

### Logic and Algebras for Cloud Computing

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## Sea Changes in Computing

#### Supercomputers

#### Minicomputers





Cray-1, 1976

PDP-11, 1970



#### Smart Phones





#### iPhone, 2007

#### Macintosh, 1984



### New Platform + New Language = Innovation



PDP-11, 1970

#### Smart Phones





#### Macintosh, 1984









### The Big Question

How will folks program the cloud? In a way that fosters unexpected innovation

Autoscaling makes it harder!

Today's compilers don't address distributed concerns

## Programming the Cloud: A Grand Challenge for Computing



## Ted Codd Turing Award 1981

# Formalize specification; automate implementation.

A.C.



## Long-Running Agendas, Recent Trends

### Declarative Networking

### Relational Machine Learning

### Compiler Analysis



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### Long-Running Agendas, Recent Trends

### Declarative Networking

### Relational Machine Learning

### Compiler Analysis



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# Trend: Logic $\rightarrow$ Algebra Semi-Rings





## Declarative Programming for the Cloud

The cloud was invented to hide how computing resources are laid out and how computations are executed.

**Relational databases were invented** to hide how data is laid out and how queries are executed.









## LLVM for the Cloud?

- A language/compiler/debugger that addresses distributed concerns!
  - Is my program consistent or will different machines disagree?
  - How can I partition state safely?
  - What failures can this tolerate and how many?
  - What data is going where and who can see it?
  - Tunable objective functions. Please optimize for:
    - \$\$, not latency.
    - 99'th percentile, not 95<sup>th</sup>
    - Etc.







COMPILER INFRASTRUCTURE



## LLVM for the Cloud?

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## Hydro

- A language/compiler/debugger that addresses distributed concerns!
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  - What failures can this tolerate and how many?
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    - 99'th percentile, not 95<sup>th</sup>
    - Etc.





### Hydro Stack

-620

Sequential Code Futures (e.g. Ray)



### Topics for Today (and WIP)

- Automatic Replication (of code and data)
  - Esp. "free" replication consistency sans coordination (CALM)
    - (algebraic CALM Theorem)
- Termination detection
  - Esp. "free" termination detection sans coordination (threshold morphisms and equivalences)
- Automatic partitioning (of code and data)
  - Esp. "free" partitioning parallel execution sans coordination (functional dependencies integrated into algebraic types)



And excellent performance! (vs hand-written C++)







### Language/Theory Work: 2010-15

#### **DEDALUS: Datalog in Time and Space**

### Formalism: **Dedalus**

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Peter Alvaro<sup>1</sup>, William R. Marczak<sup>1</sup>, Neil Conway<sup>1</sup>, Joseph M. Hellerstein<sup>1</sup>, David Maier<sup>2</sup>, and Russell Sears<sup>3</sup>

CALM Theorem: coordination in its place ✓ Consistency ⇔ Monotonicity

Image: Logic + Lattices w/stratified neg/agg, morphisms, semi-naïve eval on lattices, etc

Datalog Reloaded 2010

JMH PODS Keynote, 2010 Ameloot, et al PODS 2011 Ameloot et al. TODS 2016 Alvaro/Hellerstein CACM 2020

SOCC 2012

#### A Declarative Semantics for Dedalus

Peter Alvaro Tom J. Ameloot Joseph M. Hellerstein William Marczak Jan Van den Bussche

DOI:10.1145/336973

In distributed systems theory, CALM presents a result that delineates the frontier of the possible.

BY JOSEPH M. HELLERSTEIN AND PETER ALVARO

Keeping CALM: When Distributed Consistency Is Easy

ross many machines. Most scier tific computing and machine learning systems work in parallel across multiple processors. Even legacy desktop operating systems and applications ike spreadsheets and word processors are tightly integrated with distributed ackend services.

The challenge of building correct istributed systems is increasingly un gent, but it is not new. One traditional nswer has been to reduce this comlexity with memory consistency guar ees-assurances that accesses to memory (heap variables, database keys, and so on) occur in a controlled fashion lowever, the mechanisms used to enforce these guarantees-coordination pro tocols-are often criticized as barriers to high performance, scale, and availbility of distributed systems.

The high cost of coordination Coordination protocols enable auton mous, loosely coupled machines to ointly decide how to control basic beaviors, including the order of access to shared memory. These protocols are among the most clever and widely cited deas in distributed computing. Some well-known techniques include the Paxos<sup>33</sup> and Two-Phase Commit (2PC)<sup>25,3</sup> rotocols, and global barriers underly

» key insights

Coordination is often a limiting factor in system performance. While someti necessary for consistent outcomes

#### Logic and Lattices for Distributed Programming

DISTRIBUTED SYSTEMS ARE tricky. Multiple unreliable

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### Systems Work: 2015-2021

### Cloudburst: Stateful FaaS

Compartmentalized Paxos

Lineage Driven Fault Injection

Why-Across-Time Provenance

#### **Cloudburst: Stateful Functions-as-a-Service**

Vikram Sreekanti, Chenggang Wu, Xiayue Charles Lin, Johann Schleier-Smith, Joseph E. Gonzalez, Joseph M. Hellerstein, Alexey Tumanov<sup>†</sup> U.C. Berkeley, <sup>†</sup>Georgia Tech

#### Scaling Replicated State Machines with Compartmentalization

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Scaling Replicate

VLDB 2021

VLDB 2020



## Systems Highlight: Anna Key-Value Store

- KVS: Petri dish of distributed systems!
- "CALM" Semi-lattice Design
  - ▲ Monotonic  $\Rightarrow$  Freely Replicable (w/o coordination)
  - Update anywhere, gossip lazily
  - Zero concurrency control (locks, atomics, protocols)

#### Anna: A KVS For Any Scale

Chenggang Wu<sup>#1</sup>, Jose M. Faleiro<sup>\*2</sup>, Yihan Lin<sup>\*\*3</sup>, Joseph M. Hellerstein<sup>#4</sup>





#### **Autoscaling Tiered Cloud Storage in Anna**

Chenggang Wu, Vikram Sreekanti, Joseph M. Hellerstein

**VLDB 19** 





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### 2022 SIGMOD Jim Gray **Doctoral Dissertation Award**

ACM SIGMOD is pleased to present the 2022 SIGMOD Jim Gray Doctoral Dissertation Award to Chenggang Wu.





Chenggang Wu is Co-founder and CTO at Aqueduct, a SaaS startup building machine learning prediction infrastructure. He received his Ph.D. in 2020 from UC Berkeley, advised by Joseph M. Hellerstein. He is the recipient of best-of-conference citations for research appearing in both VLDB 2019 and ICDE 2018. He frequently serves as a PC member and a reviewer for conferences and journals such as SIGMOD, ICDE, VLDBJ, and TKDE. Chenggang's Ph.D. dissertation develops design principles for building serverless infrastructure that can achieve excellent performance seamless scalability, and rich consistency guarantees. The dissertation proposes two key ideas that are fundamental to achieving the combination of these goals: lattice-based coordination-free consistency, and LDPC (logical disaggregation with physical colocation). These ideas

#### Autoscaling Tiered Cloud Storage in Anna

Chenggang Wu, Vikram Sreekanti, Joseph M. Hellerstein

#### **VLDB 19**



### Examples of lattice composition

### Metadata "wrappers" for various replica consistency mechanisms



#### Last Writer Wins

Causal Consistency



## Anna KVS Performance + Consistency

Fast, especially under contention

- Up to 700x faster than Masstree and Intel TBB on multicore
- Up to 10x faster than Cassandra in a geo-deployment
- ▲ 350x the performance of DynamoDB for the same price

Hand-written in C++ for a Ph.D. dissertation. Implementation correct by assertion. Can we formalize and maintain speed?



### Formalisms for Distributed Correctness

- Desired: type system or compiler guarantee
- Starting from a "trusted base"
  - Basic semi-lattices, e.g.
    - Sets: (*P*(T), U)
    - Counters: ( $\mathbb{N}$ , max)
    - Composite semi-lattices, e.g.
      - KeyValueMap,
      - Product, LexicalProduct (when possible)
    - "Physical Algebra" of operators, e.g.
      - ∐, ×, filter, map, fold
      - scan, "network", mux, demux, etc.





### Anna in Hydroflow, a semi-lattice, -inspired dataflow lang (semi-lattice "query plans")

```
// Demux network inputs
network_recv = source_stream_serde(inbound)
   -> _upcast(Some(Delta))
   -> map(Result::unwrap)
   -> map(|(msg, addr)|
        KvsMessageWithAddr::from_message(msg, addr))
   -> demux_enum::<KvsMessageWithAddr>();
puts = network_recv[Put];
gets = network_recv[Get];
```

```
// Join PUTs and GETs by key, persisting the PUTs.
puts -> map(|(key, value, _addr)| (key, value)) -> [0]lookup;
gets -> [1]lookup;
lookup = join::<'static, 'tick>();
```

// Send GET responses back to the client address.
lookup

LICC// Join as a peer if peer\_server is set.

```
source_iter_delta(peer_server)
```

-> map(|peer\_addr| (KvsMessage::PeerJoin, peer\_addr))

-> network\_send;

```
// Peers: When a new peer joins, send them all data.
writes_store -> [0]peer_join;
peers -> [1]peer_join;
peer_join = cross_join()
    -> map(((key, value), peer_addr))
        (KvsMessage::PeerGossip { key, value }, peer_addr))
    -> network_send;
// Outbound gossip. Send updates to peers.
peers -> peer_store;
source_iter_delta(peer_server) -> peer_store;
peer_store = union() -> persist();
writes -> [0]outbound_gossip;
peer_store -> [1]outbound_gossip;
outbound_gossip = cross_join()
    // Don't send gossip back to same sender.
    -> filter(((_key, _value, writer_addr), peer_addr))
       writer_addr != peer_addr)
```

-> map(|((key, value, \_writer\_addr), peer\_addr)|
 (KvsMessage::PeerGossip { key, value }, peer\_addr))

```
-> network_send;
```



## In Hydroflow





# (64 vCPU, 256GB RAM,)





and and a

#### Original Anna KVS. C++ 2018 Amazon m4.16xlarge instances (64 vCPU, 256GB RAM,)



#### Anna KVS. Hydro 2023 GCP n2-standard-64 instances (64 vCPU, 256GB RAM)

High contention (zipf coefficient = 4)

Threads





and the

Hydro Anna Throughput High contention (zipf coefficient = 4)

Throughput (ops/s)





Hydro Anna (full replication) — Linear Trendline R<sup>2</sup> = 0.999

Threads

## Consistently Replicable

- At a glance!
- Sort of

and and



### A DBMS Lens on Cloud Programming



### A Classical DBMS Lens

Decreasing declarativity, increasing implementation detail

**Relational Calculus** 

=> Relational Algebra (SPJU...)



### => Physical Algebra (Scan, BtreeScan, Hashjoin, Sort, MergeJoin, etc.)







### Good News / Bad News on the state of affairs

- Good news: Dedalus is a "Relational calculus" for distributed programming Bad news: programmers don't like it. Can we leave the walled garden of logic? Functional/algebraic expressions are more palatable (ie. they're in Python)
- Good news: An Algebra for distributed updates: Semi-Lattices/CRDTs
  - Bad news: they define updates on state, but no queries/functions
- Also, we can't ignore the shifting "physical" properties of data in motion (Randomized) ordering, batching, duplication



## Ideally

Unify formalisms across Logic / Algebra / "Physical" Algebra

A Physical layer correctness proofs under network non-determinism

- Physical algebra rich enough to capture "typical reality"
- Correctness under replication, partitioning, batching, incrementalization
- Analysis of termination







### Algebras of Dataflow



## Semi-Lattices / CRDTs

### Batching of Messages = Associativity

Reordering of Messages = Comr

### Duplication of Messages = Idempotence

### Conflict-free Replicated Data Types

Marc Shapiro, INRIA & LIP6, Paris, France Nuno Preguiça, CITI, Universidade Nova de Lisboa, Portugal Carlos Baquero, Universidade do Minho, Portugal

Marek Zawirski, INRIA & UPMC, Paris, France

## (S, ⊔)

### = Commutativity



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About CRDTs	[177]										
Resources	Stéphane V	Weiss, Pa	asca	l Urso	o, an	d Pa	scal	Moll	i. Wo	ooki:	
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Implementations	pages 503512. Springer LNCS volume 4831. December										
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	Gérald Oster, Pascal Urso, Pascal Molli, and Abdessam Data consistency for P2P collaborative editing. In 20th Conference on Computer Supported Cooperative Work, C 2006, pages 259268. ACM, November 2006. [bib   DC Keywords: text-editing, WOOT										
	[179] Gérald Oster, Pascal Urso, Pascal Molli, and Abdessam Real time group editors without operational transform Research Report RR-5580, INRIA, May 2005. [bib   http Keywords: text-editing, WOOT										






# **CRDT Example: Shopping Cart**



#### SemiLattice: $(\mathcal{P}(I), \cup) \times (\mathcal{P}(I), \cup)$

#### **VLDB 2023**

#### Keep CALM and CRDT On

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## One can put a query language "on top" of this

#### Desiderata for queries over CRDT state

An expressive & intuitive query interface for programmers (Logic or Algebra or ...)

- Negation
- Recursion
- Classical query optimization e.g. operation reordering and distributivity
- Distributed optimizations



- Monotonicity analysis for replication
- Functional Dependency analysis for partitioning



#### CALM Theorem Revisited



# Challenge: Replica Consistency

Classic example: data replication

How do we know if they agree on the value of a mutable variable x?







#### Ensure that distant agents agree (or will agree) on common knowledge.

# Challenge: Replica Consistency

- Classic example: data replication
  - A How do we know if they agree on the value of a mutable variable x?
  - If they disagree now, what could happen later?
  - Split Brain divergence!
- We want to generalize to program outcomes
  - Independent of "data races" along the way



#### Ensure that distant agents agree (or will agree) on common knowledge.





# **Classical Solution: Coordination**

#### Global total order of operations

Expensive at every scale

When can we avoid?



#### via atomic instructions, locks, distributed protocols like Paxos and 2-phase commit, etc.





## Generational Shift to Reasoning at the App Level

20<sup>th</sup> Century Read/Write Access/Store Linearizability Serializability

. . .

worst-case assumptions



# Tired: Wired: Reasoning about memory access Reasoning about App Semantics

#### 21<sup>st</sup> Century

- Immutable State
- Monotonicity Analysis
- **Functional Dependencies** 
  - Data Provenance





# Big Queries: When? Why?

- When do I need Coordination?
- Why?
- No really: Why?

When is Coordination required?









-020

- WHICH PROGRAMS HAVE A COOLDINAT, ON - FREE IMPLEMENTATION!

- WHICH TROGMMS REQUIRE GOLDINATION?

A QUESTION OF COMPUTABILITY.





# Easy and Hard Questions

# Is anyone over 18?



# Who is the youngest?



## Easy and Hard Questions

# Is anyone over 18? $\exists x x > 18$



# Who is the youngest? $\exists x \forall y (x \leq y)$



## Easy and Hard Questions

# Is anyone over 18?

X > 18

Monofone



# Who is the person nobody is younger than?

Non-Monofone



# CALM: CONSISTENCY AS LOGICAL MONOTONICITY

### Theorem (CALM): A distributed program has a consistent, coordination-free distributed implementation if and only if it is monotonic.

Hellerstein JM. The Declarative Imperative:

Experiences and conjectures in distributed logic.

ACM PODS Keynote, June 2010

ACM SIGMOD Record, Sep 2010.

Ameloot TJ, Neven F, Van den Bussche J. Relational transducers for declarative networking.

*JACM*, Apr 2013.

Ameloot TJ, Ketsman B, Neven F, Zinn D. Weaker forms of monotonicity for declarative networking: a more fine-grained answer to the CALM-conjecture.

ACM TODS, Feb 2016.

Hellerstein, JM, Alvaro, P. Keeping CALM: When Distributed Consistency is Easy. CACM, Sept, 2020.



# Definitions

Monotonic: you know

Consistent: produces the same output regardless of data placement

Hence eventually consistent across replicas, runs, gossiping partitions, etc.

#### ▲ Coordination:

"Control" messages, as opposed to "Data" messages.

▲ Coordination-free: there is some partitioning of the data s.t. the query answer is reached

without communication



### More Detail

THEOREM 5.11. Let  $\mathcal{L}$  be a query language containing UCQ. For every query  $\mathcal{Q}$  that is expressible in *L*, the following are equivalent:

(1) Q can be distributedly computed by a coordination-free  $\mathcal{L}$ -transducer; (2)  $\mathcal{Q}$  can be distributedly computed by an oblivious  $\mathcal{L}$ -transducer; and, (3) Q is monotone. ANVdB JACM 2013

Oblivious: does not read /d or A// relations













#### Free Termination



# Semi-Lattices: CALM Algebra

- Semi-Lattice: <S, +>
  - Associative: x + (y + z) = (x + y) + z

Commutative: x + y = y + x

 $\blacksquare Idempotent: x + x = x$ 

Every semi-lattice corresponds to a partial order:

 $\checkmark x <= y \iff x + y = y$ 



CALM connection: monotonicity in the lattice's partial order







### Free Termination

- Without coordination, nodes don't know if they've seen the entire input What query results are certain regardless of future updates? Can we detect termination for arbitrary update and query functions?











# Free Termination Beyond Monotonicity







# Free Termination Beyond Monotonicity







### Automatic Partitioning



# HYDRO Stack

man -







#### HYDROLYSIS Compiler





# An optimizer for protocols like Paxos? Tricky!

#### 

#### THE ACM SIGOPS SOSP 2021 STUDENT RESEARCH COMPETITION GRADUATE STUDENT WINNER AWARD

is presented to

David Chu (UC Berkeley)

for their work on

Automatic Compartmentalization of Distributed Protocols





#### **Optimizing Distributed Protocols with Query Rewrites**

David Chu, Rithvik Panchapakesan, Shadaj Laddad, Lucky Katahanas<sup>†</sup>, Chris Liu, Kaushik Shivakumar, Natacha Crooks, Joseph M. Hellerstein, Heidi Howard<sup>‡</sup> UC Berkeley, Sutter Hill Ventures<sup>†</sup>, Microsoft<sup>‡</sup>





# Challenges in Optimizing Protocols like Paxos

- Many published Paxos variants are unrecognizably equivalent
- We won't try to synthesize these human-generated variants
- Goal: using simple correct optimizations, achieve excellent performance.
  - Aim to match performance of the human innovations
  - In a small, provably equivalent search space of programs



# Simple, Provable Equivalence

Two forms of "compartmentalization"



#### Scaling Replicated State Machines with Compartmentalization

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#### **VLDB 2021**

Hand-written in Scala, correct by assertion. How much can we formalize/automate?





# Mutually Independent Decoupling

#### C1 and C2 mutually independent

-0-0





## Monotonic Decoupling

#### Cland C2 mutually independent

#### C2 monotonic (persistent)



## Functional Decoupling

#### Cland C2 mutually independent

#### C2 monotonic (persistent)

#### C2 a pure function



### Partitioning Discovery

#### Parallel Disjoint Correctness

[Bruhati, Koutris, Schwentick, Dagstuhl 2020]

#### Co-Hash predicates in a single rule body

#### • P(A, B, C) :- R(A, B), S(B, C)



**Definition 4.1.** A distribution policy *D* over component *C* is *parallel disjoint correct* if for any fact *f* of *C*, for any two facts  $f_1, f_2$  in the proof tree of f,  $D(f_1) = D(f_2)$ .



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• P(A, B, C) :- R(A, B), S(B, C)

- Avoid re-partitioning across head-body dependencies
  - P(A, B, C) :- R(A, B), S(B, C)
  - T(A, C) :- P(A, B, C), Q(B, C)



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Co-Hash by Inverse Functional Dependency

▲ P(A, D) :- R(A, B), H(C, B), S(C, D)

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Given:  $h(c_1) = h(c_2) \Rightarrow$  same partition

 $(c_1 = c_2) \Rightarrow h(c_1) = h(c_2) \Rightarrow$  same partition





# Partitioning Discovery

- Parallel Disjoint Correctness
  - [Bruhati, Koutris, Schwentick, Dagstuhl 2020]
    - Co-Hash predicates in a single rule body
      - P(A, B, C) :- R(A, B), S(B, C)
    - Avoid re-partitioning across head-body dependencies
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- Co-Hash by Inverse Functional Dependency
  - ▲ P(A, D) :- R(A, B), H(C, B), S(C, D)

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### Beats SOTA Paxos implementations





# Halfway there!

Rules proven correct, provide desired wins

### Need:

- Cost model for an objective function
- Search techniques to find optimal rewritings

### E-graphs meet Query Optimizers

- See Max's prior talk on Egg and Egglog
- Very similar technologies!











## Open Questions



# Four Open Questions

- Can we build a unified theory for all this business?
- 2. What's a good type system for a physical algebra (Hydroflow)?
- 3. What role declarative languages in the era of generative AI?
- 4. What is time for? When should we spend time?







# 1. A Unifying Theory, Please?

- CRDTs are semi-lattices for monotonic update across time/space
- Dedalus has a model theoretic semantics of time/space
- CALM Theorem proved using relational transducers for time/space
- Distributed system time often discussed in order theory terms
- Programmers willing to embrace functional/algebraic dataflow
- People often want to reason about transactions
- Not to mention ... semi-rings!



# 2. Hydroflow Properties

- ▲ Stream *S* characterized by properties (V, O, P, T, M, @, X):
  - V: a multiset of *values*
  - O: a total order of arrival
  - P: a parenthesization (batching)
  - ▲ T: a type (possibly algebraic)
  - ▲ *M*: monotonicity relationship between  $\leq_{T}$  and *O*
  - ▲ *a: atomistic* or not, *i.e.* is each item an atom of T
  - ▲ X: are all pairs x, y of items exclusive, i.e. if  $z \leq_T x$ ,  $z \leq_T y$  then z = 0

### Operators act on properties

- Output invariant to input
- Output preserves input
- Output enforces property
  - Deterministically
  - Non-Deterministically





4. The Narrow Waist Between Generative Al and Reliable Infrastructure



# 4. What is Time for?

# "*Time is what keeps everything from happening at once.*" Ray Cummings, *The Girl in the Golden Atom, 1922*









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### path(X,Z) :- link(X,Y), path(Y,Z)

Pipeline Semi-Naïve Evaluation Loo, et al. SIGMOD 2006







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$$p@t+1:-p@t$$
  
Time proof of cycle

Time provides *local stratification* of cycles through negation (every proof tree has finite depth)

<text>





# Time In Distributed Systems is Semi-Lattice Based

- Lamport's Happens-Before: A Partial Order
  - Total-order per node (a "clock")
  - Message send precedes receive

- Lamport clock: a semi-lattice (N, max)
  - Provides Happens-Before relation

- ✓ Vector clock: a semi-lattice MapLattice(Id  $\Rightarrow$  (N, max))
  - Provides Happens-Before, Concurrent, Causal relations



https://newbiettn.github.io/2014/05/03/lamport-clock-vs-vector-clock/

# Time can be Immaterial

Wild assertion: systems folk often "pay too much" to track time.

Dedalus says time is irrelevant unless we cannot stratify, or we are awaiting a message

But details in the Dedalus paper do enforce causality of messages

Causal order is not needed for positive Datalog.

Can assert facts before their antecedents are known!

(E.g. during recovery).

A variant of the "CRON Conjecture", which was too broad.

Datalog 2.0, 2012

### On the CRON Conjecture

Tom J. Ameloot \* and Jan Van den Bussche



# How Many Clocks?

### Dedalus has one "clock" per node

Increment on "event", and to compute a cycle through negation

## Timely/Differential Dataflow: Chronomania?

E.g. using clocks to track async-but-monotonic iteration

 $\checkmark$  When/why do we employ a (N, max) semi-lattice wrapper?

Can a compiler decide this?





# Thank You! https://hydro.run

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