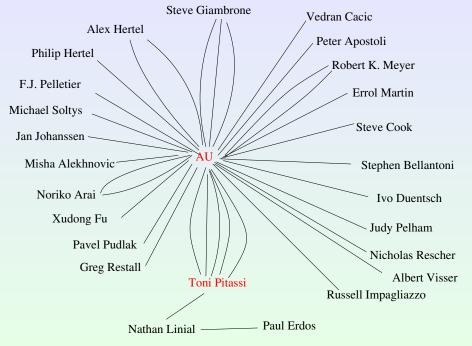
## My Collaborations with Toniann Pitassi

Alasdair Urquhart

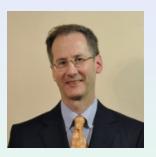
University of Toronto

March 2023





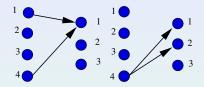




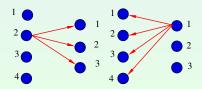
Toni Pitassi and Steve Bellantoni

#### The pigeonhole framework

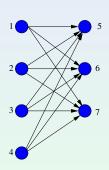
For the pigeonhole principle, we have  $(\neg P_1^1 \lor \neg P_1^4) \ldots$  etc.

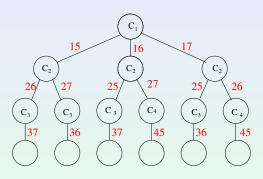


The assignments are the partial matchings between D and R. The positive clauses are of the form  $C_i = \bigvee \{P_j^i : j \in R\}$ , and  $C_j = \bigvee \{P_i^i : i \in D\}$ .



#### A pigeonhole decision tree

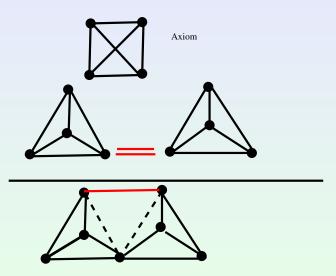




#### Second collaboration (with Toni and Russell)

Upper and lower bounds for tree-like cutting plane proofs.

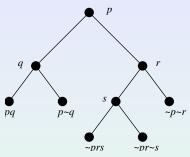
### The Hajos calculus





Fourth collaboration (with Toni and Noriko Arai)

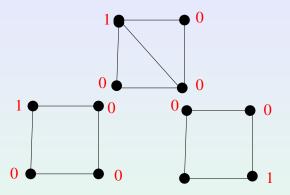
Complexity of analytic tableaux



These tree-based sets of clauses separate clausal tableaux from tree resolution. However, Fabio Massacci pointed out that if we formulate tableaux with binary decomposition, then we can get an exponential speedup. The paper with Toni and Noriko provides a nearly complete analysis of the possibilities.

# Fifth collaboration (with Jan Johannsen) Exponential separation between regular and general resolution.





Representing resolution as an operation on labelled graphs.

Problem: Prove or disprove that regular refutations are minimal for the Tseitin clauses.