Follow along at https://slides.com/russtedrake/rl-2020-bc/live or view later at https://slides.com/russtedrake/rl-2020-bc/

A Few Challenge Problems from Robotics

Russ Tedrake





#### My goals for today

How well is control working in robotics today?

- A few core questions/challenges
  - What role can simulation play?
  - Why/when does gradient-based policy search work?
  - Parameterizations/algorithms from control.
  - RL in the rare-event regime.
- Challenge problem instances
  - Raibert's hopper, planar gripper, plates, onions, shoe laces.

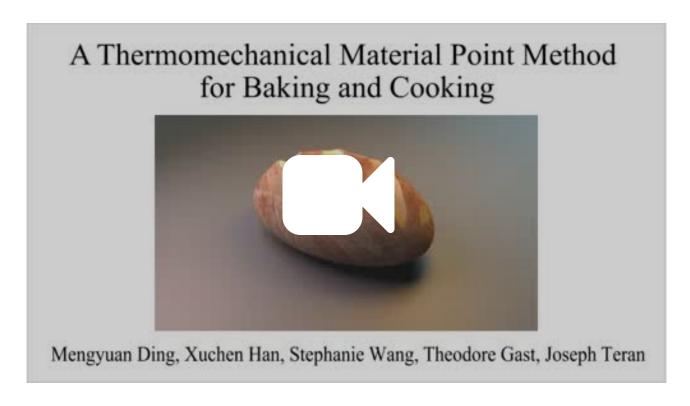
#### How well is control working in robotics?

https://www.youtube.com/embed/fRj34o4hN4I? enablejsapi=1&mute=1



#### Feels like an opportunity for RL?

Is the task difficult because we don't have a model?



## What role can simulation play?

for spreading peanut butter, buttoning my shirt, etc.

As more people started applying RL to robots, we saw a distinct shift from "model-free" RL to "model-based" RL.

(most striking at the 2018 Conference on Robot Learning)

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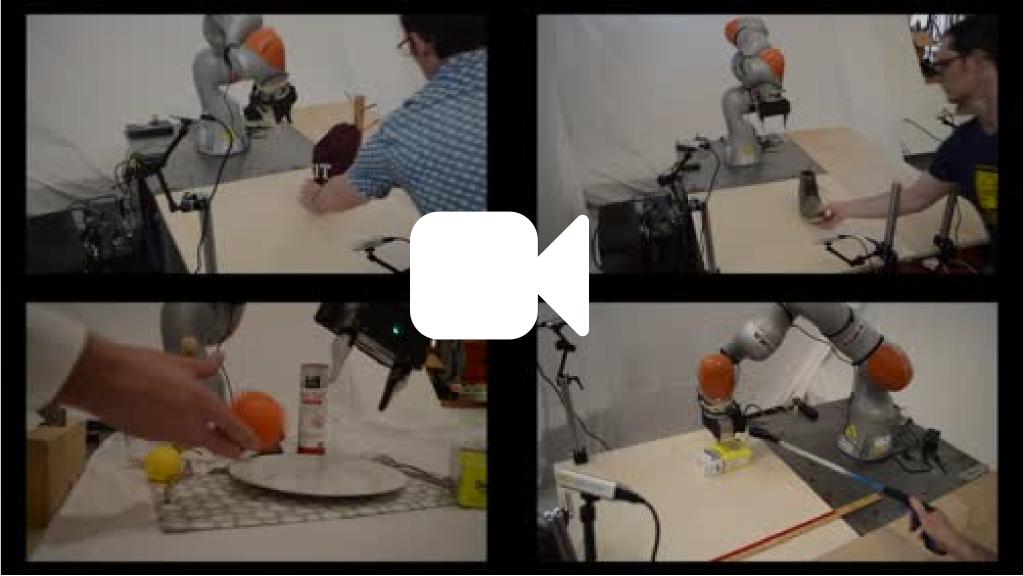
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Recent IFRR global panel on "data-driven vs physicsbased models" As more people started applying RL to robots, we saw a distinct shift from "model-free" RL to "model-based" RL.

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(caveat: I didn't choose the panel name)

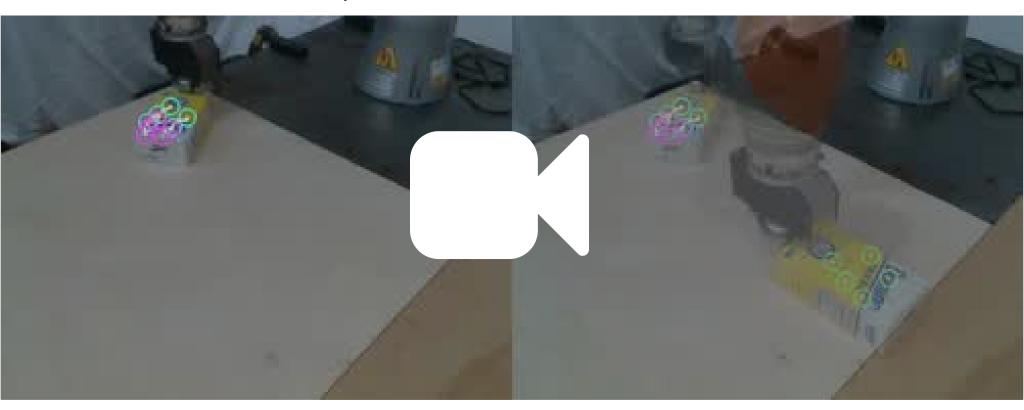


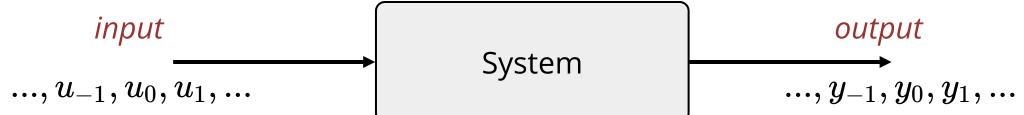
Core technology: Deep learning perception module that learns "dense correspondences"

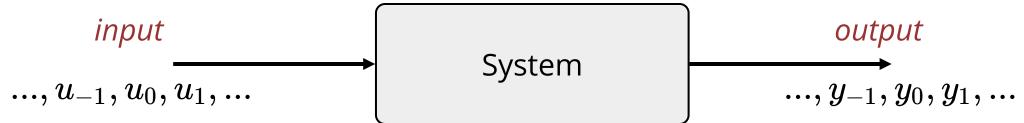


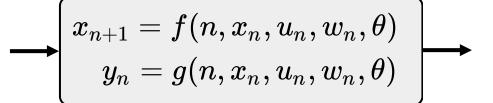
Learn a *deep* dynamic model of "keypoint" dynamics.

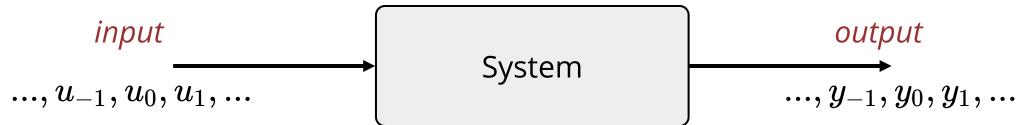
Online: use model-predictive control (MPC)

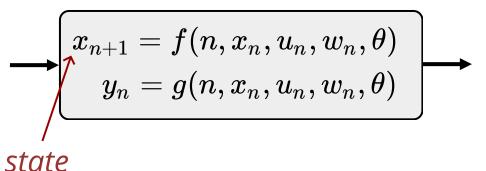


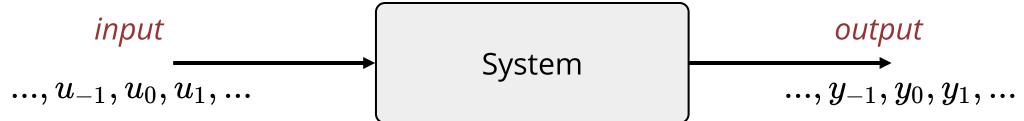


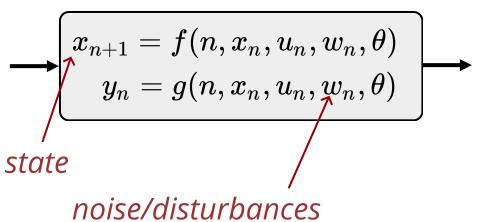


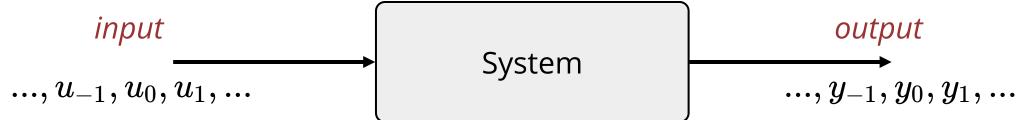


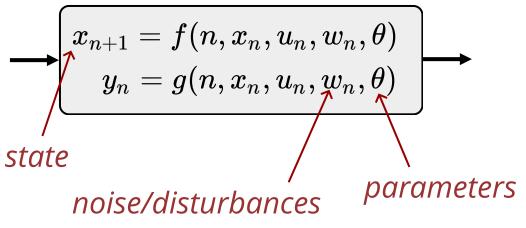


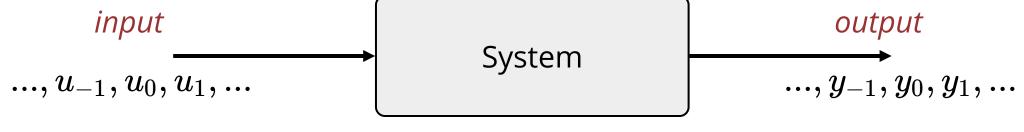


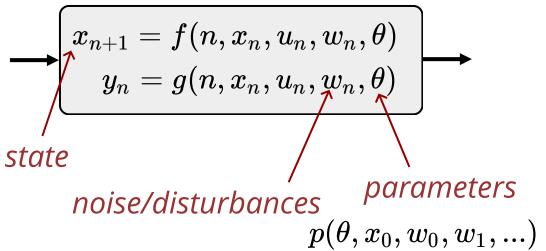


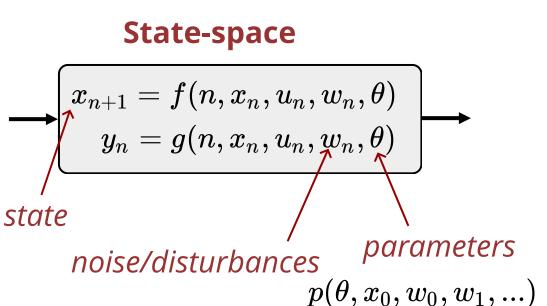


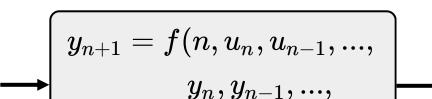






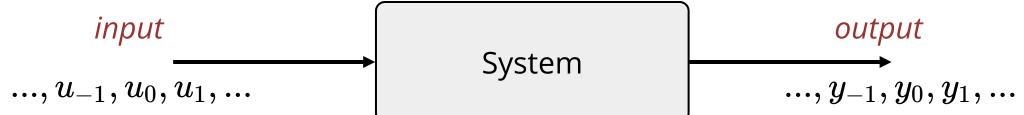






 $(w_n,w_{n-1},..., heta)$ 

**Auto-regressive (eg. ARMAX)** 



$$\underbrace{ \begin{array}{c} \textit{input} \\ ..., u_{-1}, u_0, u_1, ... \end{array}}_{\textit{System}} \underbrace{ \begin{array}{c} \textit{output} \\ ..., y_{-1}, y_0, y_1, ... \end{array}}_{\textit{output}}$$

## State-space

$$oldsymbol{
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Lagrangian mechanics, Recurrent neural networks (e.g. LSTM), ...

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Lagrangian mechanics, Feed-forward networks Recurrent neural networks (e.g. LSTM), ... (e.g.  $y_n$ = image)

**Auto-regressive (eg. ARMAX)** 

 $y_{n+1} = f(n, u_n, u_{n-1}, ...,$ 

 $y_n, y_{n-1}, ...,$ 

 $w_n,w_{n-1},..., heta)$ 

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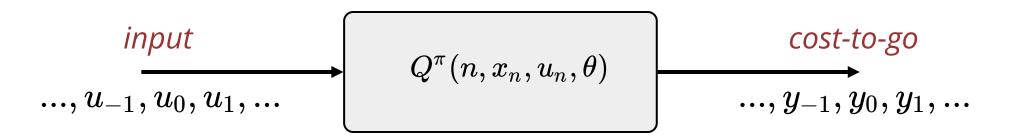
Lagrangian mechanics, Recurrent neural networks (e.g. LSTM), ... Auto-regressive (eg. ARMAX)  $y_{n+1} = f(n,u_n,u_{n-1},...,$ 

 $y_n, y_{n-1}, ...,$ 

 $w_n, w_{n-1}, ..., heta)$ Feed-forward networks

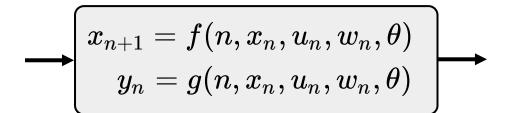
(e.g.  $y_n$ = image)

#### Models come in many forms

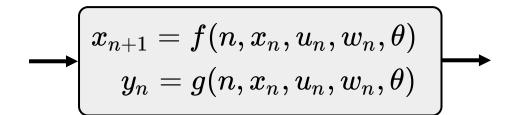


Q-functions are models, too. They try to predict only one output (the cost-to-go).

As you know, people are using Q-functions in practice on non-Markovian state representations.



• *f* and *g* describe the model class.



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#### "Deep models vs Physics-based models?" is about model **class**:

Should we prefer writing f and g using physics or deep networks?

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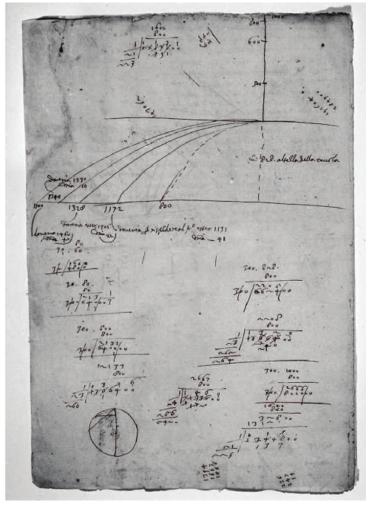
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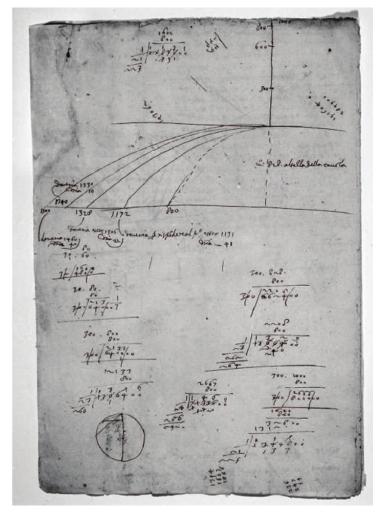
Maybe not so different from

- should we use ReLU or tanh?
- should we use LSTMs or Transformers?



Galileo's notes on projectile motion

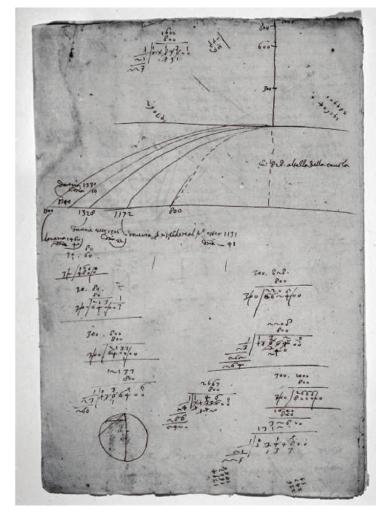
They fit very simple models to very noisy data.



Galileo's notes on projectile motion

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Gave us a rich *class* of parametric models that *we* could fit to new data.

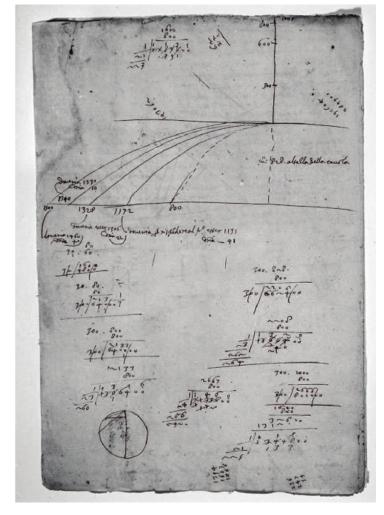


Galileo's notes on projectile motion

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Gave us a rich *class* of parametric models that *we* could fit to new data.

What if Newton had deep learning...?



Galileo's notes on projectile motion

"All models are wrong, but some are useful" -- George Box

#### What makes a model useful?

#### e.g., for

- generating synthetic training data
- Monte-Carlo policy evaluation
- offline policy optimization



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Unreal 5 engine trailer

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Unreal 5 engine trailer

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- *Corollary:* Reliable system identification (data  $\Rightarrow \theta$ )
- Generalizable, efficient, repeatable, interpretable/debuggable, ...



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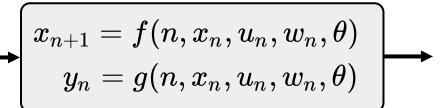
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- Observable
- Task-relevant

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State-space models tend to be more efficient/compact, but require *state estimation*.

#### **State-space**



VS.

$$y_{n+1}=f(n,u_n,u_{n-1},...,\ y_n,y_{n-1},...,\ w_n,w_{n-1},..., heta)$$

**Auto-regressive** 

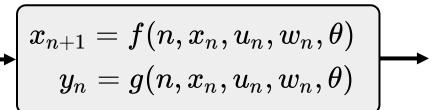
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- Doesn't imply "no mechanics"

#### **State-space**

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**Auto-regressive** 

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  - Conservation of mass
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  - Inverse dynamics have "branch-induced sparsity"

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  - Inertial matrix is positive definite
  - Inverse dynamics have "branch-induced sparsity"
- Without structure, maybe we can only ever do stochastic gradient descent...?

For e.g. onions, laundry, peanut butter, ...

The failings of our physics-based models are mostly due to the **unreasonable** burden of estimating the "Lagrangian state" and parameters.

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The failings of our deep models are mostly due to our inability to due *efficient/reliable* planning, control design and analysis.

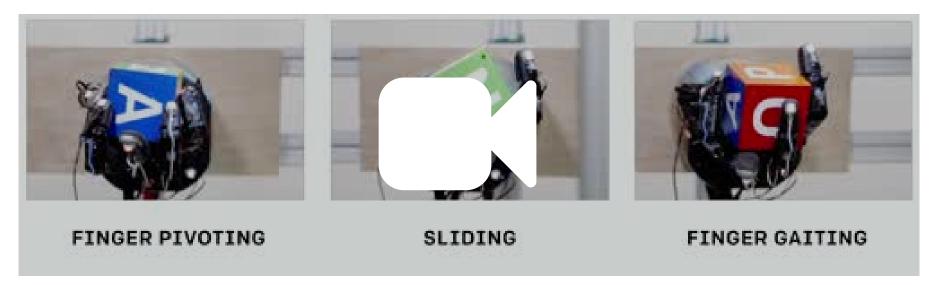
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The failings of our physics-based models are mostly due to the **unreasonable** burden of estimating the "Lagrangian state" and parameters.

The failings of our deep models are mostly due to our inability to due *efficient/reliable* planning, control design and analysis.

I want the next Newton to come around and to work on onions, laundry, peanut butter...

# Why/when does gradient-based policy search work?



**OpenAl** - Learning Dexterity

"PPO has become the default reinforcement learning algorithm at OpenAl because of its ease of use and good performance."

https://openai.com/blog/openai-baselines-ppo/

#### Global Convergence of Policy Gradient Methods for the Linear Quadratic Regulator

Maryam Fazel<sup>1</sup>, Rong Ge<sup>2</sup>, Sham M. Kakade<sup>1</sup>, and Mehran Mesbahi<sup>1</sup>

Proceedings of Machine Learning Research vol 120:1–9, 2020

2nd Annual Conference on Learning for Dynamics and Control

#### Learning the model-free linear quadratic regulator via random search

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Ming Hsieh Department of Electrical and Computer Engineering, University of Southern California, Los Angeles, CA 90089.

#### But there are also cases where it will not work...

A simple counter-example from static output feedback:

$$\dot{x} = \mathbf{A}x + \mathbf{B}u, \quad y = \mathbf{C}x,$$

$$\mathbf{A} = egin{bmatrix} 0 & 0 & 2 \ 1 & 0 & 0 \ 0 & 1 & 0 \end{bmatrix}, \quad \mathbf{B} = egin{bmatrix} 1 \ 0 \ 0 \end{bmatrix}, \quad \mathbf{C} = egin{bmatrix} 1 & 1 & 3 \end{bmatrix},$$

$$u = -ky$$
.

The set of stabilizing k is a disconnected set.

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<i>k</i>	Maximum real closed-loop eigenvalue
0.9	-0.035
1.5	0.032
2.1	-0.009

The set of stabilizing k is a disconnected set.

### What characterizes the good cases?

- Maybe it is over-parameterization of deep policies?
  - Is there a comparable story to interpolating solutions in high-dimensional policy space?

- Maybe it is the *distribution over tasks*?
  - Control has traditionally studied algorithms that must work for all A,B,C. Maybe the world never gives us the hard ones?
  - Optimizing simultaneously over diverse tasks might be easier than optimizing over one task.

# **Lessons from Control**

(for instance: better controller parameterizations)

- Just because you *can* search over u = -Kx directly, does not mean that you should!
  - Slow convergence
  - Set of stabilizing K is nontrivial
- If model is known, searching Q and R is better.

# Feedback Controller Parameterizations for Reinforcement Learning

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Ian R. Manchester CSAIL, MIT Cambridge, MA 02139 Email: irm@mit.edu

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Youla parameterization (disturbance-based feedback)

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- Youla parameterization (disturbance-based feedback)
- LMI formulations

# Feedback Controller Parameterizations for Reinforcement Learning

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- Youla parameterization (disturbance-based feedback)
- LMI formulations
- Result in convex formulations only for linear systems, but the benefits are likely more general.

# Feedback Controller Parameterizations for Reinforcement Learning

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### Youla parameters (time-domain, no-noise)

http://underactuated.csail.mit.edu/lqr.html

$$egin{aligned} \min \sum_{n=0}^{N-1} \mathbf{x}^T[n] \mathbf{Q} \mathbf{x}[n] + \mathbf{u}^T[n] \mathbf{R} \mathbf{u}[n], & \mathbf{Q} = \mathbf{Q}^T \succeq 0, \mathbf{R} = \mathbf{R}^T \succ 0 \ & ext{subject to} & \mathbf{x}[n+1] = \mathbf{A} \mathbf{x}[n] + \mathbf{B} \mathbf{u}[n], \ & \mathbf{x}[0] = \mathbf{x}_0 \end{aligned}$$

$$egin{aligned} \mathbf{u}[n] &= \mathbf{K}_n \mathbf{x}[n], \ \mathbf{x}[1] &= \mathbf{A}\mathbf{x}_0 + \mathbf{B}\mathbf{K}_0 \mathbf{x}_0, \ \mathbf{x}[2] &= \mathbf{A}(\mathbf{A} + \mathbf{B}\mathbf{K}_0) \mathbf{x}_0 + \mathbf{B}\mathbf{K}_1 (\mathbf{A} + \mathbf{B}\mathbf{K}_0) \mathbf{x}_0 \ \mathbf{x}[n] &= \left(\prod_{i=0}^{n-1} (\mathbf{A} + \mathbf{B}\mathbf{K}_i) 
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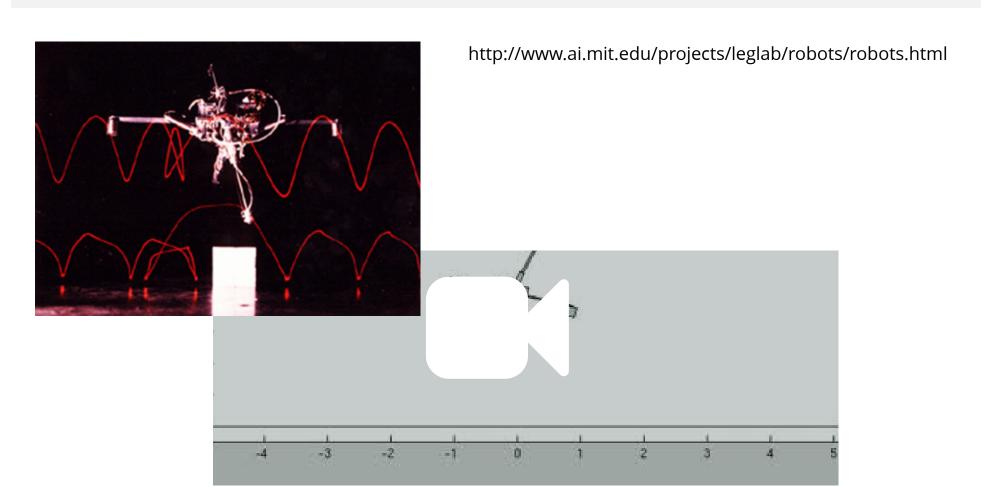
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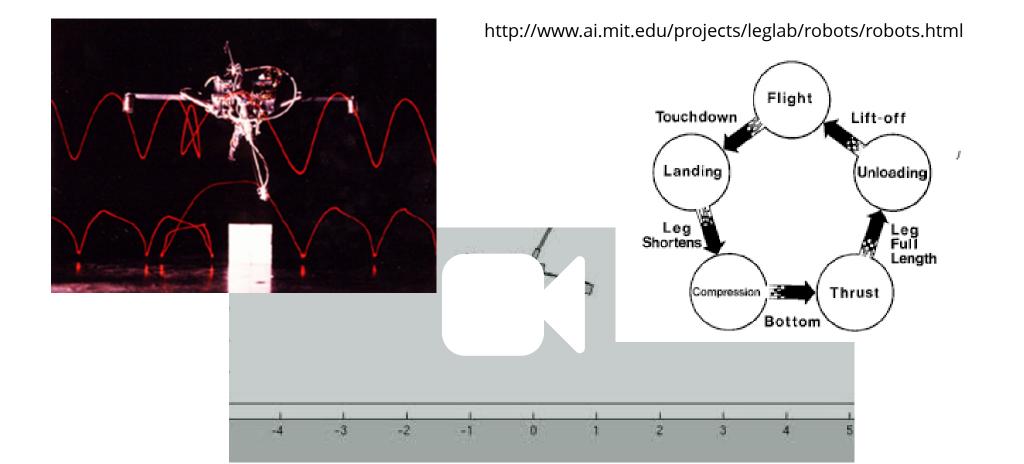
# Control parameterizations from the "robot whisperers"



# The MIT Leg Lab Hopping Robots



# The MIT Leg Lab Hopping Robots



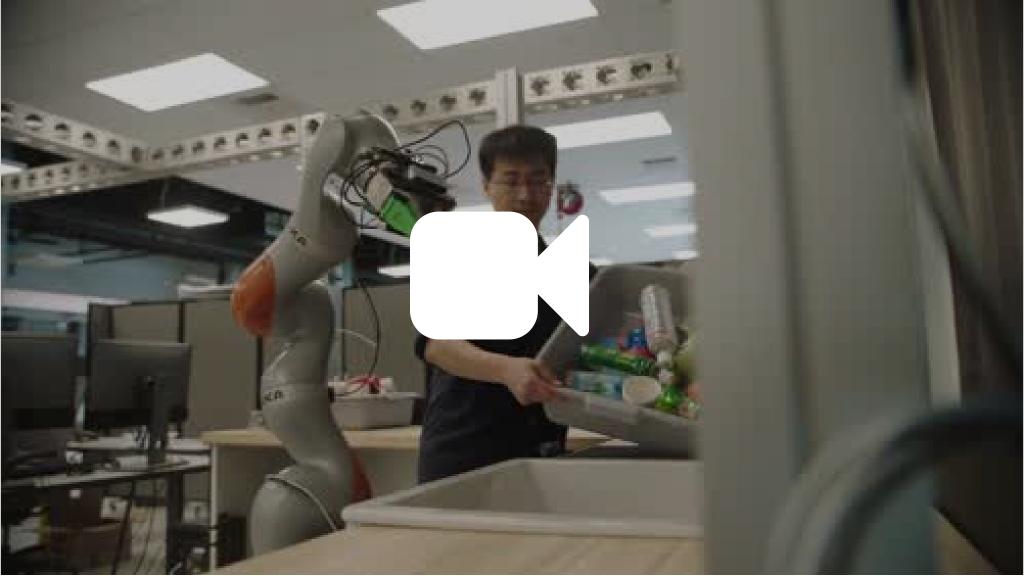
# RL in the rare-event regime (for robotics)

#### **Motivation**

Consider the task of loading a dishwasher...

(One project I've been working on at TRI Robotics)

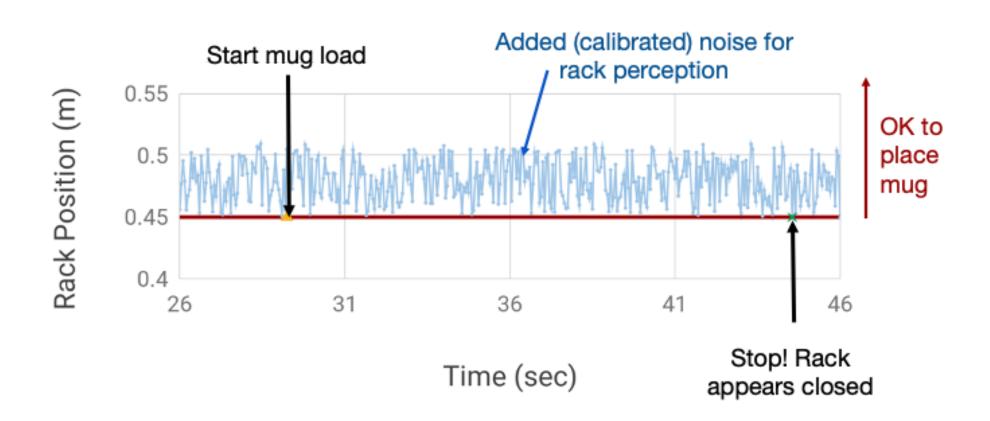


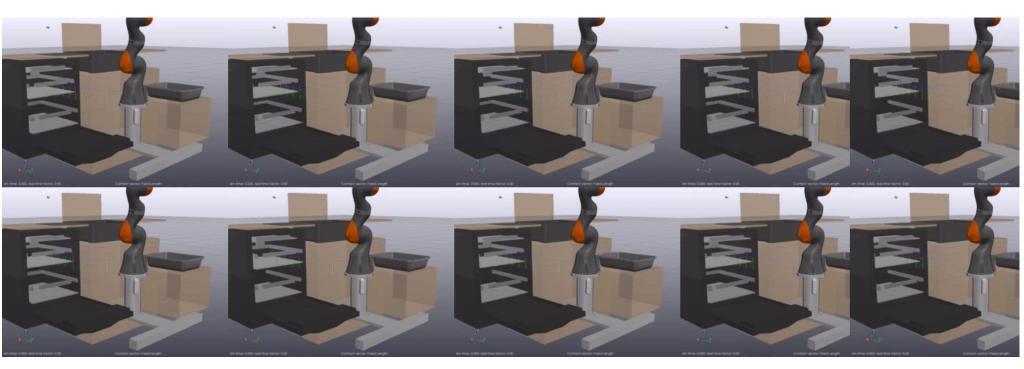






# Finding subtle bugs





# Estimating failure probability

for black-box, very highdimensional, complex simulators

- adaptive multi-level splitting
- Hamiltonian MC
- parametric warping distributions via normalizing flows

# Scalable End-to-End Autonomous Vehicle Testing via Rare-event Simulation

Matthew O'Kelly<sup>\*1</sup> Aman Sinha<sup>\*2</sup> Hongseok Namkoong<sup>\*2</sup> John Duchi<sup>2</sup> Russ Tedrake<sup>3</sup>

> <sup>1</sup>University of Pennsylvania <sup>2</sup>Stanford University <sup>3</sup>Massachusetts Institute of Technology

mokelly@seas.upenn.edu {amans,hnamk,jduchi}@stanford.edu russt@mit.edu

paper link

Neural Bridge Sampling for Evaluating Safety-Critical Autonomous Systems

Aman Sinha<sup>\*1</sup> Matthew O'Kelly<sup>\*2</sup> John Duchi<sup>1</sup> Russ Tedrake<sup>3</sup>

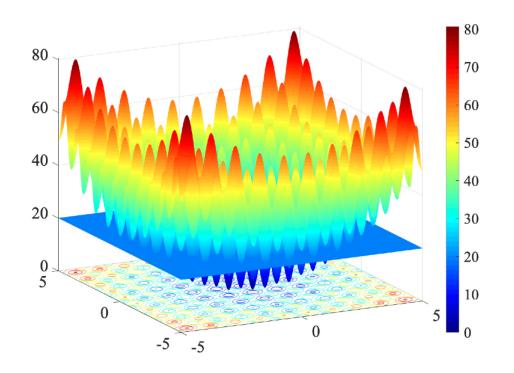
<sup>1</sup>Stanford University <sup>2</sup>University of Pennsylvania <sup>3</sup>Massachusetts Institute of Technology

amans@stanford.edu, mokelly@seas.upenn.edu, jduchi@stanford.edu, russt@mit.edu

paper link

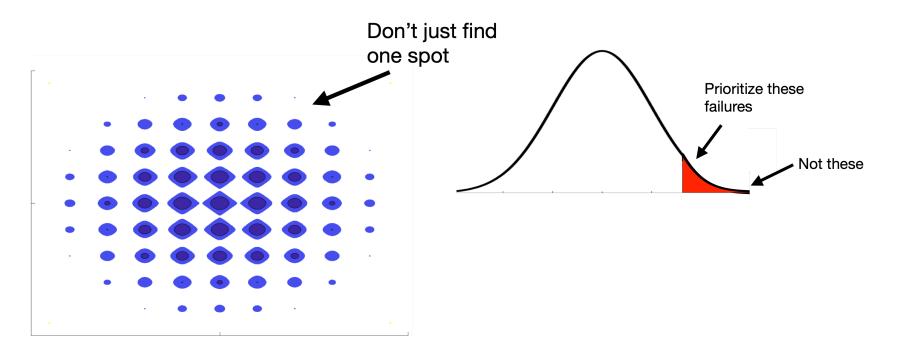
# Failure probability vs "falsification"

Falsification algorithms are not designed for coverage.

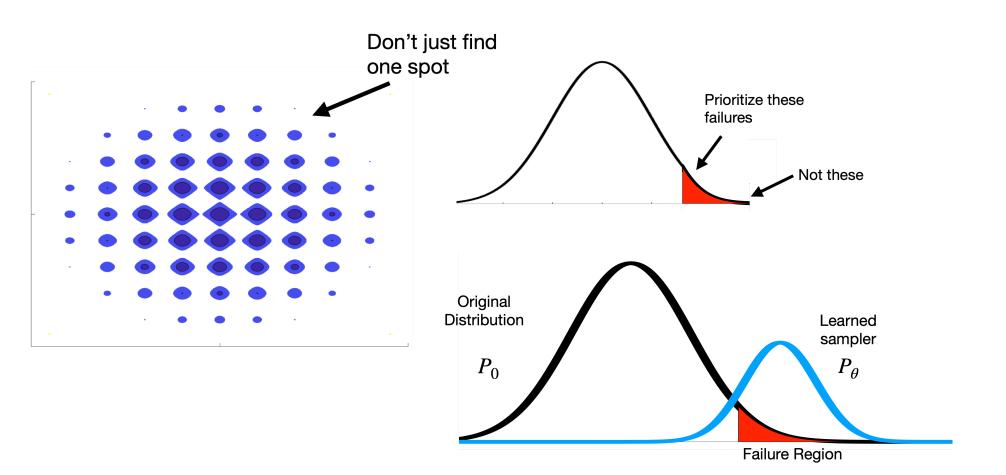


 $find \ x < 20$  VS  $estimate \ p(x < 20)$ 

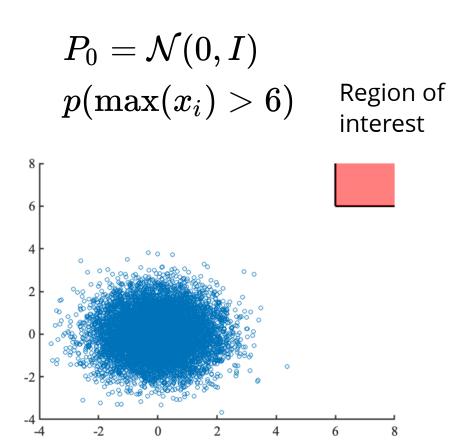
#### The risk-based framework



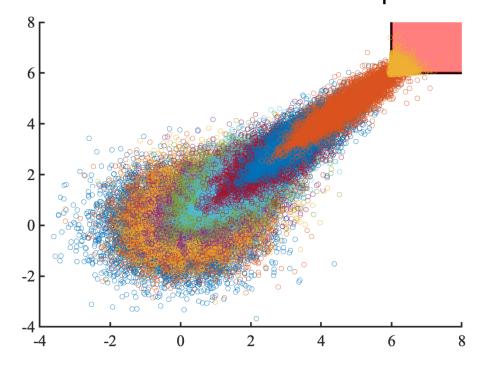
#### The risk-based framework



#### The risk-based framework



a smooth ladder of samplers



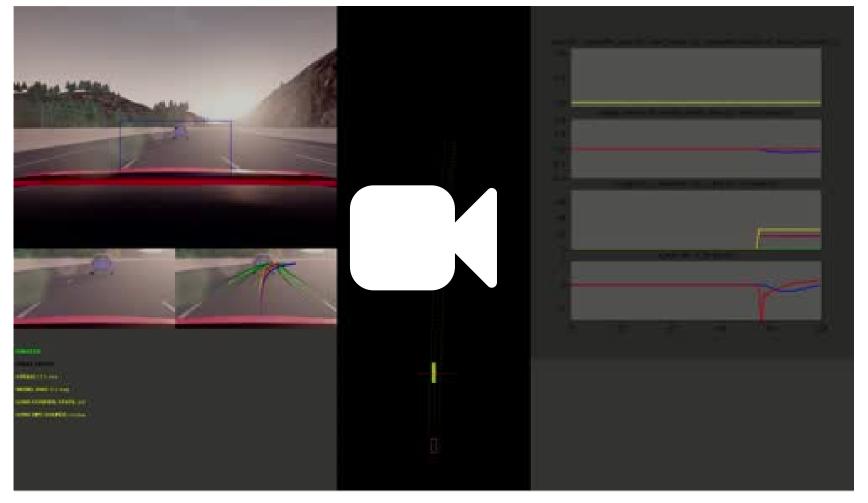
Finds surprisingly rare and diverse failures of the full comma.ai openpilot in the Carla simulator.





The primary authors have now created a startup:







### RL in the rare-event regime

Invites super interesting questions for RL / control.

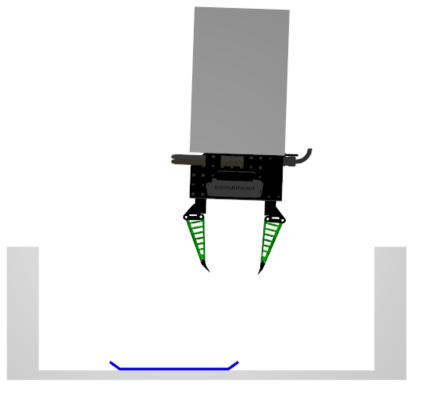
- Convinced me that empirical risk estimation might actually to scale to high dimensional data.
- Plausible formulation of "safety" in difficult domains.

 Do the parameterized warping distributions enable more efficient importance-sampling RL?

# Some specific robotics problem instances









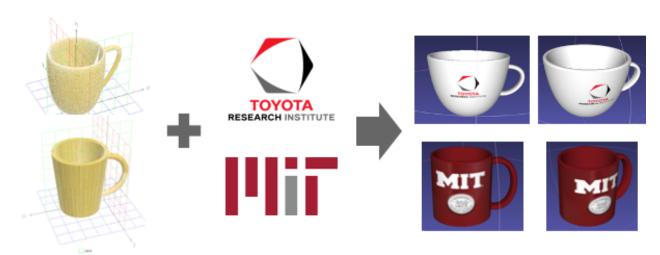


#### **Distributional Robustness**

We have parameterized simulations to study distributional robust / distribution shift.

- Parameterized environments (lighting conditions, etc)
- Carefully parameterized procedural mugs!

• ...









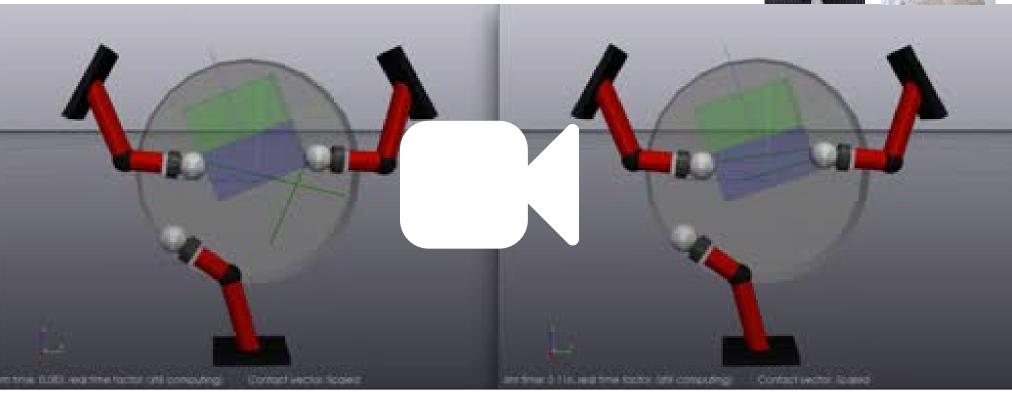
FINGER PIVOTING

SLIDING

FINGER GAITING









Releasing all of these as a part of my fall manipulation class at MIT (which is open and online).

https://people.csail.mit.edu/russt/uploads/iiwa.html

## Summary

How well is control working in robotics today?

- A few core quesitons/challenges
  - What role can simulation play?
  - Why/when does gradient-based policy search work?
  - Parameterizations/algorithms from control.
  - RL in the rare-event regime.
- Challenge problem instances
  - Plates, planar gripper, Raibert's hopper, onions, shoe laces...

https://groups.csail.mit.edu/locomotion/6-881-website/data/intro.html

Click here (on this slide)

or from Ch.1 at http://manipulation.mit.edu

https://groups.csail.mit.edu/locomotion/6-881-website/data/intro.html



or from Ch.1 at http://manipulation.mit.edu

You will need to rerun this cell if you restart the kernel, but it should be fast because the machine will already have drake installed.



```
import importlib
import sys
from urllib.request import urlretrieve

# Install drake.
if 'google.colab' in sys.modules and importlib.util.find_spec('pydrake') is None:
    version='20200901'
```