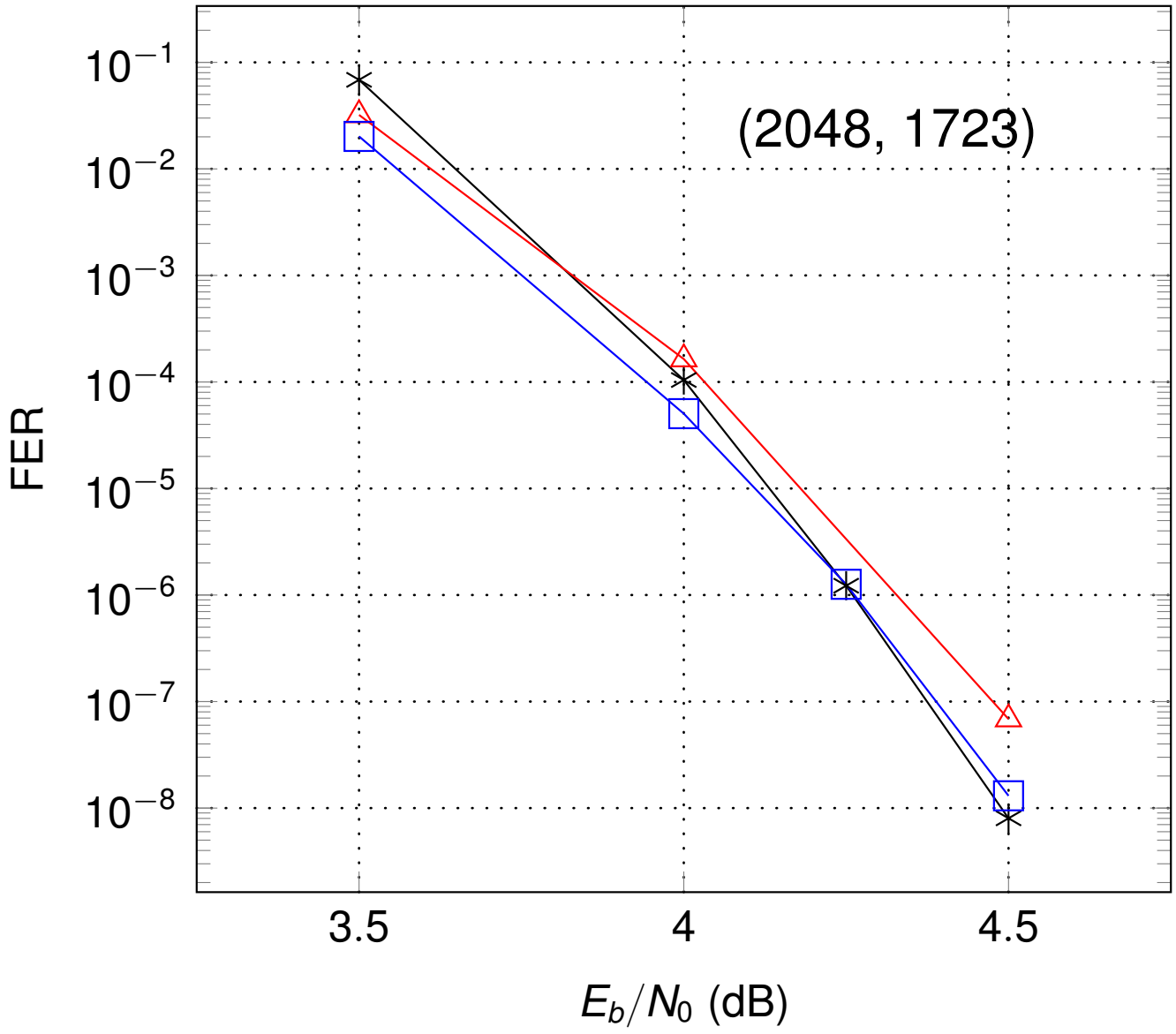


Two-Step SW List Decoder

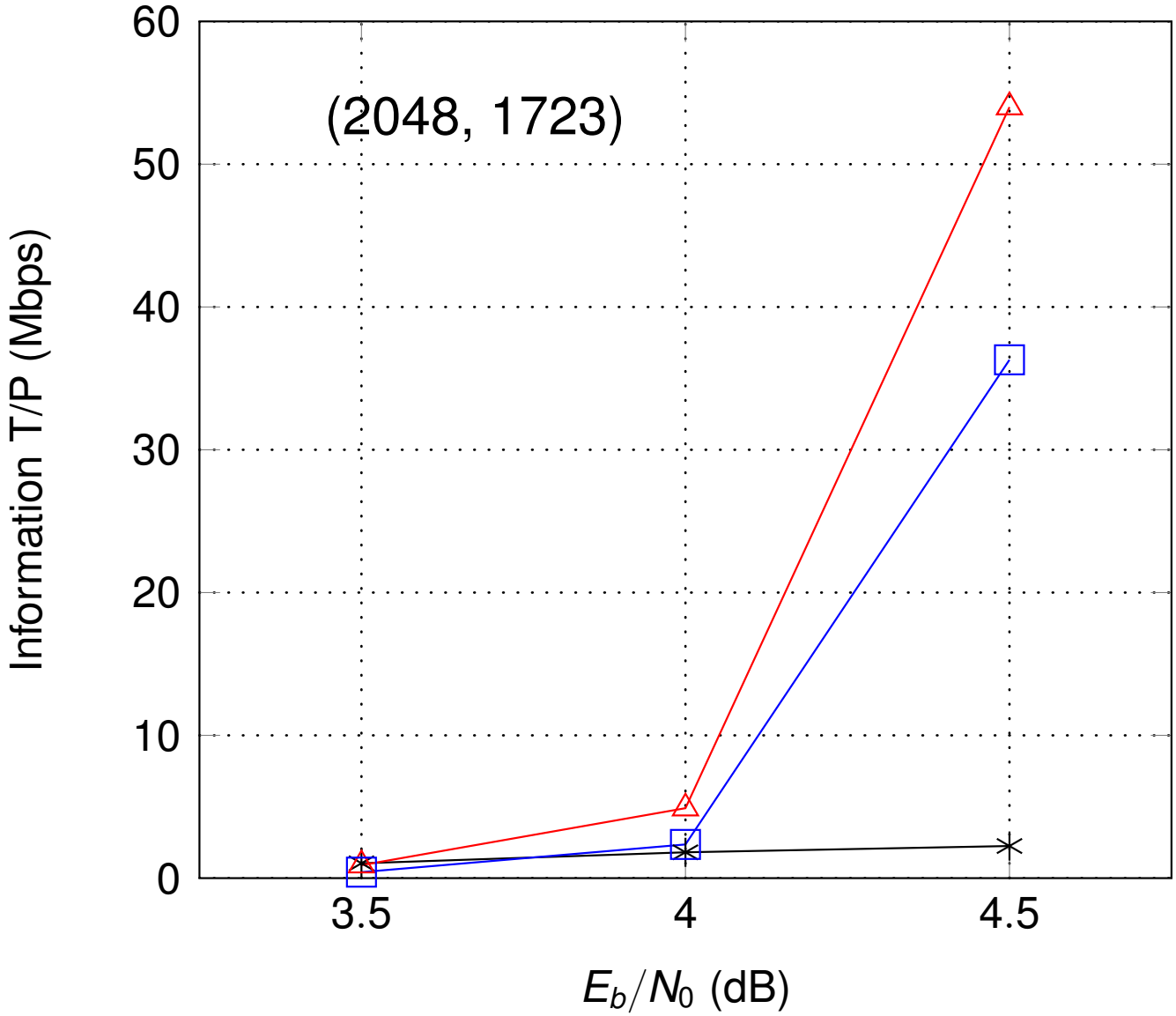


$$\mathcal{T} = \frac{k}{(1-\mathrm{FER_F})\mathcal{L}(\text{Fast-SSC}) + \mathrm{FER_F}\mathcal{L}(\text{List})} \text{ bit/s}$$

Two-Step SW List Decoder



Two-Step SW List Decoder



Conclusion

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Thank you!